

Momentum Collimation at Q9

S. Peggs

November 1995

Collider Accelerator Department
Brookhaven National Laboratory

U.S. Department of Energy

USDOE Office of Science (SC)

Notice: This technical note has been authored by employees of Brookhaven Science Associates, LLC under Contract No. DE-AC02-76CH00016 with the U.S. Department of Energy. The publisher by accepting the technical note for publication acknowledges that the United States Government retains a non-exclusive, paid-up, irrevocable, world-wide license to publish or reproduce the published form of this technical note, or allow others to do so, for United States Government purposes.

DISCLAIMER

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or any third party's use or the results of such use of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof or its contractors or subcontractors. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

Momentum collimation at Q9

S. Peggs, G.F. Dell

Introduction

Gold ions are prone to diffusion in transverse and longitudinal phase space, through Intra Beam Scattering (IBS). For example, the transverse emittance of a gold bunch is expected to increase to 40π microns during a 10 hour store, while the longitudinal emittance rises to fill and overflow the bucket of the 197 MHz RF system in which it is contained. If no remedial action is taken, gold ions that escape the RF bucket will streamline around the ring to give an approximately constant longitudinal background density. These particles will contribute to unwanted background in the experiments. If there is a sufficient number of them in the abort gap, they may cause magnet quenches when the beam is aborted - or dumped at the end of a fill.

This paper considers two simultaneous remedial actions:

1. Turn on the 28 MHz accelerating RF system during storage. This creates 360 "macro-buckets", each one surrounding 7 storage buckets like peas in a pod. Gold ions that escape a storage bucket remain confined in the macro-bucket, where IBS diffusion rates are greatly reduced.
2. Remove gold ions that approach the macro-bucket separatrix with a momentum collimator installed next to a Q9 quadrupole, in a drift space where the horizontal dispersion is large. Only those Q9 locations where the beam and the collimator spray are moving away from the Interaction Point (IP), towards Q10, are sensible. Five such locations in each ring have vacant drifts that are, in principle, available for the installation of a momentum collimator. One location, downstream of the 6 o'clock IP, is already occupied by injection kicker modules.

Macro-buckets

The small oscillation synchrotron tune is given by

$$Q_{s0} = \left(\frac{h\eta_T}{2\pi} \cdot \frac{Z}{A} \cdot \frac{eV}{m_0 c^2 \gamma} \cdot \frac{1}{\beta^2} \right)^{\frac{1}{2}} \quad (1)$$

where V is the voltage of a single RF system with harmonic number h , η_T is the slip factor, Z and A are the charge and nucleon counts of an ion with an average mass of m_0 per nucleon, and β and γ are relativistic factors. By direct analogy with transverse phase space nomenclature, the aspect ratio of a small bunch in longitudinal phase space ($z, \Delta p/p$) is given by the longitudinal beta function β_z ,

$$\beta_z \equiv \frac{\sigma_z}{\sigma_p/p} = \frac{C}{2\pi} \cdot \frac{\eta_T}{Q_{s0}} \quad (2)$$

where C is the machine circumference and σ_z is the rms bunch length. Finally, the maximum value of the off-momentum parameter $\delta = \Delta p/p$ on the separatrix is given by

$$\hat{\delta}_{sep} = \frac{\lambda}{\pi \beta_z} = \frac{2Q_{s0}}{h\eta_T} \quad (3)$$

where $\lambda = C/h = 3833.845/(360 \times 7) = 1.521\text{m}$ is the RF wavelength of the storage system.

The case of interest is gold ions in storage at top energy, when $Z = 79$, $A = 197$, $m_0 = 0.93113 \text{ GeV}/c^2$, $\gamma = 108.395$, and $\eta_T = 1.823 \times 10^{-3}$. In this case

$$Q_{s0} = 4.174 \times 10^{-3} \left(\frac{V_{197}[\text{MV}]}{6.0} \right)^{\frac{1}{2}} \quad (4)$$

$$\hat{\delta}_{sep} = 1.818 \times 10^{-3} \left(\frac{6.0}{V_{197}[\text{MV}]} \right)^{\frac{1}{2}}, \quad (5)$$

where the dependence on voltage is explicitly referred to $V_{197} = 6.0 \text{ MV}$, the nominal value that is implicitly assumed from here on.

