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Accelerator physics colde comparison

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Collider Accelerator Department
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AD/AP/Tech.Note No. 8

ACCELERATOR DEVELOPMENT DEPARTMENT

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Accelerator Physics Technical Note No. 8

"ACCELERATOR PHYSICS CODE COMPARISON"

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October 1987

ACCELERATOR PHYSICS CODE COMPARISON

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ABSTRACT

We present a comparison between results obtained from accelerator physics codes used in the design and analysis of accelerators.

I. INTRODUCTION

Comparison of accelerator codes have been the topic of investigation and speculation by many (for sample notes on code comparisons see past issues of the Proceedings of Accelerator conferences). There are several beam optics programs that have been considered as standard codes for design and analysis of accelerators. For example, we have used programs SYNCH (as standard) and MAD for the design and analysis of the AGS - Booster and the proposed Super Conducting Super Collider (SSC).

In Section II, we Tabulate the parameters obtained from the recent Vax - Version of SYNCH* (Table I) for comparison with those obtained from program MAD - Versions 6.01 (Table II) and 4.03 (Table III) for the same sample (AGS - Booster) lattice. Comparison of the parameters in Tables I-III (e.g. items 6) shows a good agreement between the values of the tune shifts (Q_x , Q_z), lattice functions etc. for $\Delta(P)/P = 0$ but somewhat differs for $\Delta(P)/P \neq 0$. The difference become larger when the sextupoles (e.g. Eddy Current) are included in the input lattices since they are handled differently by these programs.

Table II, was obtained using the recent Vax Version of SYNCH* which includes the correction to the chromaticity calculation that was not included (and was inaccurate) in the CDC and previous VAX versions of SYNCH. The effect of the chromaticity calculation correction is two fold:

- 1) In finding the closed orbit for off momentum, CDC - Version produces the wrong bending angles except for zero - gradient rectangular magnet.
- 2) In computing chromaticity for bending magnets with nonzero exit and entrance angle one term in the chromaticity formula had the wrong sign, resulting in the wrong sextupole strength correction.

Thus, we recommend the use of the parameters obtained from the corrected Version of SYNCH for the design, analysis or code comparison, since the data produced from the CDC Version of SYNCH is inaccurate.

In conclusion, the parameters obtained from several beam optics programs agree for $\text{DELTA}(P)/P = 0$, but there still are differences in the results obtained from programs SYNCH [1] and MAD [2] for $\text{DELTA}(P)/P \neq 0$.

Acknowledgement

We thank Dr. E. Courant for the information on SYNCH and note that, this code comparison was made at his recommendation for the presentation at the Oct. 15, 1987 A.P. meeting.

* available in BNLDAG::DUA0:[PARSA1.SYNCH]SYNSEP.EXE

[1]. A. A. Garren, principal author.

[2]. F. C. Iselin, principal author.

TABLE I

SYNCH VAX - Version 987

SYNCH RUN BST

AGS-BOOSTER

14-OCT-87 15:40:17

1. DELTA(P)/P = -0.0100 :

CIRCUMFERENCE =	201.6976 M	QX =	4.87006	QY =	4.88460
RADIUS =	32.1012 M	QX' =	-5.03758	QY' =	-5.60968
(DS/S)/(DP/P) =	0.0393852	THETX =	6.28318530 RAD		
MAXIMA --- BETX(21) =	13.84289	THETY =	0.00000000 RAD		
DX(35) =	3.00980	GAMMA(TR) = (5.03887, 0.00000)		
MINIMA --- BETX(18) =	3.50410	BETY(18) =	13.65464		
DX(1) =	0.44193	BETY(47) =	3.63202		
MAXIMA XCO(1)=	-4.89001	YCO(52)=	0.00000		
MINIMA XCO(35)=	-29.66112	YCO(52)=	0.00000		

