

## RHIC RF system

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**U.S. Department of Energy**

USDOE Office of Science (SC)

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AD/RHIC-RD-10

RHIC RF System

*(Mini-Workshop on RHIC RF Systems)*

*July 11-15, 1988  
Collider Center*

M. Puglisi  
BNL

## ACKNOWLEDGEMENTS

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## **THE HIGH FREQUENCY SYSTEM ( HFS) BASIC DESIGN GOALS**

**The HFS should exhibit some basic properties**

- 1) Full transparency to the beam**
- 2) Modulability: From a total voltage less than 1MV to a total voltage of not less than 12MV**
- 3) Insensitivity to the steady and dynamic beam loading**
- 4) Easy response to feedback loops**
- 5) Reliability and capability of quick recovery from faulty operation**
- 6) Insensitivity to the multi-pacting**

## **BASIC DESIGN CRITERIA**

Without totally ruling out the trivial solution: "ID EST" a sistem with extremely low output impedance, it is important to realize that the above requirements do not necessarily depend upon the hardware. [for example: the modulability can be realized both via hardware as it is well known or via the low level system counter phasing the cavity as it is proposed to do.]

On the contrary, the hardware should be designed in such a way as to be a "tamed horse" in the hands of the low level system.

## PARAMETERS

$$\text{GOLD} \quad m = 1.1 \text{ } \omega^9 \quad \text{SC} = 79 \quad M = 197$$

$$l = 3833.845 \text{ m}$$

$$f_r = \frac{c}{l} = 78.19564954$$

$$f = N f_r = N \frac{c}{l} = 4.457152024 ; T = 2.243585129$$

$$f_{rf1} = h_1 * f = 6 * f = 26.74291214 \text{ MHz}$$

$$f_{rf2} = h_2 f_{rf1} = 6 * f_{rf1} = 160.4574729 \text{ MHz}$$

$$q = n e s c = 139.04 \text{ } 10^{-8} \text{ COULOMBS}$$

$$Q = N q = 7.92528 \text{ } 10^{-7} \text{ COULOMBS}$$

$$I_{AVE} = Q * f_2 = 0.061972241 \text{ AMP}$$

Despite the very different shapes of the bunch,  
the corresponding spectra are not widely different.

This allows to design the hardware without a precise  
knowledge of the beam shape.

The important parameters are

$q$ =charge per bunch

$\tau$ =time length of the bunch

For RHIC, the absolute limits are

$$q = 1.1 \times 10^9 \times e = 1.39^{-8}$$

$$1\text{ns} \quad \tau \quad 17\text{ns}$$

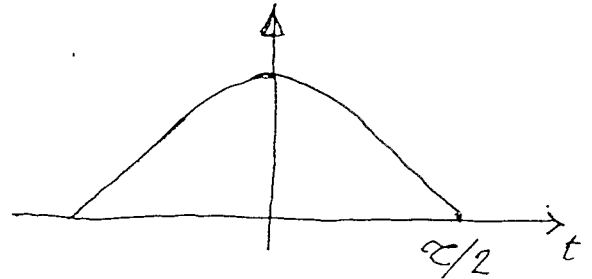
$$13.9 \quad I_{peak} \quad 27.8$$



# BEAM HARMONICS

a) - ARC OF COSINE

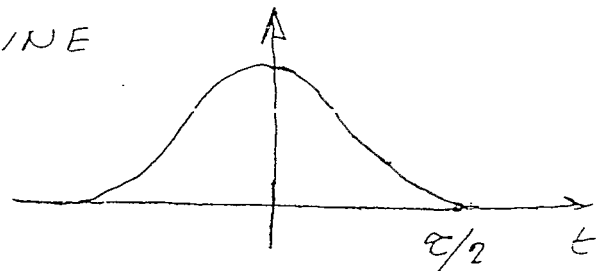
$$I_b(t) = \frac{\pi}{2} \frac{q}{\tau} \cos \pi \frac{t}{\tau}$$



$$\bar{I}_m = 2 \frac{q}{\tau} \frac{\cos \pi m \frac{\tau}{\tau}}{\left(\frac{\tau}{\tau}\right)^2 - (2\pi)^2}$$

b) - SQUARED ARC OF COSINE

$$I_b(t) = 2 \frac{q}{\tau} \cos^2 \pi \frac{t}{\tau}$$



$$\bar{I}_m = \frac{2q}{\pi \tau m} \frac{\sin \pi m \frac{\tau}{\tau}}{1 - \left(m \frac{\tau}{\tau}\right)^2}$$

| I           | F           | I           | F           |        |
|-------------|-------------|-------------|-------------|--------|
| $\tau, 33$  | $\tau, 33$  | $\tau, 34$  | $\tau, 34$  | $\tau$ |
| 0.12160779  | 0.12237969  | 0.12145523  | 0.12227404  | 1      |
| 0.11432956  | 0.11731253  | 0.1137469   | 0.11690443  | 2      |
| 0.10290664  | 0.10924069  | 0.10169421  | 0.10837472  | 3      |
| 0.08831507  | 0.0986882   | 0.08638751  | 0.09727141  | 4      |
| 0.07176256  | 0.08632074  | 0.06916513  | 0.08433481  | 5      |
| 0.05455509  | 0.07288657  | 0.05145694  | 0.07038965  | 6      |
| 0.03795731  | 0.05915229  | 0.03462328  | 0.05627036  | 7      |
| 0.02306446  | 0.04584005  | 0.01981047  | 0.04274925  | 8      |
| 0.01070111  | 0.03357251  | 0.00784129  | 0.03047526  | 9      |
| 0.00135798  | 0.02283084  | -0.00084702 | 0.01992926  | 10     |
| -0.00482727 | 0.013929    | -0.00621188 | 0.01139955  | 11     |
| -0.00804602 | 0.00700609  | -0.00856406 | 0.0049789   | 12     |
| -0.00875731 | 0.00203596  | -0.00848535 | 0.00058154  | 13     |
| -0.00760023 | -0.00114837 | -0.00672    | -0.0020236  | 14     |
| -0.00529354 | -0.00281947 | -0.00405728 | -0.00316864 | 15     |
| -0.00253707 | -0.00331417 | -0.00122241 | -0.00323782 | 16     |
| 0.00007225  | -0.00299148 | 0.00120934  | -0.00261997 | 17     |

| I           | F           | I           | F           |        |
|-------------|-------------|-------------|-------------|--------|
| $\tau, 35$  | $\tau, 35$  | $\tau, 36$  | $\tau, 36$  | $\tau$ |
| 0.12129826  | 0.12216532  | 0.1211369   | 0.12205352  | 1      |
| 0.1131491   | 0.11648533  | 0.11253635  | 0.11605534  | 2      |
| 0.10045628  | 0.10748862  | 0.09919372  | 0.10658286  | 3      |
| 0.08443333  | 0.09582914  | 0.08245486  | 0.09436272  | 4      |
| 0.06655731  | 0.08232704  | 0.06394365  | 0.08030015  | 5      |
| 0.04838657  | 0.06788747  | 0.04535094  | 0.0653845   | 6      |
| 0.03137602  | 0.05341421  | 0.02822401  | 0.05059005  | 7      |
| 0.01671562  | 0.03972824  | 0.01378763  | 0.03678423  | 8      |
| 0.00521354  | 0.02750015  | 0.00282125  | 0.02465389  | 9      |
| -0.00276216 | 0.01720341  | -0.00439259 | 0.01465734  | 10     |
| -0.00727901 | 0.00909227  | -0.00804602 | 0.00700609  | 11     |
| -0.0087778  | 0.00320508  | -0.00871879 | 0.00167614  | 12     |
| -0.00796635 | -0.00060982 | -0.00724504 | -0.0015555  | 13     |
| -0.00568841 | -0.00265066 | -0.00455881 | -0.00305602 | 14     |
| -0.00278952 | -0.00330836 | -0.00154441 | -0.00327267 | 15     |
| 0           | -0.00300987 | 0.00108517  | -0.00266875 | 16     |
| 0.00214908  | -0.00216594 | 0.00286566  | -0.00166775 | 17     |