A concise description of the double RF system is given by a Hamiltonian that is parameterized by the storage RF quantities Q_{s0} and $\hat{\delta}_{sep}$

$$H(p, \phi) = (2\pi Q_{s0})^2 \left[\frac{1}{2} p^2 + (1 - \cos(\phi)) + 7v(1 - \cos(\frac{\phi}{7})) \right] \quad (6)$$

One canonical coordinate is ϕ , the RF phase of the 197 MHz (storage) system, and the other is p , the scaled off-momentum parameter

$$p = 2 \left(\delta / \hat{\delta}_{sep} \right) \quad (7)$$

The equations of motion of this system are

$$\frac{dp}{dt} \equiv -\frac{\partial H}{\partial \phi} = -(2\pi Q_{s0}) \left[\sin(\phi) + v \sin\left(\frac{\phi}{7}\right) \right] \quad (8)$$

$$\frac{d\phi}{dt} \equiv \frac{\partial H}{\partial p} = (2\pi Q_{s0}) p \quad (9)$$

where time, t , is measured in turns. Equation 8 confirms that v is the scaled voltage of the 28 MHz (acceleration) system

$$v = \frac{V_{28}}{V_{197}} \leq \frac{0.8}{6.0} = 0.133 \quad (10)$$

It has a maximum value of $v = 0.133$ (when $V_{28} = 0.8$ MV) that may only be possible in pulsed, and not in CW, operation [1]. It is reasonable and conservative to expect a CW value of $v = 0.1$.

Inspection of the equations of motion in the limit of small ϕ shows that

$$Q_{s0}(v) = Q_{s0}(0) \left(1 + \frac{v}{7} \right)^{\frac{1}{2}} \quad (11)$$

so that the synchrotron tune increases only slightly, by less than 2% at most. The momentum width of the macro-bucket separatrix is obtained by equating the value of the Hamiltonian $H(p, \phi)$ at its unstable fixed point, with the value at the widest part of the bucket

$$H(0, \pm 7\pi) = H(\hat{p}, 0) \quad (12)$$

and solving for \hat{p} . Substitution of Eqns 6 and 7 reveals that

$$\hat{\delta}_{sep}(v) = \hat{\delta}_{sep}(0) (1 + 7v)^{\frac{1}{2}} \leq 2.526 \times 10^{-3} \quad (13)$$

showing that the macro-bucket can be as much as 39% wider in momentum than a naked storage bucket. Figure 1 displays the longitudinal phase space behavior observed by the simulation code TEAPOT when $v = 0.133$, independently confirming the quantitative predictions made above.