2. DELTA(P)/P = -0.00800 :

CIRCUMFERENCE =	201.7137 M	QX =	4.85992	QY =	4.87337
RADIUS =	32.1037 M	QX' =	-5.01543	QY' =	-5.54011
(DS/S)/(DP/P) =	0.0399131	THETX =	6.28318530 RAD		
MAXIMA --- BETX(21) =	13.84715	THETY =	0.00000000 RAD		
DX(35) =	2.99672	GAMMA(TR) = (5.00544, 0.00000)		
MINIMA --- BETX(18) =	3.51844	BETY(18) =	13.65237		
DX(52) =	0.46227	BETY(47) =	3.64632		
MAXIMA XCO(52)=	-3.99552	YCO(52)=	0.00000		
MINIMA XCO(35)=	-23.70182	YCO(52)=	0.00000		

3. DELTA(P)/P = -0.00600 :

CIRCUMFERENCE =	201.7300 M	QX =	4.84985	QY =	4.86229
RADIUS =	32.1063 M	QX' =	-4.99358	QY' =	-5.47090
(DS/S)/(DP/P) =	0.0404352	THETX =	6.28318530 RAD		
MAXIMA --- BETX(21) =	13.85156	THETY =	0.00000000 RAD		
DX(35) =	2.98438	GAMMA(TR) = (4.97302, 0.00000)		
MINIMA --- BETX(18) =	3.53273	BETY(18) =	13.65018		
DX(52) =	0.48223	BETY(47) =	3.66060		
MAXIMA XCO(52)=	-3.05855	YCO(52)=	0.00000		
MINIMA XCO(35)=	-17.75746	YCO(52)=	0.00000		

4. DELTA(P)/P = -0.00400:

CIRCUMFERENCE = 201.7465 M QX = 4.83984 QY = 4.85137
 QX' = -4.97202 QY' = -5.40198
 THETIX = 6.28318530 RAD
 THETY = 0.00000000 RAD
 GAMMA(TR)=(4.94155, 0.00000)
 MAXIMA --- BETX(21) = 13.85613 BETY(18) = 13.64807
 DX(35) = 2.97275 DY(52) = 0.00000
 MINIMA --- BETX(18) = 3.54698 BETY(47) = 3.67487
 DX(52) = 0.50183 DY(52) = 0.00000
 MAXIMA XCO(52)= -2.07984 YCO(52)= 0.00000
 MINIMA XCO(35)= -11.82661 YCO(52)= 0.00000

5. DELTA(P)/P = -0.00200

CIRCUMFERENCE = 201.7632 M QX = 4.82989 QY = 4.84061
 THETIX = 6.28318530 RAD
 THETY = 0.00000000 RAD
 GAMMA(TR)=(4.91098, 0.00000)
 RADIUS = 32.1116 M
 (DS/S)/(DP/P)= 0.0414633
 MAXIMA --- BETX(21) = 13.86084 BETY(18) = 13.64603
 DX(35) = 2.96178 DY(52) = 0.00000
 MINIMA --- BETX(18) = 3.56119 BETY(47) = 3.68911
 DX(52) = 0.52109 DY(52) = 0.00000
 MAXIMA XCO(52)= -1.06010 YCO(52)= 0.00000
 MINIMA XCO(35)= -5.90789 YCO(52)= 0.00000

6. DELTA(P)/P = 0.0000

CIRCUMFERENCE = 201.7800 M QX = 4.82000 QY = 4.83000
 QX' = -4.92970 QY' = -5.26488
 THETIX = 6.28318530 RAD
 THETY = 0.00000000 RAD
 GAMMA(TR)=(4.88124, 0.00000)
 RADIUS = 32.1143 M
 (DS/S)/(DP/P)= 0.0419701
 MAXIMA --- BETX(21) = 13.86571 BETY(52) = 13.64403
 DX(35) = 2.95145 DY(52) = 0.00000
 MINIMA --- BETX(18) = 3.57537 BETY(35) = 3.70334
 DX(1) = 0.54003 DY(52) = 0.00000
 MAXIMA XCO(52)= 0.00000 YCO(52)= 0.00000
 MINIMA XCO(35)= 0.00000 YCO(52)= 0.00000