| I           | F           | I           | F           |        |
|-------------|-------------|-------------|-------------|--------|
| $\tau, 37$  | $\tau, 37$  | $\tau, 38$  | $\tau, 38$  | $\tau$ |
| 0.12097115  | 0.12193866  | 0.12080104  | 0.12182074  | 1      |
| 0.11190884  | 0.11561456  | 0.11126678  | 0.1151631   | 2      |
| 0.09790741  | 0.10565791  | 0.09659826  | 0.10471427  | 3      |
| 0.08045444  | 0.09287346  | 0.07843443  | 0.09136272  | 4      |
| 0.06132866  | 0.07825683  | 0.05871677  | 0.07619976  | 5      |
| 0.04235677  | 0.06288514  | 0.03941052  | 0.06039371  | 6      |
| 0.02517511  | 0.04780382  | 0.02223651  | 0.04506122  | 7      |
| 0.01103298  | 0.03392387  | 0.00845691  | 0.03115324  | 8      |
| 0.00066585  | 0.02194222  | -0.00125311 | 0.01936988  | 9      |
| -0.00574595 | 0.01229365  | -0.00683227 | 0.01011352  | 10     |
| -0.00853293 | 0.00513806  | -0.008762   | 0.00348346  | 11     |
| -0.00842047 | 0.00038154  | -0.00791747 | -0.00069105 | 12     |
| -0.00636613 | -0.00227469 | -0.0053734  | -0.00278791 | 13     |
| -0.00338147 | -0.00326705 | -0.00220261 | -0.00331148 | 14     |
| -0.00036916 | -0.00309502 | 0.00069672  | -0.00280759 | 15     |
| 0.00199891  | -0.0022503  | 0.00271799  | -0.00178709 | 16     |
| 0.00334687  | -0.00115892 | 0.00359323  | -0.00066763 | 17     |

## Construction Technique

- a) Efficient and fast feedback operations are possible only with tubes directly mounted on the cavity
- b) Two "small" tubes per cavity are preferable than one with twice the power. This is due to the fact that the frequency is already high and the "small" tube should be always a tube with more than 20kV of plate dissipation and this implies large mechanical sizes.
- c) Counter phasing seems a very good and economical technique for amplitude modulation of the total voltage. This implies an even number of cavities.
- d) Beam loading is well under control because each cavity works at nearly full voltage.

Having decided for an even number of cavities a series modulator can be used grouping the cavities two by two.

One series tube controls two cavities:

1. The cost is heavily reduced
2. In case of faulty operation a unit of two counterphased cavities is automatically eliminated.
3. With this system the counter phasing should be done with the beam "at 90 degrees" in case of total counterphasing.

$$V = 2 \times 500 \text{ kV} = 1.0 \text{ MV}$$

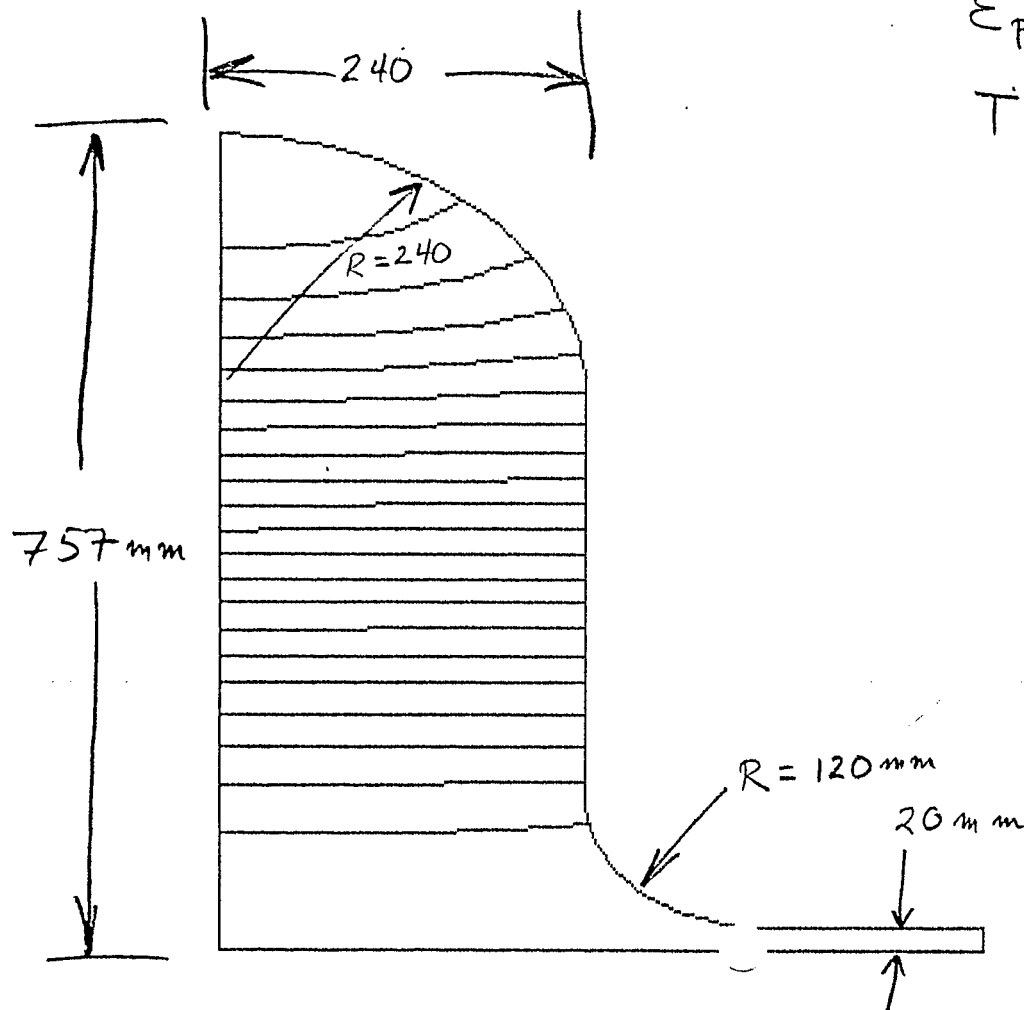
$$P = 2 \times 33 \text{ kW} = 66 \text{ kW}$$