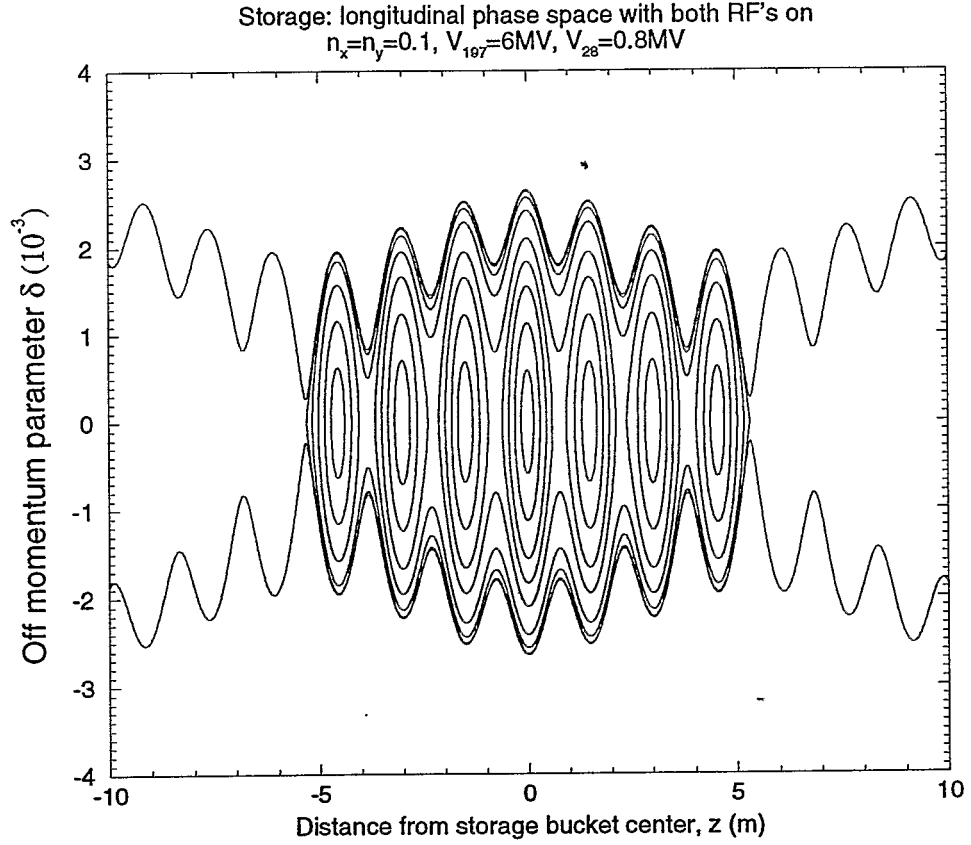


Figure 1: Longitudinal phase space, as observed with TEAPOT, when $V_{28} = 0.8$ MV and $V_{197} = 6.0$ MV. A “macro-bucket” of momentum width ± 0.0025 surrounds 7 storage buckets, each approximately ± 0.0018 wide.

Momentum collimation

Suppose that a collimator is inserted from the radial outside of the beam to a (positive) displacement of \hat{x} . A particle will just scrape the collimator, at some time in its history, if

$$n_x \sigma_x + \eta_x \hat{\delta} = \hat{x} \quad (14)$$

where n_x is the horizontal betatron amplitude measured in units of the beam size σ_x , the horizontal dispersion is η_x , and $\hat{\delta}$ is the maximum value of the off-momentum parameter. This equation can be rewritten to explicitly show how the maximum betatron amplitude depends on $\hat{\delta}$,

$$n_x(\hat{\delta}) = n_x(0) - \frac{\eta_x}{\sigma_x} \hat{\delta} \quad (15)$$

where the parameter $n_x(0)$ is just the collimator offset measured in units of the beam size. If the goal of momentum collimation is to remove all particles with a momentum greater than some value $\hat{\delta}_{coll}$, then

$$n_x(\hat{\delta}_{coll}) = 0 \quad (16)$$

so that

$$n_x(0) = \frac{\eta_x}{\sigma_x} \hat{\delta}_{coll} \quad (17)$$

For momentum collimation to be practical, the value of $n_x(0)$ must be large enough that only the inconsequential betatron tails of the on-momentum beam are scraped.

In the case of gold ions stored for 10 hours in RHIC, the normalized transverse emittance is taken to be $\epsilon = 40\pi\mu\text{m}$, so that

$$\sigma_x = \sqrt{\frac{\beta_x \epsilon}{6\pi(\beta\gamma)}} = \sqrt{\frac{\beta_x [\text{m}]}{16.26}} [\text{mm}] \quad (18)$$

yielding

$$n_x(0) = 4.03 \times 10^3 \frac{\eta_x [\text{m}]}{\sqrt{\beta_x [\text{m}]} } \hat{\delta}_{coll} \quad (19)$$

This shows the important result that $\eta_x/\sqrt{\beta_x}$ is the fundamental optical “quality factor”, of paramount importance when deciding where to place a momentum collimator. It is approximately constant in the dispersion matched FODO cells of the RHIC arcs, but falls to approximately zero in the dispersion suppressed interaction regions.

