# Power Supply Accuracy Requirements Due to Fluctuations in the Tune 

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Brookhaven National Laboratory

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## RHIC PROJECT

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## 1. Introduction

It is assumed that the goal in setting the power supply accuracy is to keep the variation in the tune to within

$$
\Delta \nu \leq 1 \times 10^{-3}
$$

This note will consider only the major sources of $\Delta \nu$, of which there are three:

1. $I_{Q}$, the current in all the quadrupoles except Q1, Q2, Q3. Errors in $I_{Q}$ will generate a $\Delta \nu$ according to

$$
\Delta \nu_{Q}=C_{Q}\left(\frac{\Delta I}{I}\right)_{Q}
$$

2. $I_{Q 123}$, the current in Q1, Q2, Q3

$$
\Delta \nu_{Q 123}=C_{Q 123}\left(\frac{\Delta I}{I}\right)_{Q 123}
$$

3. $I_{B}$, the current in all the dipoles except BC 1 which is separately powered

$$
\Delta \nu_{B}=C_{B}\left(\frac{\Delta I}{I}\right)_{B}
$$

$(\Delta I / I)_{B}$ causes an orbit displacement, and this displacement at the sextupoles causes a $\Delta \nu$.

It may be shown analytically that $C_{Q}$ is equal to the chromaticity due to these quadrupoles, $C_{Q 123}$ is the equal to the chromaticity due to $\mathrm{Q} 1, \mathrm{Q} 2, \mathrm{Q} 3$ and $C_{B}$ is equal to the chromaticity of the sextupoles if the contribution of BC 1 to the chromaticity is small, which it is.

Thus if the chromaticity is set to nearly zero, then

$$
C_{B}+C_{Q}+C_{Q 123} \simeq 0
$$

For a First Pass, the $\Delta \nu$ due to all other bypasses and trim and the BC 1 power supplies will be neglected. It is assumed that the power supply accuracies can be chosen to make
these sources of $\Delta \nu$ relatively small. If this is not always true, one can correct the results on a Second Pass.

It is assumed that in computing the power supply accuracy, the relevant energy swing is 3.33 , from $\gamma=30$ to $\gamma=100$.

One can compute $C_{B}, C_{Q}$ and $C_{Q 123}$ and find the results

$$
\begin{array}{ll}
\beta^{*}=6 & C_{Q}=31 \\
& C_{Q 123}=16 \\
& C_{B}=-47 \\
\beta^{*}=2 & C_{Q}=31 \\
& C_{Q 123}=47 \\
& C_{B}=-78
\end{array}
$$

These results show that $\mathrm{Q} 1, \mathrm{Q} 2, \mathrm{Q} 3$ can generate as much $\Delta \nu$ as the arc quadrupoles.

## 2. Computation of the Power Supply Accuracy

The $\Delta \nu$ due to all 3 sources is given by

$$
\begin{align*}
\Delta \nu= & C_{B}\left(\frac{\Delta I}{I}\right)_{B}+C_{Q}\left(\frac{\Delta I}{I}\right)_{Q}+C_{Q 123}\left(\frac{\Delta I}{I}\right)_{Q 123}  \tag{1}\\
& C_{B}+C_{Q}+C_{Q 123} \simeq 0
\end{align*}
$$

Case 1: Series Connection, one power supply

$$
\begin{aligned}
\left(\frac{\Delta I}{I}\right)_{B} & =\left(\frac{\Delta I}{I}\right)_{Q}=\left(\frac{\Delta I}{I}\right)_{Q 123} \\
\Delta \nu & =\left(C_{B}+C_{Q}+C_{Q 123}\right)\left(\frac{\Delta I}{I}\right)_{B}
\end{aligned}
$$

Because $C_{B}+C_{Q}+C_{Q 123} \simeq 0, \Delta \nu$ does not give a tolerance on $(\Delta I / I)_{B}$. The tolerance will come from other effects which are not considered here. The accuracy of $(\Delta I / I)_{B}$ will probably be set at whatever is the best value technically feasible, which is about (G. Cottingham)

$$
\left(\frac{\Delta I}{I}\right)_{B} \lesssim 3 \times 10^{-5}
$$

at the lowest current level that is important, which may be at $\gamma=30$.