$$R = \frac{(10^6)^2}{2 \times 66 \times 10^3} = 7.6 \text{ M}\Omega$$

$$R/Q = 123 \Omega$$

$$E_{\text{peak}} = 2.2 \text{ MV/m}$$

$$T = 0.88$$



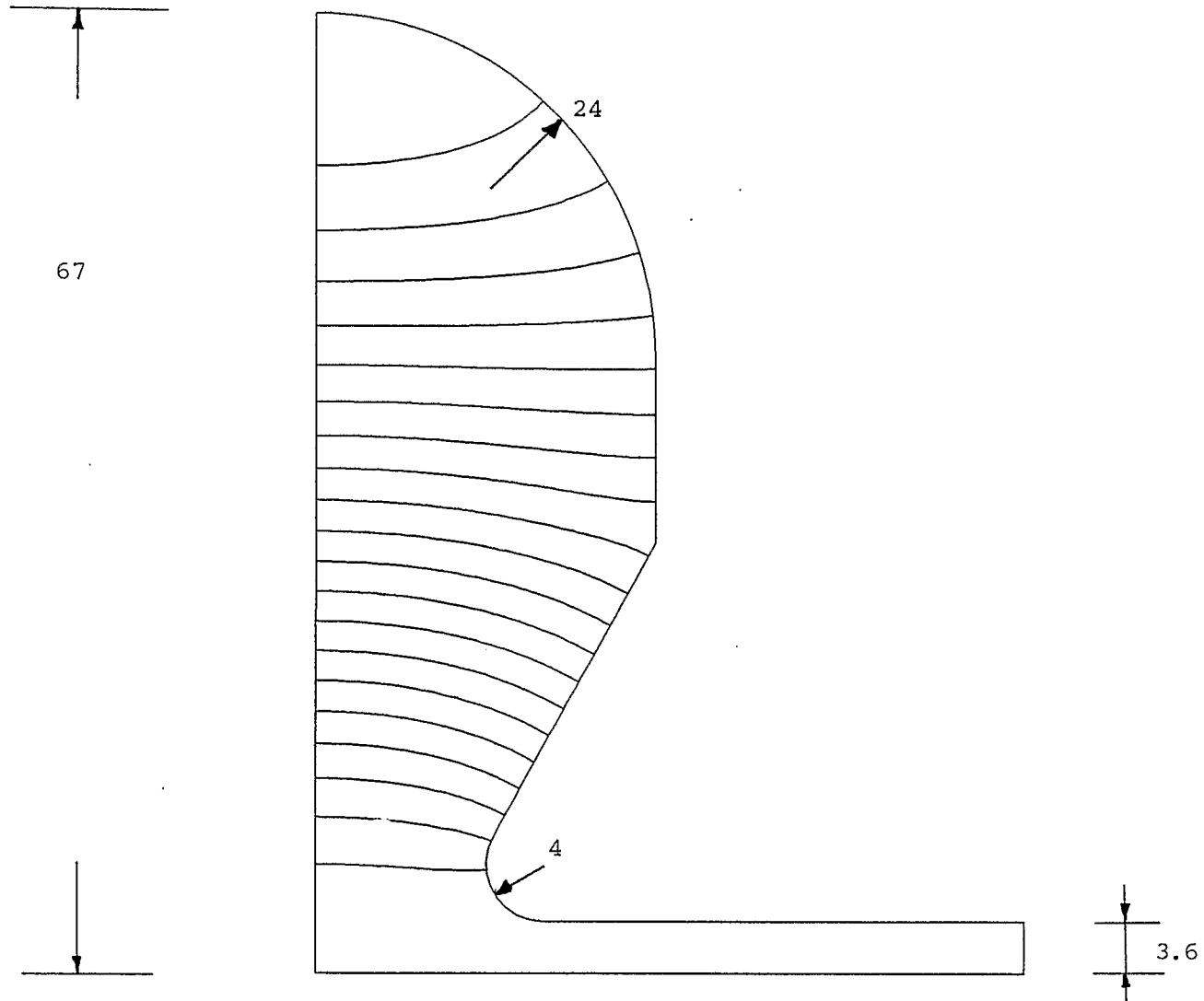
$F = 163.2 \text{ MHz}$

$P_d = 72.94 \text{ kW}$

$R_s = 6.85 \text{ M}$

$R/Q = 123$

$E_{\text{peak}} = 6.4 \text{ MV/m}$



## Comments on the cavity design.

The cavity is not at all a problem; nevertheless some performances are important.

- a.) The intrinsic shunt impedance should be as high as possible. In fact there are many techniques that permit to lower the gap shunt impedance. The contrary is impossible.
- b.) The transient behavior as well as the sensitivity to the beam loading depend upon the ratio  $R/Q$ . An effort should be made in order to keep  $R/Q$  as small as possible.
- c.) For stability reasons, the ratio between peak and accelerating field should not be too large. In any case, it is not safe to push the peak field above 6-8 MV/m.
- d.) A dome shaped cavity is to be preferred for reducing the multipactoring.
- e.) A not extremely transit time factor would help in reducing the effect of the higher order modes.

## Comment on the power amplifiers.

- After many runs of superfish, it became clear that a shunt impedance (theoretical-intrinsic) of  $6\text{M}\Omega$  is the most likely to occur.
- The imperfect matching, the ceramic windows and eventually the H O M suppressor easily reduce this impedance to  $4\text{M}\Omega$ . Assuming a voltage of  $700\text{kV}$  per cavity (power and gradient limitations), we obtain a power of about  $60\text{ kW}$ .
- This power demands for somewhat large tubes. Moreover at the frequency of  $160\text{ MHz}$  many tubes are to be derated. Furthermore, besides the demand of power, there is the demand of current (fast compensation of the transient beam loading) Taking into account the various requirements, a  $80 - 100\text{ kW}$  plate dissipation tube is absolutely requested.



- The actual need of fast and slow feedback loops (and in general of some gymnastic with feed forward techniques) render mandatory to connect the driveing tube(s) directly to the cavity. In other words a cavity coupling system is needed instead of an amplifier connected to the cavity with coaxial cables.

- The mechanical sizes of the cavity are in the park of: 1.5 m (diameter), 0.5 m (thickness) and it is difficult to change drastically those sizes  
On the other hand a tube with 80-100kW of plate dissipation may be inscribed in a cylinder 40 cm long and 30 cm large. Those sizes do not combine well with the sizes of the cavity and difficulties are to be expected with the electro-mechanic construction.

- The situation considerably improves if two small tubes per cavity are used. With this option we have several important advantages.

Each tube is small and a simple and compact mounting is feasible. The feedback distances are not big even for 160 MHz.

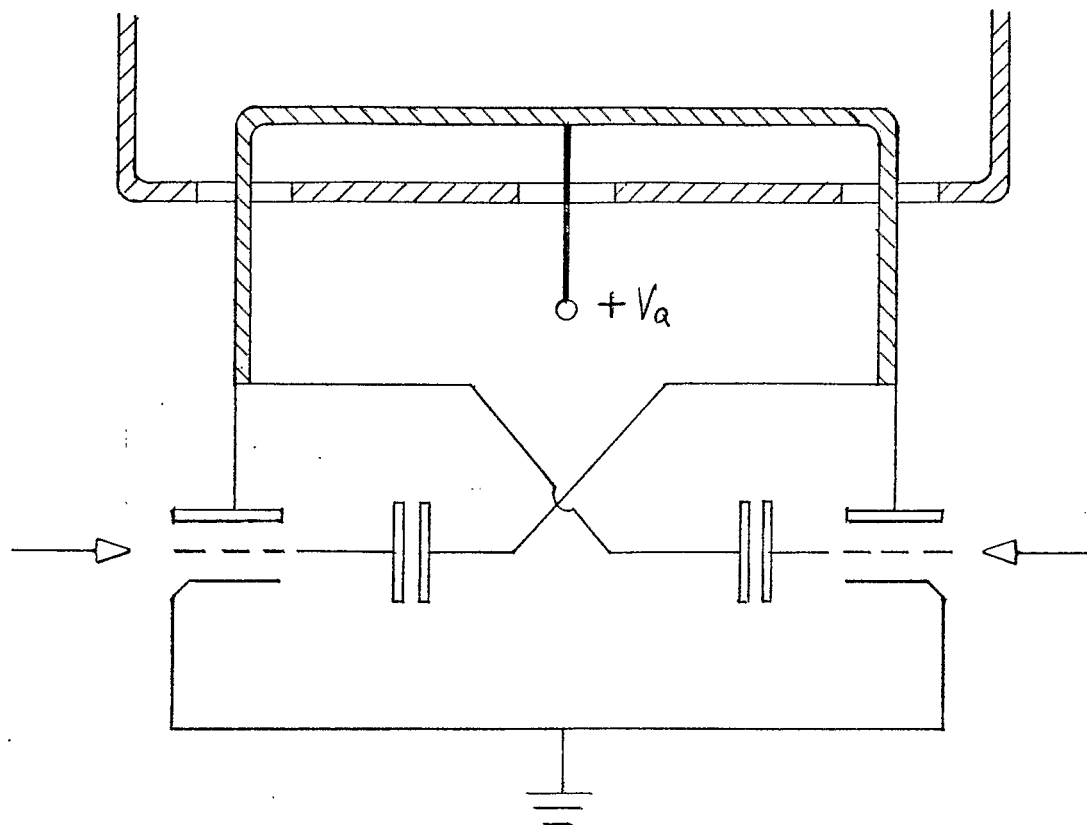
Push pull or push push operation is possible. If push push operation is chosen and neutralized triodes are used, then the gap input impedance can be lowered at no cost.

The cavity can be feed in a more simmetric way and the impedance of the H O M is reduced.