Table 1 shows the design optical parameters at potential momentum collimation locations, near Q9 quadrupoles downstream of interaction points with

Name	s [m]	$\mu_x/2\pi$	β_x [m]	η_x [m]	$\eta_x/\sqrt{\beta_x}$ [m ^{1/2}]
clock6	0.000	0.000	0.97	0.005	0.005
q3o6	35.830	0.246	506.95	0.470	0.021
q4ot6	74.175	0.691	24.61	0.097	0.020
qda6	142.347	1.273	10.73	0.777	0.237
INJECTION KICKER					
erds	150.974	1.354	29.38	1.390	0.256
ds	153.924	1.368	39.91	1.617	0.256
qf	157.163	1.379	48.83	1.795	0.257
clock8	639.445	5.239	0.97	0.005	0.005
q3i8	675.275	5.485	1354.43	-0.768	-0.021
q4it8	713.620	5.509	46.17	-0.273	-0.040
qfa8	781.717	5.929	49.74	1.658	0.235
F LOCATION (1 m)					
erds	790.339	5.973	19.68	1.167	0.263
ds	793.289	6.002	13.65	1.017	0.275
qd	796.523	6.047	10.59	0.919	0.282
clock10	1277.948	9.411	10.15	-0.016	-0.005
q3o10	1313.778	9.621	51.90	-0.023	-0.003
q4ot10	1352.123	9.951	37.32	0.240	0.039
qda10	1420.295	10.651	10.61	0.822	0.252
D LOCATION (10 m)					
erds	1428.923	10.732	29.51	1.452	0.267
ds	1431.872	10.746	40.19	1.685	0.266
qf	1435.112	10.757	49.27	1.866	0.266
clock12	1917.393	14.581	9.90	0.017	0.005
q3i12	1953.223	14.792	147.30	0.244	0.020
q4it12	1991.568	14.925	17.85	-0.067	-0.016
qfa12	2059.666	15.365	48.69	1.597	0.229
F LOCATION (10 m)					
erds	2068.288	15.411	19.53	1.154	0.261
ds	2071.237	15.439	13.68	1.020	0.276
qd	2074.471	15.484	10.78	0.941	0.287

Table 1: Design optics near potential momentum collimator locations and other places of interest, in the Blue ring. Locations near F and D Q9 quads, and near $\beta^* = 1$ and 10 m interaction points, are all roughly equivalent in $\eta_x/\beta_x^{1/2}$.

