

BNL-101548-2014-TECH RHIC/PG/5;BNL-101548-2013-IR

Definition Of Beam Emittances

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November 1983

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U.S. Department of Energy

USDOE Office of Science (SC)

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RHIC-PG-5

DEFINITION OF BEAM EMITTANCES

A.G. Ruggiero

(BNL, November 20, 1983)

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Betatron Emittances

that the beam has a gamissian Assume distribution in both 2 and 2' (Hor V). A beam management profile measurement will give the rms width o De rms emittance is den defined as $\mathcal{E}_{\rm SMS} = 2\pi \frac{\sigma^2}{\beta_{\rm Z}}$ udere B2 is the corresponding lattice amplitude value udere the beam profile is taken. The following emittances $\mathcal{E} = 4\pi \frac{\sigma^2}{\beta_2} \quad \text{and} \quad 5\pi \frac{\sigma^2}{\beta_2}$

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are commonly used in Europe and USA -The primer define a 90% beam contour, the latter 95% of the beam. For questime requirement consideration I propose the definition that corresponds to 95% of the beam (1) $\varepsilon = 6\pi \frac{\delta^2}{\beta_2}$ The Jackse To will always be left explainly Normalized Emillance De emittance défined by () is not an invariant. The normalised emittance En is defined so that the actual emittance & at some brann energy the described by the rela divisitie parameters B and y is given by $\mathcal{E} = \frac{\varepsilon_N}{\beta \gamma}$ (2)

First heavy ions and protons En is a truly in variant provided dilution and diffusions are not introduced by external means -We will use definition (2) for heavy ions as well as for protour-Also observe that definition (2) is indepen-dent of the charge status of the ion. In fact also nder the ion goes through a stripping fill, as long & and y do not vary so its momentum will not vary and the emit tance is not effected by the stripping (except by possible scattering which cause transfer from logitudical & the transverse momentum) Other Relations Instead of the smis midth o we could measure the rms angle Q in 2', then we also have $\mathcal{E} = 6\pi \frac{\sigma^2}{\beta_2}$ (3) $= 6\pi \circ \theta$ = $6\pi \theta^2 \beta_z$

Longitudinal Beam Area A. Bunded Beam-dongitudine Area of individual bund $S = 6\pi \delta_{\tau} \delta_{\varepsilon}$ in eV-sec (4)

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oz, me bunch leigth in time unit Or = Oe /BC De, sms bunch length Be, bunch relocity TE, sons evergy gread For heavy ion of could be measured in eV/A and then the bunch area will be in eV/A-sec mits Observe that here T is not left explicitly out but is included in the computation Eq. (4) défines the contour for 95% of the beam bunch -

B. Unburched Beam -Longitudiual Area of total Beam in eV-sec $B = 4 \sigma_{E} \cdot T_{o}$ (5)

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where

To revolution period Te, mis energy spread For heavy ion of could be measured in eV/A and then the beam area will be in eV/A-sec-Also eq. (5) défines a contour for 95% of the beam -Observe that eq. \$(4) and (5) are invariants Laside from possible external sources of dilution and diffusion) and do not dyand on the beam energy or 4 on the particle charge startus-