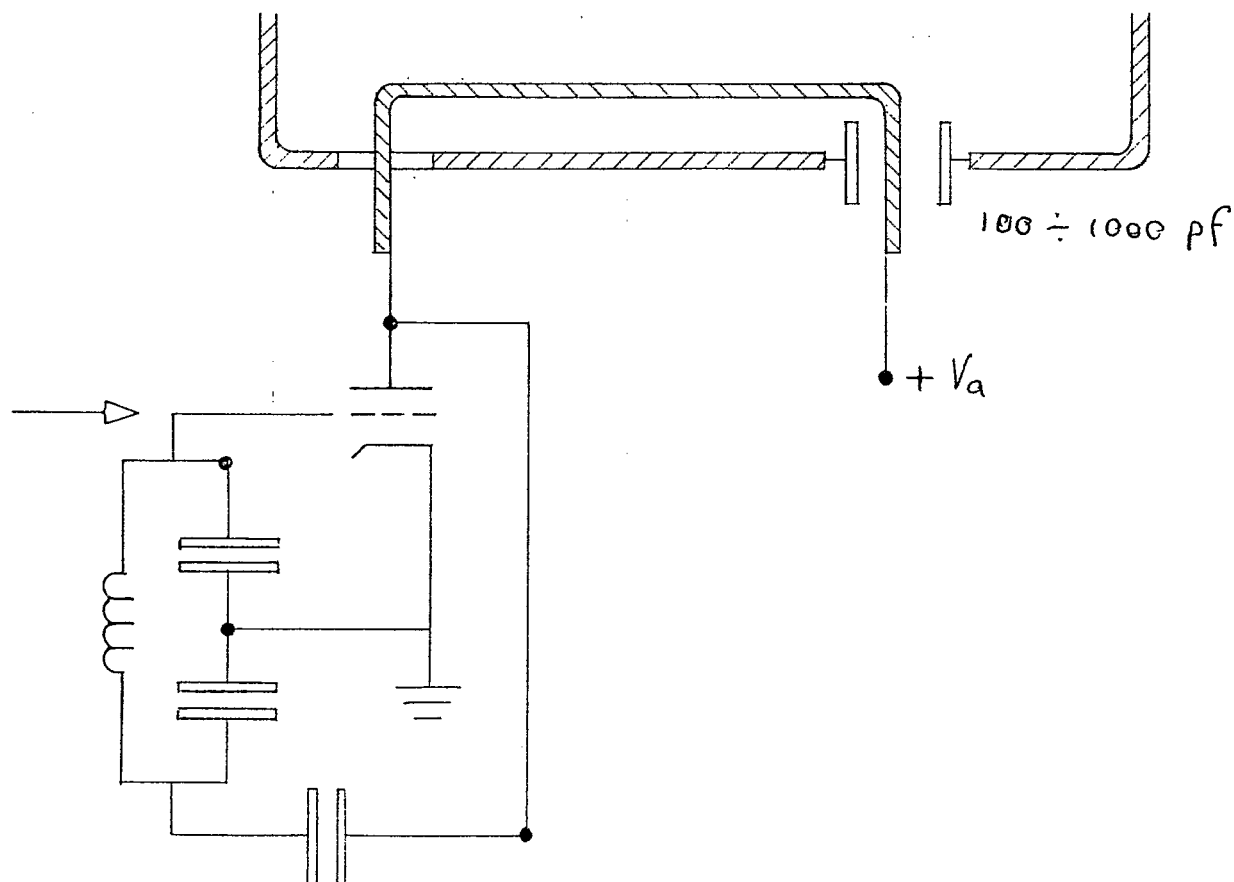
The ceramic windows are easier to fabricate and allow a safer operation.

Once the anodes are mounted, then the grid circuit can be chenged without much effort.

# PUSH PULL CAVITY COUPLING SYSTEM

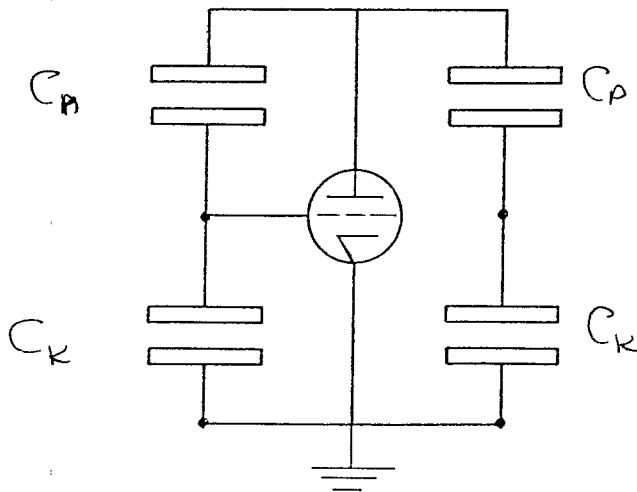
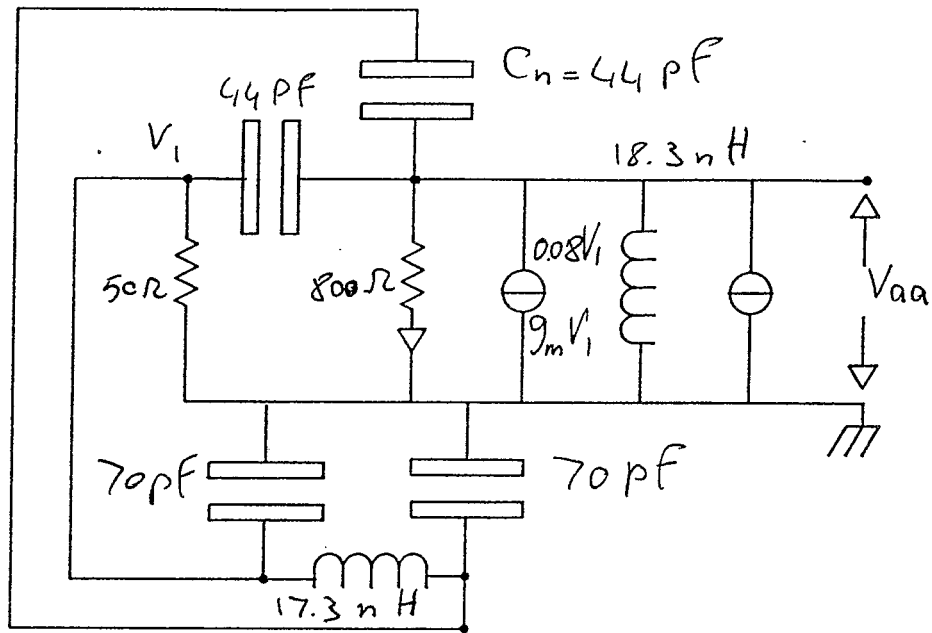