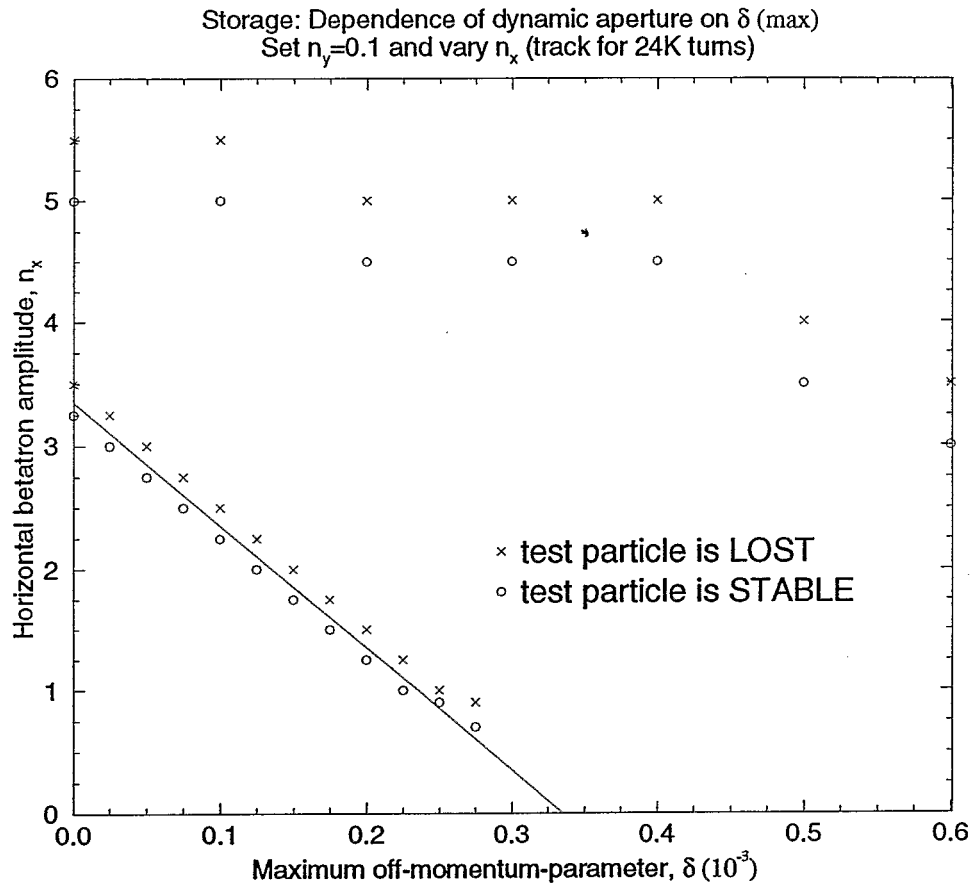


Figure 2: RHIC dynamic aperture after about 100 synchrotron periods, in a storage lattice with all errors turned on and all corrections applied. The lower solid line applies when a 4 mm aperture restriction is placed at Q9. The upper line shows the natural dynamic aperture, dominated by the triplet quadrupoles. In all cases the vertical betatron amplitude is $n_y = 0.1$, while $V_{197} = 6.0$ MV and $V_{28} = 0.8$ MV.

low and high β^* values [2, 3]. All potential locations - whether F or D, whether $\beta^* = 1$ m or 10 m - are roughly equivalent from an optical perspective. Taking a typical Q9 value of $\eta_x/\sqrt{\beta_x} = 0.25$ [m^{1/2}], then

$$n_x(0) = 10^3 \hat{\delta}_{coll} \quad (20)$$

a fortuitously simple result. Finally, if momentum collimation is performed at the macro-bucket separatrix when $v = 0.133$, then

$$n_x(0) = 10^3 \hat{\delta}_{sep} = 2.5 \quad (21)$$

This shows that the collimation of on-momentum particles is NOT comfortably far off in the betatron tails, at least for gold ions with an emittance of 40π microns. Figure 2 shows results from a TEAPOT simulation of momentum collimation, with a physical aperture of 4 mm asserted at the Q9 quadrupole downstream of the 8 o'clock IP. These results confirm the simple picture given above, although there are signs that nonlinear and chromatic effects are not completely negligible.

Conclusions

Macro-buckets created by turning on the 28 MHz RF system may be used to trap gold ions that diffuse out of the storage buckets.

A momentum scraper at any one of five downstream Q9 locations in each ring may be used to remove gold ions that approach the macro-bucket separatrix. Unfortunately, these locations require the added expense of warm-to-cold transitions.

A momentum collimator near Q9 reaches uncomfortably close - about $2.5\sigma_x$ - to the betatron core of on-momentum gold ions, when the transverse emittance is at its largest, $\epsilon = 40\pi$ microns. A modest improvement in optical or RF parameters - raising $\hat{\delta}_{sep}$, raising η_x , or lowering β_x - would move Q9 momentum collimation from "satisfactory" to "solid" performance.

A Q9 momentum collimator would NOT be efficient as a secondary betatron collimator, in conjunction with a primary betatron collimator just upstream, between Q3 and Q4. Even though the betatron phase advance is near optimum, the completely different values of $\eta/\sqrt{\beta_x}$ at the two locations makes the combination very ill-matched [4].

References

- [1] M. Brennan, private communication.
- [2] The design optics data were taken from the file
/rap/Holy_Lattice/Blue/twiss_store.asc .
- [3] S. Tepikian, "Twiss Functions and Beam Sizes of the RHIC Insertion",
RHIC/AP/25, 1994.
- [4] M. Seidel, "The Proton Collimation System of HERA", PhD thesis, DESY
94-103, 1994.