BNL-101546-2014-TECH

RHIC/PG/3;BNL-101546-2013-IR

Short Bunches Performance With Intrabeam Scattering

A. G. Ruggiero

November 1983

Collider Accelerator Department

Brookhaven National Laboratory

U.S. Department of Energy

USDOE Office of Science (SC)

DISCLAIMER

RHIC-PG-3

SHORT BUNCHES PERFORMANCE WITH INTRABEAM SCATTERING

A.G. Ruggiero

(BNL, November 17, 1983)

Short Bunches

$$\mathcal{L} = \frac{N_c^2 B\, f_{rev}}{2\pi\, \alpha\, \sigma_\ell\, \sigma_v}$$

σ_ℓ = 10 cm

σ_v = 0.0037 cm

α = 4 mrad

B = 57

f_{rev} = 78.1973 KHz

$N_c = 6.24 \times 10^8$

$\mathcal{L} = 1.9 \times 10^{27}\ cm^{-2}\ s^{-1}$

Filling sequence :

- one AGS pulse is made of 3 bunches
- 19 AGS pulses stacked in a box-car fashion

Filling Time : about 1 minute -

Longitudinal Stability of short Bunches

$$\left|\frac{Z}{n}\right| = \frac{E|\eta|}{eI_p}\left(2\,\frac{\sigma_E}{E}\right)^2\frac{A}{Z^2}$$

I_p, peak current $= N_c\, e\, \beta c \,/\, (\sigma_\ell \sqrt{2\pi})$

N_c, no. of particles / bunch $=$ ~~xx~~ 6.24×10^8
σ_ℓ, rms bunch length $= 10$ cm $\quad (\sigma_\tau = 0.33$ nsec$)$

$$I_p = 0.12 \text{ Amp - particle} \quad (\beta \sim 1)$$

For Gold (Au) $\quad A = 197 \quad$ and $\quad Z = 79$
Assume a coupling impedance of $|Z/n| = 10$ ohm
E, energy per nucleon ~ 100 GeV/A
$\eta = \gamma^{-2} - \gamma_T^{-2}$, $\quad \gamma_T$ = transition energy / rest energy
σ_E/E, rms energy spread at stability

$\mathcal{B} = 6\pi\, \sigma_E \cdot \sigma_\tau$, bunch area

The following table explores the dependence on γ_T of the threshold energy spread σ_E/E and the corresponding bunch area -

γ_T	$\lvert\eta\rvert$	σ_E/E threshold @ 100 GeV/A	B eV/A - sec
10	.0099	0.98×10^{-4}	0.061
20	.0024	1.99×10^{-4}	0.124
30	1.011×10^{-3}	3.07×10^{-4}	0.191
50	3×10^{-4}	5.63×10^{-4}	0.350
80	5.625×10^{-5}	13.00×10^{-4}	0.809

Intrabeam scattering diffusion rates @ 100 GeV/A

$\varepsilon_N = 4.0\ \pi$ mm. mrad

σ_E/E	t_E	t_β
$1. \times 10^{-4}$	0.13 hours	0.32 hours
$2. \times 10^{-4}$	0.68	0.43
$4. \times 10^{-4}$	4.4	0.7

At injection (12 GeV/A) we keep the same σ_E/E but lengthen the bunch by a factor $100/12 = 8.333$ then the peak current at injection is

$$I_p = 0.014 \text{ Amp-particle} \quad (\beta \sim 1)$$

Intrabeam Scattering Diffusion Rates @ 12 GeV/A

$\varepsilon_N = 4.0\ \pi$ mm·mrad

σ_E/E	t_E	t_β
$1. \times 10^{-4}$	0.057 hours	5.5 hours
2.	0.37	8.8
4.	4.0	24.
8.	350.	700.