7. DELTA(P)/P = 0.00200

CIRCUMFERENCE = 201.7970 M QX = 4.81017 QY = 4.81955
 QX' = -4.90893 QY' = -5.19663
 THETIX = 6.28318530 RAD
 THETY = 0.00000000 RAD
 GAMMA(TR)=(4.85229, 0.00000)
 RADIUS = 32.1170 M
 (DS/S)/(DP/P)= 0.0424725
 MAXIMA --- BETX(21) = 13.87071 BETY(52) = 13.65707
 DX(35) = 2.94173 DY(52) = 0.00000

MINIMA	--- BETX(18) =	3.58950	BETY(21) =	3.71581
DX(52) =	0.55866	DY(52) =	0.00000	
MAXIMA	XCO(35)=	5.89831	YCO(52)=	0.00000
MINIMA	XCO(52)=	1.09981	YCO(52)=	0.00000

8. DELTA(P)/P = 0.00400

CIRCUMFERENCE =	201.8142 M	QX =	4.80040	QY =	4.80925
		QX' =	-4.88841	QY' =	-5.12853
RADIUS =	32.1197 M	THETX =	6.28318530 RAD		
(DS/S)/(DP/P)=	0.0429707	THETY =	0.000000000 RAD		
MAXIMA	--- BETX(21) =	13.87587	BETY(52) =	13.67025	GAMMA(TR)=(4.82407, 0.00000)
DX(35) =	2.93261	DY(52) =	0.00000		
MINIMA	--- BETX(18) =	3.60361	BETY(21) =	3.72813	
DX(52) =	0.57700	DY(52) =	0.00000		
MAXIMA	XCO(35)=	11.78824	YCO(52)=	0.00000	
MINIMA	XCO(52)=	2.23873	YCO(52)=	0.00000	

9. DELTA(P)/P = 0.00600

CIRCUMFERENCE =	201.8316 M	QX =	4.79069	QY =	4.79911
		QX' =	-4.86812	QY' =	-5.06055
RADIUS =	32.1225 M	THETX =	6.28318530 RAD		
(DS/S)/(DP/P)=	0.0434650	THETY =	0.000000000 RAD		
MAXIMA	--- BETX(21) =	13.88116	BETY(52) =	13.68358	GAMMA(TR)=(4.79656, 0.00000)
DX(35) =	2.92405	DY(52) =	0.00000		
MINIMA	--- BETX(18) =	3.61768	BETY(21) =	3.74028	
DX(52) =	0.59506	DY(52) =	0.00000		
MAXIMA	XCO(35)=	17.67094	YCO(52)=	0.00000	
MINIMA	XCO(52)=	3.41617	YCO(52)=	0.00000	

10. DELTA(P)/P = 0.00800

CIRCUMFERENCE =	201.8492 M	QX =	4.78104	QY =	4.78913
		QX' =	-4.84806	QY' =	-4.99265
RADIUS=	32.1253 M	THETX =	6.28318530 RAD		
(DS/S)/(DP/P)=	0.0439557	THETY =	0.000000000 RAD		
MAXIMA	--- BETX(21) =	13.88659	BETY(52) =	13.69704	GAMMA(TR)=(4.76971, 0.00000)
DX(35) =	2.91603	DY(52) =	0.00000		
MINIMA	--- BETX(18) =	3.63171	BETY(21) =	3.75227	
DX(52) =	0.61285	DY(52) =	0.00000		
MAXIMA	XCO(35)=	23.54750	YCO(52)=	0.00000	
MINIMA	XCO(52)=	4.63157	YCO(52)=	0.00000	