Case 2: 3 Power Supplies, $I_{Q 123} \neq I_{B}$
The dipoles are on one power supply which determines $I_{B}$. The quadrupoles are on a second power supply that determines $I_{Q}$. Q1Q2Q3 have a 2000 Amp bypass that determines $I_{Q 123}$.

The power supply tolerances depend on how these power supplies are set. It is assumed that the $I_{Q}$ power supply is set by monitoring $I_{Q}-I_{B}$, and the $I_{Q 123}$ bypass is set by monitoring $I_{Q 123}-I_{B}$.

In the case of the $I_{Q 123}$ bypass, one can think of several other current combinations that one might monitor. The above choice tends to make $\Delta \nu_{B}$ small.

In order to find the current tolerances one has to distribute the allowed $\Delta \nu=1 \times 10^{-3}$ among the 3 sources. To do this in a reasonable way, one has to rewrite Eq. (1) so that the currents being monitored, $I_{Q}-I_{B}$ and $I_{Q 123}-I_{B}$ are obviously displayed. Let us write

$$
\begin{aligned}
I_{Q} & =I_{B}+\left(I_{Q}-I_{B}\right), \\
I_{Q 123} & =I_{B}+\left(I_{Q 123}-I_{B}\right) .
\end{aligned}
$$

Then

$$
\begin{aligned}
\Delta \nu & =\left(C_{B}+C_{Q} \frac{I_{B}}{I_{Q}}+C_{Q 123} \frac{I_{B}}{I_{Q 123}}\right) I_{B} \\
& +C_{Q} \frac{\Delta\left(I_{Q}-I_{B}\right)}{I_{Q}}+C_{Q 123} \frac{\Delta\left(I_{Q 123}-I_{B}\right)}{I_{Q 123}}
\end{aligned}
$$

For $\beta^{*}=6$

$$
\Delta \nu=11\left(\frac{\Delta I}{I}\right)_{B}+31 \frac{\Delta\left(I_{Q}-I_{B}\right)}{I_{Q}}+16 \frac{\Delta\left(I_{Q 123}-I_{B}\right)}{I_{Q 123}}
$$

We assume the 3 terms are uncorrelated and will add quadratically. We then allow $1 / \sqrt{3} \times$ $10^{-3}=0.58 \times 10^{-3}$ for each term. This gives the current tolerances at $\gamma=30$

$$
\begin{aligned}
\left(\frac{\Delta I}{I}\right)_{B} & =\frac{0.58 \times 10^{-3}}{11}=5.3 \times 10^{-5} \\
\frac{\Delta\left(I_{Q}-I_{B}\right)}{I_{Q}} & =\frac{0.58 \times 10^{-3}}{31}=1.9 \times 10^{-5} \\
\frac{\Delta\left(I_{Q 123}-I_{B}\right)}{I_{Q}} & =\frac{0.58 \times 10^{-3}}{16} \times \sqrt{6}=8.9 \times 10^{-5}
\end{aligned}
$$

It has been assumed that the 6 Q1Q2Q3 bypasses are independently powered.

For $\beta^{*}=2$
One can compute the $\Delta \nu$ due to each term using the above tolerances. One finds

$$
\Delta \nu=31\left(\frac{\Delta I}{I}\right)_{B}+31 \frac{\Delta\left(I_{Q}-I_{B}\right)}{I_{Q}}+47 \frac{\Delta\left(I_{Q 123}-I_{B}\right)}{I_{Q}}
$$

Thus at $\gamma=30$

$$
\begin{aligned}
\Delta \nu_{B} & =1.6 \times 10^{-3} \\
\Delta \nu_{Q} & =0.58 \times 10^{-3} \\
\Delta \nu_{Q 123} & =1.74 \times 10^{-3}
\end{aligned}
$$

These $\Delta \nu$ are too large, but one can introduce $\beta^{*}=2$ at higher energies where these $\Delta \nu$ become smaller. The above $\Delta \nu$ are for $6 \beta^{*}=2$ insertions.

The above analysis can be applied to a new design of Q1Q2Q3 where $I_{Q 123} \simeq 5600$. The main change is that $\Delta \nu_{B}$ becomes smaller. The tolerances on $\Delta\left(I_{Q}-I_{B}\right) / I_{Q}$ and $\Delta\left(I_{Q 123}-I_{B}\right) / I_{Q 123}$ are unchanged.

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