# SINGLE ENDED CAVITY COUPLING SYSTEM





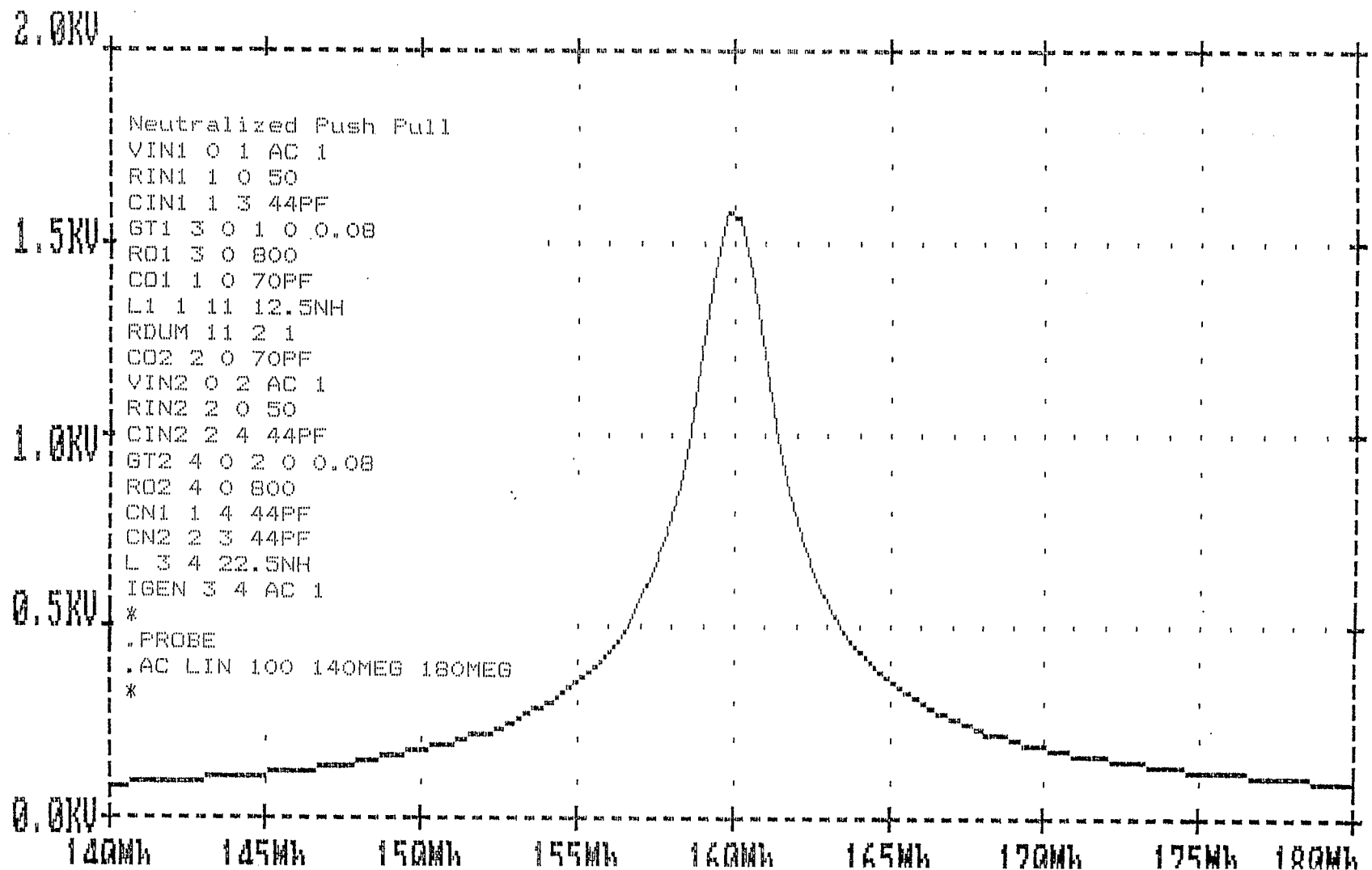
# NEUTRALIZED SINGLE ENDED OUTPUT IMPEDENCE



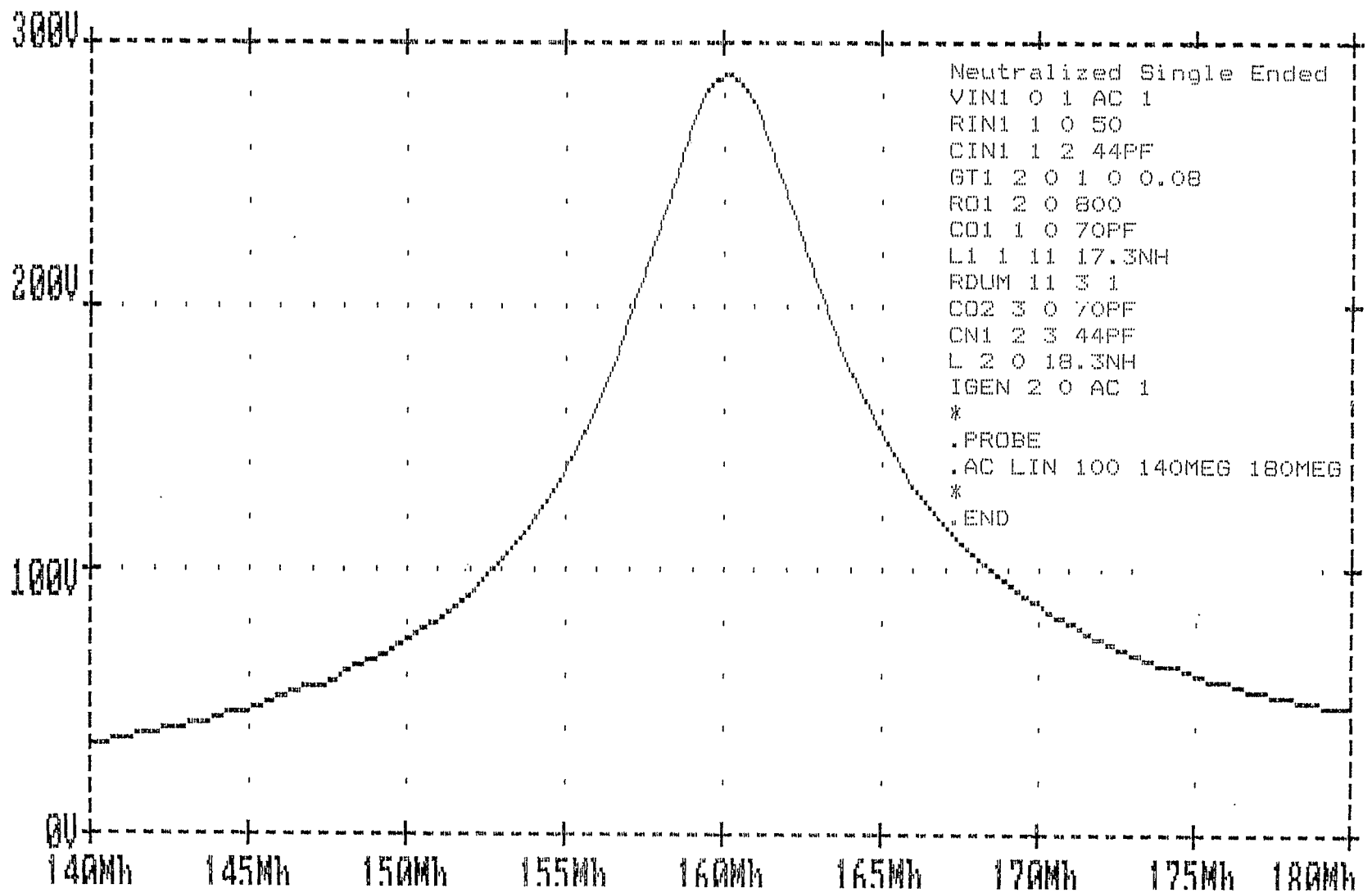
$$\frac{C_p}{C_k} = \frac{C_n}{C_k} \Rightarrow C_p = C_n$$

$$\begin{cases} C_a = 2 \frac{C_p C_k}{C_p + C_k} = 54\text{ pF} \\ C_g = \frac{1}{2} (C_p + C_k) = 57\text{ pF} \end{cases}$$