11. $\Delta(P)/P = 0.01000$

CIRCUMFERENCE =	201.8669 M	QX =	4.77144	QY =	4.77930
		QX' =	-4.82823	QY' =	-4.92482
RADIUS =	32.1281 M	THETX =	6.28318530 RAD		
(DS/S)/(DP/P) =	0.0444431	THETY =	0.00000000 RAD		
MAXIMA	--- BETX(21) =	13.89216	BETY(52) =	13.71064	GAMMA(TR)=(4.74349, 0.00000)
DX(35) =	2.90853	DY(52) =	0.00000		
MINIMA	--- BETX(18) =	3.64572	BETY(21) =	3.76410	
DX(52) =	0.63039	DY(52) =	0.00000		
MAXIMA	XCO(35)=	29.41897	YCO(52)=	0.00000	
MINIMA	XCO(52)=	5.88440	YCO(52)=	0.00000	

END OF SYNCH RUN BST

TABLE II

'MAD" VERSION 6.01/03:

MAD6.01 OUTPUT FOR THE BOOSTER LATTICE WITHOUT SEXTUPOLES [SF, SD, SV=0]

1. For DELTA(P)/P = -0.01:

TOTAL LENGTH =	201.780000	QX =	4.869524	QY =	4.882689
		QX' =	-4.974135	QY' =	-5.314419
ALFA =	0.397978E-01	BETAX(MAX) =	13.981287	BETAY(MAX) =	13.795012
GAMMA(TR) =	5.012688	DX(MAX) =	3.039104	DY(MAX) =	0.000000
		XCO(MAX) =	29.938897	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	16.640292	YCO(R.M.S.) =	0.000000

2. FOR DELTA(P)/P = -0.008000:

TOTAL LENGTH =	201.780000	QX =	4.859582	QY =	4.872144
		QX' =	-4.965049	QY' =	-5.304147
ALFA =	0.402414E-01	BETAX(MAX) =	13.957912	BETAY(MAX) =	13.764037
GAMMA(TR) =	4.984983	DX(MAX) =	3.020217	DY(MAX) =	0.000000
		XCO(MAX) =	23.879696	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	13.311186	YCO(R.M.S.) =	0.000000

3. FOR DELTA(P)/P = -0.006000:

TOTAL LENGTH =	201.780000	QX =	4.849659	QY =	4.861603
		QX' =	-4.956066	QY' =	-5.294075
ALFA =	0.406801E-01	BETAX(MAX) =	13.934668	BETAY(MAX) =	13.733463
GAMMA(TR) =	4.958030	DX(MAX) =	3.002033	DY(MAX) =	0.000000
		XCO(MAX) =	17.857561	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	9.983220	YCO(R.M.S.) =	0.000000

4. FOR DELTA(P)/P = -0.004000:

TOTAL LENGTH =	201.780000	QX =	4.839755	QY =	4.851065
		QX' =	-4.947183	QY' =	-5.284184
ALFA =	0.411142E-01	BETAX(MAX) =	13.911553	BETAY(MAX) =	13.703278
GAMMA(TR) =	4.931783	DX(MAX) =	2.984527	DY(MAX) =	0.000000
		XCO(MAX) =	11.871112	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	6.655764	YCO(R.M.S.) =	0.000000

5. FOR DELTA(P)/P = -0.002000:

TOTAL LENGTH =	201.780000	QX =	4.829868	QY =	4.840531
		QX' =	-4.938396	QY' =	-5.274457
ALFA =	0.415441E-01	BETAX(MAX) =	13.888567	BETAY(MAX) =	13.673471
GAMMA(TR) =	4.906198	DX(MAX) =	2.967673	DY(MAX) =	0.000000

XCO(MAX) =	5.919019	YCO(MAX) =	0.000000
XCO(R.M.S.) =	3.328215	YCO(R.M.S.) =	0.000000

6. FOR DELTA(P)/P = 0.000000:

TOTAL LENGTH =	201.780000	QX =	4.820000	QY =	4.829999
		QX' =	-4.929702	QY' =	-5.264883
ALFA =	0.419701E-01	BETAX(MAX) =	13.865707	BETAY(MAX) =	13.644032
GAMMA(TR) =	4.881238	DX(MAX) =	2.951449	DY(MAX) =	0.000000
		XCO(MAX) =	0.000000	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	0.000000	YCO(R.M.S.) =	0.000000

7. FOR DELTA(P)/P = 0.002000:

TOTAL LENGTH =	201.780000	QX =	4.810150	QY =	4.819471
		QX' =	-4.921099	QY' =	-5.255452
ALFA =	0.423924E-01	BETAX(MAX) =	13.842974	BETAY(MAX) =	13.629735
GAMMA(TR) =	4.856865	DX(MAX) =	2.935830	DY(MAX) =	0.000000
		XCO(MAX) =	5.887179	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	3.329428	YCO(R.M.S.) =	0.000000

8. FOR DELTA(P)/P = 0.004000:

TOTAL LENGTH =	201.780000	QX =	4.800317	QY =	4.808946
		QX' =	-4.912583	QY' =	-5.246156
ALFA =	0.428113E-01	BETAX(MAX) =	13.820366	BETAY(MAX) =	13.615495
GAMMA(TR) =	4.833046	DX(MAX) =	2.920797	DY(MAX) =	0.000000
		XCO(MAX) =	11.743710	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	6.660591	YCO(R.M.S.) =	0.000000

9. FOR DELTA(P)/P = 0.006000:

TOTAL LENGTH =	201.780000	QX =	4.790501	QY =	4.798424
		QX' =	-4.904152	QY' =	-5.236988
ALFA =	0.432270E-01	BETAX(MAX) =	13.797883	BETAY(MAX) =	13.601316
GAMMA(TR) =	4.809750	DX(MAX) =	2.906327	DY(MAX) =	0.000000
		XCO(MAX) =	17.570742	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	9.993989	YCO(R.M.S.) =	0.000000

10. FOR DELTA(P)/P = 0.008000:

TOTAL LENGTH =	201.780000	QX =	4.780703	QY =	4.787905
		QX' =	-4.895804	QY' =	-5.227943
ALFA =	0.436398E-01	BETAX(MAX) =	13.775524	BETAY(MAX) =	13.587203
GAMMA(TR) =	4.786948	DX(MAX) =	2.892402	DY(MAX) =	0.000000
		XCO(MAX) =	23.369382	YCO(MAX) =	0.000000
		XCO(R.M.S.) =	13.330097	YCO(R.M.S.) =	0.000000

11. FOR DELTA(P)/P = 0.010000 :

TOTAL LENGTH = 201.780000 QX = 4.770922 QY = 4.777389
 QX' = -4.887536 QY' = -5.219016
 ALFA = 0.440499E-01 BETAX(MAX) = 13.753287 BETAY(MAX) = 13.573160
 GAMMA(TR) = 4.764614 DX(MAX) = 2.879003DY(MAX) = 0.000000
 XCO(MAX) = 29.140701 YCO(MAX) = 0.000000
 XCO(R.M.S.) = 16.669372 YCO(R.M.S.) = 0.000000

TABLE III

"MAD" VERSIN 4.03

MAD403 OUTPUT FOR AGS BOOSTER LATTICE WITHOUT SEXTUPOLES [SF,SD,SV=0]

1. FOR DELTA(P)/P = -0.010000 :

TOTAL LENGTH = 201.780000 QX = 4.869536 QY = 4.882249
 QX' = -4.974658 QY' = -5.291287
 ALFA = 0.397978E-01 BETAX(MAX) = 13.981250 BETAY(MAX) = 13.796343
 GAMMA(TR) = 5.012688 DX(MAX) = 3.039108 DY(MAX) = 0.000000

2. FOR DELTA(P)/P = -0.008000 :

TOTAL LENGTH = 201.780000 QX = 4.859589 QY = 4.871899
 QX' = -4.965323 QY' = -5.292399
 ALFA = 0.402414E-01 BETAX(MAX) = 13.957891 BETAY(MAX) = 13.764777
 GAMMA(TR) = 4.984983 DX(MAX) = 3.020219 DY(MAX) = 0.000000