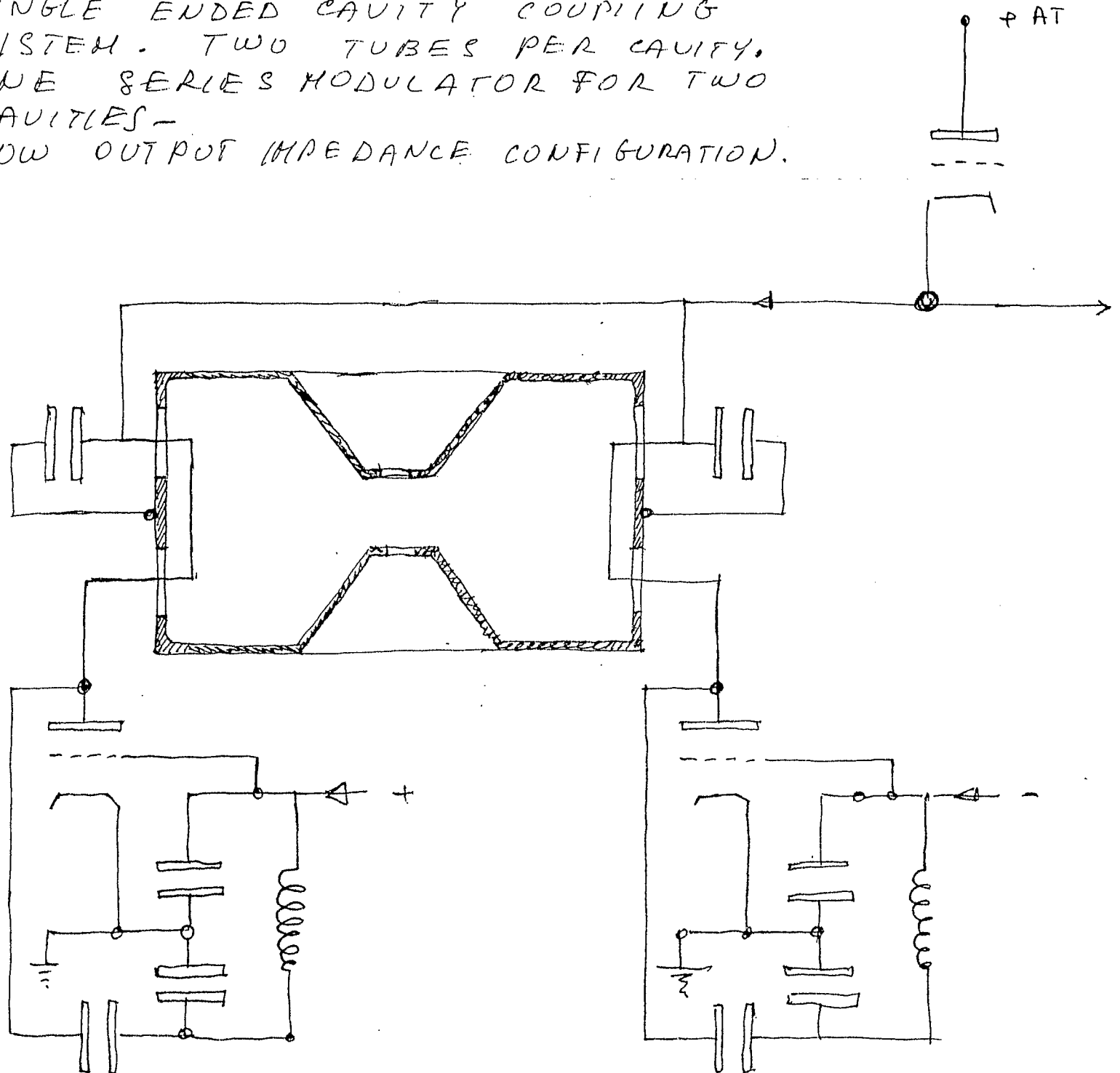
# Neutralized Push Pull Output Impedance



# NEUTRALIZED SINGLE ENDED OUTPUT IMPEDENCE



SINGLE ENDED CAVITY COUPLING  
SYSTEM. TWO TUBES PER CAVITY,  
ONE SERIES MODULATOR FOR TWO  
CAVITIES -  
LOW OUTPUT IMPEDANCE CONFIGURATION.





## OUTLINE DRAWING

3/16 DIA INDEX HOLE THRU ON  
8.750 DIA PC. TO ALIGN WITH  
LOCKING PIN & WATER FITTING  
WITHIN 10°

5/16 DIA HOLE THRU, 8 HOLES  
EQUALLY SPACED ON 8.750 DIA PC.  
222.25

1/4-20 UNC 2B THRU, 12 HOLES  
EQUALLY SPACED ON 7.375 DIA PC.  
187.33

5/16-18 UNC-2A STUD WITH  
2 HEX NUTS ANODE D.C.  
CONNECTION (MAY BE USED  
FOR LIFTING TUBE)

FITTING NUT & IMPERIAL FITTING  
& SLEEVE FOR 3/4 O.D. TUBING

SK-2100 WATER JACKET  
NOT SUPPLIED UNLESS ORDERED

1/4-20 UNC-2A x 5/8 LG ST STL  
BLTTON HEAD CAP SCREW  
SOCKET DR, 12 REQD SUPPLIED  
WITH WATER JACKET

ANODE R.F. CONNECTION

DO NOT CONTACT O.D.

SURFACE 'a'

3/16 DIA PIN, SEE INDEX HOLE

TUBE MOUNTED  
ON SURFACE 'a'  
FEATURES &  
DATUM AT MMC

E .015 DIA  
0.38

| DIM | INCHES |        |         | MILLIMETERS |        |        |
|-----|--------|--------|---------|-------------|--------|--------|
|     | MIN    | MAX    | REF     | MIN         | MAX    | REF    |
| A   | 9.468  | 9.531  |         | 240.49      | 242.09 |        |
| B   |        |        | 5.000   |             |        | 127    |
| C   | .125   |        |         | 3.18        |        |        |
| D   | 1.230  | 1.270  |         | 31.24       | 32.26  |        |
| E   | 3.865  | 3.885  |         | 98.17       | 98.68  |        |
| F   | 4.240  | 4.260  |         | 107.7       | 108.2  |        |
| G   | 4.490  | 4.510  |         | 114.05      | 114.55 |        |
| H   |        |        | 7.750   |             |        | 196.85 |
| J   | .069   | .149   |         | 1.75        | 3.79   |        |
| K   | .382   | .462   |         | 9.70        | 11.74  |        |
| L   | .797   | .922   |         | 20.24       | 23.42  |        |
| M   | 5.875  | 6.000  |         | 149.23      | 152.6  |        |
| N   |        |        | 11.500  |             |        | 292.1  |
| P   |        |        | 1.375   |             |        | 34.93  |
| R   | .410   | .475   |         | 10.41       | 12.07  |        |
| S   |        |        | 22 1/2° |             |        |        |
| T   |        |        | 30°     |             |        |        |
| U   | 13.750 | 14.250 |         | 349.25      | 361.95 |        |
| V   | 6.437  | 6.562  |         | 163.7       | 166.88 |        |
| W   | 3.187  | 3.313  |         | 80.95       | 84.15  |        |
| X   |        |        | .562    |             |        | 14.28  |
| Y   |        |        | .312    |             |        | 7.93   |