3. FOR DELTA(P)/P = -0.006000 :

TOTAL LENGTH = 201.780000 QX = 4.849663 QY = 4.861481
 QX' = -4.956193 QY' = -5.288761
 ALFA = 0.406801E-01 BETAX(MAX) = 13.934657 BETAY(MAX) = 13.733831
 GAMMA(TR) = 4.958030 DX(MAX) = 3.002034 DY(MAX) = 0.000000

4. FOR DELTA(P)/P = -0.004000 :

TOTAL LENGTH = 201.780000 QX = 4.839756 QY = 4.851017
 QX' = -4.947229 QY' = -5.282268
 ALFA = 0.411142E-01 BETAX(MAX) = 13.911549 BETAY(MAX) = 13.703424
 GAMMA(TR) = 4.931783 DX(MAX) = 2.984527 DY(MAX) = 0.000000

5. FOR DELTA(P)/P = -0.002000 :

TOTAL LENGTH = 201.780000 QX = 4.829869 QY = 4.840520
 QX' = -4.938405 QY' = -5.274067
 ALFA = 0.415441E-01 BETAX(MAX) = 13.888566 BETAY(MAX) = 13.673504
 GAMMA(TR) = 4.906198 DX(MAX) = 2.967673 DY(MAX) = 0.000000

6. FOR DELTA(P)/P = 0.000000 :

TOTAL LENGTH = 201.780000 QX = 4.820000 QY = 4.829999
 QX' = -4.929702 QY' = -5.264883
 ALFA = 0.419701E-01 BETAX(MAX) = 13.865707 BETAY(MAX) = 13.644032
 GAMMA(TR) = 4.881238 DX(MAX) = 2.951449 DY(MAX) = 0.000000

7. FOR DELTA(P)/P = 0.002000:

TOTAL LENGTH = 201.780000 QX = 4.810150 QY = 4.819462
 QX' = -4.921105 QY' = -5.255196
 ALFA = 0.423924E-01 BETAX(MAX) = 13.842973 BETAY(MAX) = 13.629764
 GAMMA(TR) = 4.856865 DX(MAX) = 2.935830 DY(MAX) = 0.000000

8. BEAM DELTA(P)/P = 0.004000:

TOTAL LENGTH = 201.780000 QX = 4.800318 QY = 4.808910
 QX' = -4.912603 QY' = -5.245338
 ALFA = 0.428113E-01 BETAX(MAX) = 13.820363 BETAY(MAX) = 13.615603
 GAMMA(TR) = 4.833046 DX(MAX) = 2.920797 DY(MAX) = 0.000000

9. FOR DELTA(P)/P = 0.006000:

TOTAL LENGTH = 201.780000 QX = 4.790504 QY = 4.798347
 QX' = -4.904188 QY' = -5.235560
 ALFA = 0.432270E-01 BETAX(MAX) = 13.797876 BETAY(MAX) = 13.601548
 GAMMA(TR) = 4.809750 DX(MAX) = 2.906328 DY(MAX) = 0.000000

10. FOR DELTA(P)/P = 0.008000 :

TOTAL LENGTH = 201.780000 QX = 4.780707 QY = 4.787774
 QX' = -4.895849 QY' = -5.226062
 ALFA = 0.436398E-01 BETAX(MAX) = 13.775511 BETAY(MAX) = 13.587601
 GAMMA(TR) = 4.786948 DX(MAX) = 2.892404 DY(MAX) = 0.000000

11. FOR DELTA(P)/P = 0.010000 :

TOTAL LENGTH = 201.780000 QX = 4.770928 QY = 4.777190
 QX' = -4.887580 QY' = -5.21701
 ALFA = 0.440499E-01 BETAX(MAX) = 13.753267 BETAY(MAX) = 13.573763
 GAMMA(TR) = 4.764614 DX(MAX) = 2.879005 DY(MAX) = 0.000000