REF DIMENSIONS ARE FOR  
INFORMATION ONLY

(\*) MINIMUM CONTACT SURFACE

TYP  
\*

SCREEN GRID

CONTROL GRID

FILAMENT

## ELECTRICAL

Filament ..... Thoriated Tungsten

Voltage ..... 15.5 ± 0.75 V

Current, at 15.5 V ..... 215 A

Direct Interelectrode Capacitances,  
Cathode grounded

Input ..... 370 pF

Output ..... 60 pF

Feedback ..... 1.0 pF

Grid grounded

Input ..... 175 pF

Output ..... 60 pF

Feedback ..... 0.35 pF

Maximum Frequency,

for maximum CW ratings ..... 103 MHz

## Absolute Maximum Ratings

Plate Voltage ..... 20 kVdc

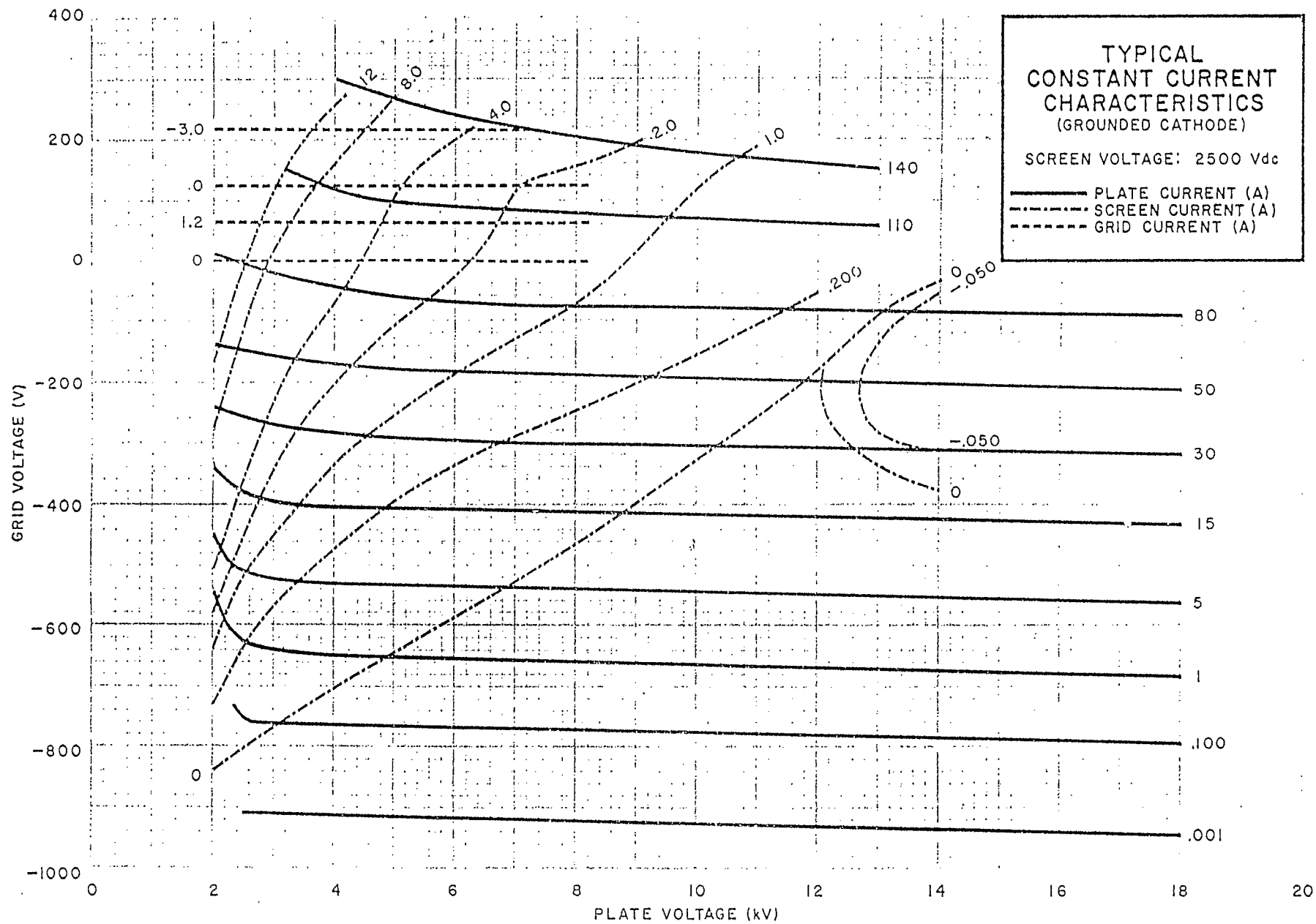
Screen Voltage ..... 2.5 kVdc

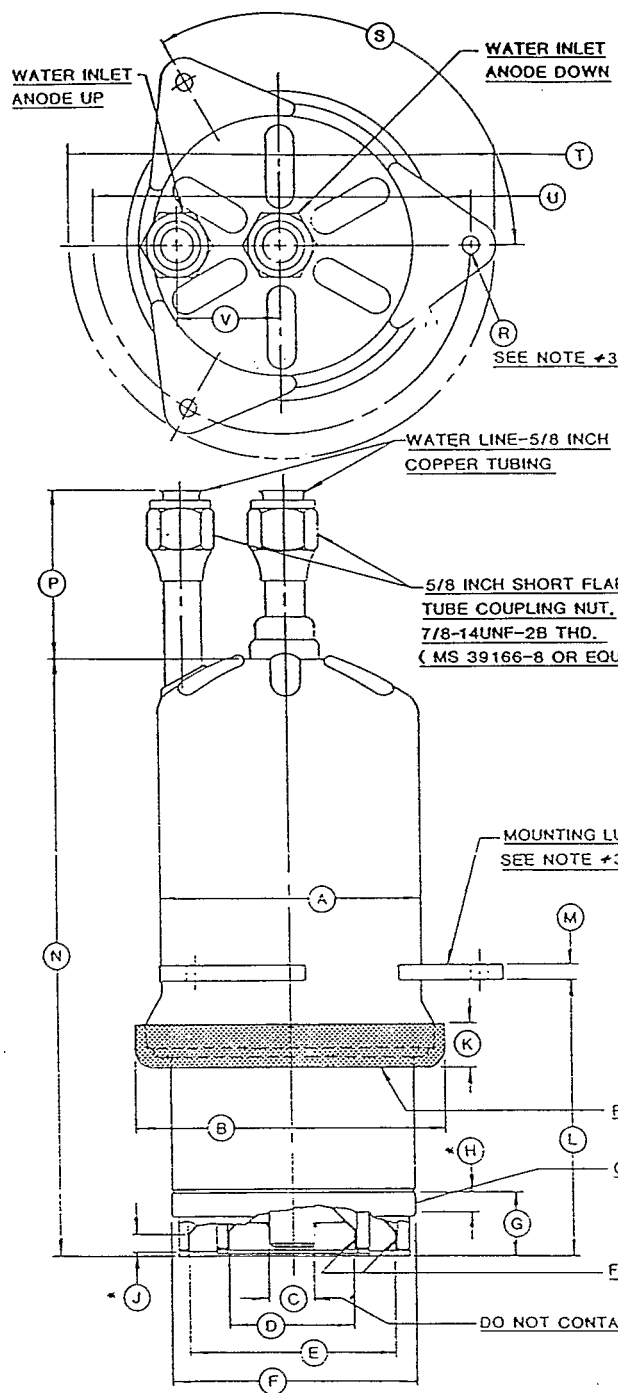
Plate Current ..... 16 Adc

Plate Dissipation ..... 100 kW

Screen Dissipation ..... 1750 W

Grid Dissipation ..... 500 W





| DIMENSIONAL DATA |        |       |       |      |             |      |
|------------------|--------|-------|-------|------|-------------|------|
| DIM              | INCHES |       |       | REF. | MILLIMETERS |      |
|                  | MIN    | MAX   |       |      | MIN.        | MAX. |
| A                | 4.062  | 4.188 |       |      |             |      |
| B                |        |       | 4.926 |      |             |      |
| C                | .600   | .760  |       |      |             |      |
| D                | 1.826  | 1.936 |       |      |             |      |
| E                | 3.133  | 3.173 |       |      |             |      |
| F                | 3.792  | 3.832 |       |      |             |      |
| G                | .986   | 1.050 |       |      |             |      |
| H                | .188   |       |       |      |             |      |
| J                | .188   |       |       |      |             |      |
| K                |        |       | .712  |      |             |      |
| L                | 4.350  | 4.450 |       |      |             |      |
| M                |        |       | .250  |      |             |      |
| N                | 9.400  | 9.600 |       |      |             |      |
| P                |        |       | 2.625 |      |             |      |
| R                |        |       | .265  |      |             |      |
| S                | 118°   | 122°  |       |      |             |      |
| T                |        |       | 6.750 |      |             |      |
| U                | 5.957  | 6.025 |       |      |             |      |
| V                |        |       | 1.625 |      |             |      |

**NOTES:**

1. REF DIMENSIONS ARE FOR INFO ONLY & ARE NOT REQUIRED FOR INSPECTION PURPOSES.
2. (\*) CONTACT SURFACE.
3. 3 MOUNTING HOLES IN MOUNTING LUGS

7

Filament: Thoriated Tungsten

Voltage . . . . . 12.0 ± 0.5 V

Current @ 12.0 Volts . . . . . 120 A

Direct Interelectrode Capacitance (grounded cathode) <sup>2</sup>

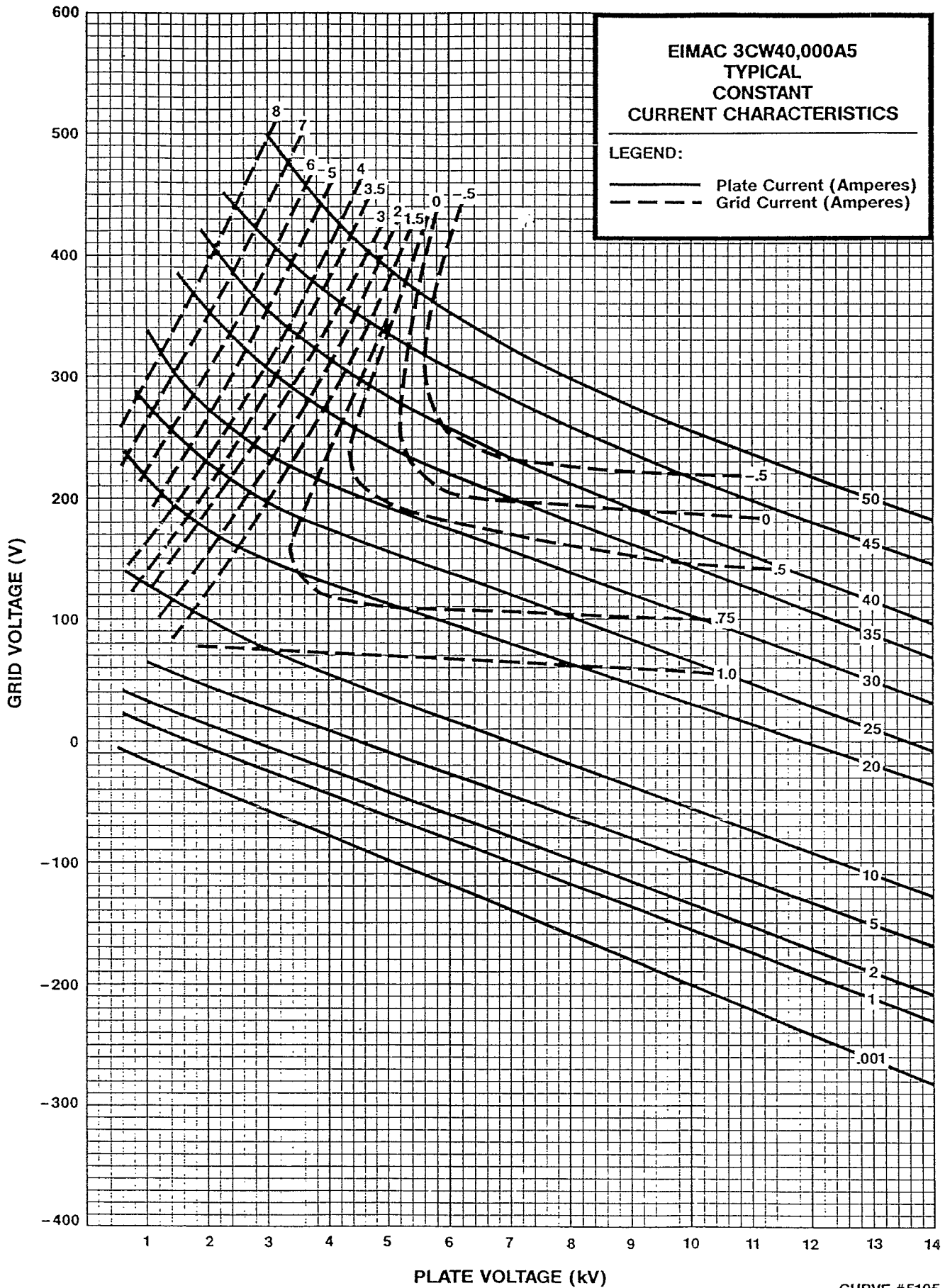
Cin . . . . . 70.0 pF

Cout . . . . . 2.3 pF

Cgp . . . . . 43.0 pF

Amplification factor . . . . . 55

Frequency of Maximum Rating (CW) . . . . . 90 MHz



CURVE #5105

## THE CAVITY COUPLING SYSTEM.

### a) THE CAVITY.

SUPER-FISH PARAMETER  $f = 163 \text{ MHz}$

$$R/Q = 123 \Omega \quad C_{eq} = 8.09 \text{ pF}$$

$$R = 6.8 \text{ M}\Omega$$

FOR  $V_{gap} = 700 \text{ kV}$  AND  $R \approx 4 \times 10^6$

WE OBTAIN:  $W \approx 60 \text{ kW}$

### b) THE AMPLIFIER.

WE ASSUME TWO EIMAC 3CW40,000 A5.

WITH THE ALREADY SHOWN SPLIT GRID NEUTRALIZATION

THE OUTPUT IMPEDANCE IS  $\sim 300 \Omega$ . WITH A VOLTAGE

RATIO OF 35 ( $700 \text{ kV} / 2 \times 10,000$ ) THE

GAP EQ. IMPEDANCE BECOMES EQUAL TO  $\sim$

$700 \text{ k}\Omega$ . WITH AN EQUIVALENT Q EQUAL TO

$\sim \frac{R_{eq}}{R/Q} \approx 5700$  AS SEEN FROM THE 1st BEAM

IN STEADY CONDITIONS.

EACH TUBE HAS 40 KW PLATE POWER DISSIPATION -- FULL RATING OF THE TUBE IS AT 80 KHz  $\rightarrow$  FOR 160 KHz WE SHOULD REDUCE THE INPUT AND 60 KW OF POWER ARE EASILY OBTAINED FROM TWO TUBES --

c) - BEAM LOADING (STEADY) --

$$\Delta C = \frac{I_{RF}}{2\pi f V_{RF}} \quad \text{ASSUMING } I_{RF} = \sim 0.12 \text{ A}$$

$$V_{RF} = 200 \text{ KV}$$

$$\Delta C \approx 6 \cdot 10^{-16} =$$

$$\frac{\Delta f}{f} = \frac{1}{2} \frac{\Delta C}{C} = \frac{I_{RF} / 2\pi f V_{RF}}{C} = \frac{1}{2} \frac{R}{Q} \frac{I_{RF}}{V_{RF}} = 3.69 \cdot 10^{-5}$$

$\Delta f \approx 6 \text{ KHz}$  IN THE WORST CONDITIONS --

$$Z = \frac{R}{1 + j Q_L \left( \frac{f}{f_0} - \frac{f_0}{f} \right)}$$

IS THE IMPEDANCE OF THE CAVITY LOADED BY THE AMPLIFIER

$$\xi = f/f_0 - f_0/f \approx -2 \frac{\Delta f}{f_0} = 7.5 \cdot 10^{-5}$$

$$\xi Q_L = -0.427 \quad \varphi = +24^\circ$$

D) - THE BEAM INDUCED VOLTAGE.

THE FIRST COMPONENT OF THE BEAM CURRENT HAS A FREQUENCY EQUAL TO 4.45 MHz - THE FUNDAMENTAL COMPONENT, I.E. THE ONE WITH THE RF. FREQUENCY CORRESPOND TO THE 36<sup>TH</sup> HARMONIC

FOR THIS COMPONENT THE GAP EQ. IMPEDANCE IS EQUAL TO:

$$Z = \frac{R}{1 + j \xi Q_L} = ; |Z| = 643 \text{ k}\Omega$$

AND THE CORRESPONDING VOLTAGE IS  $V_i \approx 77.8 \text{ kV}$

THE NEXT HARMONIC HAS NEARLY THE SAME AMPLITUDE BUT THE

DISSONANCE INCREASES :

$$\xi)_{37} = \frac{2 * 4.45 10^6}{160 10^6} = 5.56 10^{-2}$$

$$Q_L \xi = 317 \rightarrow |Z| \cong 2.20 \text{ k}\Omega$$

AND THE INDUCED VOLTAGE DUE TO THE  
37<sup>th</sup> HARMONIC IS EQUAL TO 269 V<sub>eff</sub>  
AT, PRATICALLY 90°.

THE OTHER HARMONICS GIVE ALSO  
NEGGLIGIBLE CONTRIBUTION