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Shunt impedance measurements using the bead perturbation technique

C. Quiery

July 1993

Collider Accelerator Department Brookhaven National Laboratory

# **U.S. Department of Energy**

USDOE Office of Science (SC)

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### RHIC/RF-10

# **RHIC Project** BROOKHAVEN NATIONAL LABORATORY

**RHIC/RF** Technical Note No. 10

Shunt Impedance Measurements Using the Bead Perturbation Technique

> C. Quiery J. Rose S. Ellerd

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## SHUNT IMPEDANCE MEASUREMENTS USING

### THE BEAD PERTURBATION TECHNIQUE

C. Quiery J. Rose S. Ellerd

#### Brookhaven National Laboratory July 1993

#### Introduction

The shunt impedance of the rf accelerator cavities is measured using a beadpull test set. The method is based upon the field perturbation technique developed by Slater.<sup>1</sup> The perturbation of the electromagnetic fields caused by a metal or ceramic sphere as it moves along the axis of the cavity causes a small change in the resonant frequency of the cavity. The magnitude of this frequency shift, which can be measured to high accuracy, is proportional to the value of the square of the electric and magnetic field at the point of perturbation. A beadpull test set was developed and results were compared to computer models of a test cavity.

#### Computational

The SUPERFISH subset of the Poisson codes were used to calculate the shunt impedance and Q of the test cavity. SUPERFISH calculates either TE or TM modes of axisymmetric cylindrical cavities based on the boundary conditions. The SUPERFISH results were used as a method of comparison for the data obtained from the beadpull test. SUPERFISH is quite accurate when dealing with the fundamental mode and with perfectly

1

axisymmetrical cavities. However, when the cavity symmetry is broken by either tuners, amplifiers, or mode dampers, the code results are no longer exact and another method is needed to measure the field distribution. The objective of the beadpull is to supplement our computational tools in determining shunt impedance and field patterns. This is especially true for transverse modes in asymmetric cavities.

The boundary conditions that delineated the physical regions inside the cavity was the input file for AUTOMESH. AUTOMESH creates a file called TAPE73 which is used for the LATTICE program. LATTICE fills the defined regions with an irregular triangular mesh that fits the boundaries of the cavity. SUPERFISH is the eigenvalue solver which calculates the resonant frequency and determines the magnetic field values throughout the mesh problem. The cavity boundary is shown in Appendix 1. The SUPERFISH output routine, SF01, accepts the input file and prints information about the properties of the cavity. All quantities appearing in the output of SUPERFISH are normalized by assuming that the average electric field on the axis is 1MV/meter. The SF01 output file contains the value of  $E_z$  at points on the axis, the values of moment integrals of  $E_z$  along the axis, and tables for each segment on which power and frequency calculations were sought. The SUPERFISH output postprocessor (Appendix 2) also provides us with the data we need to calculate R/Q. R is the shunt impedance and Q is the ratio of the time-average energy stored at a resonant frequency to the energy dissipated in one period of this frequency. According to SUPERFISH calculations, the shunt impedance and quality factor, Q, for the small scale model was  $0.394543M\Omega$  and 5716, respectively. The R/Q value was calculated as 69.02 ohms. This value of R/Q could now be used as a comparison in the bead perturbation test.

2

#### **BEAD PERTURBATION TEST**

#### Theory

The perturbation theory demonstrates that the introduction of a small body into a resonant electromagnetic cavity will change the frequency by an amount that is related to the size, shape, and material of the object and the values of the electric and magnetic fields of the cavity. There are two important conditions that must be remembered when applying the perturbation theory.<sup>2</sup> One, is that the theory is only applicable for infinitesimal perturbations, and strictly speaking cannot be applied for finite distortions. Second, the formulas about to be derived will not hold when any distortion is made from a situation not originally satisfying the boundary conditions. This is due to the fact that the perturbation formula is based on the unperturbed electric and magnetic fields satisfying the boundary conditions is introduced. In practice, this method may be used as long as the perturbation is small and does not distort the fields patterns in the cavity.

The frequency shift due to the introduction of a perturbing sphere in an electromagnetic resonant cavity is derived by Papas<sup>3</sup> as:

$$\frac{-\delta\omega_0}{\omega_0} = \frac{3\mu_0\frac{\mu_1-\mu_0}{\mu_1+2\mu_0}H_0H_0^*+3\epsilon_0\frac{\epsilon_1-\epsilon_0}{\epsilon_1+2\epsilon_0}E_0E_0^*}{4U}\Delta V$$

where  $\omega_{o}$  = resonant frequency

$$\epsilon_1 = \epsilon_0 \epsilon_r$$
  
 $\epsilon_0 = 8.85*10^{-12} (F/m)$ 

$$V = volume of the bead (m3)$$

$$U = total stored energy in cavity (J)$$

A perturbation consisting of a dielectric sphere introduced into the cavity affects only electric fields, and so one can neglect the magnetic field contributions. Therefore, for a ceramic sphere, the equation above becomes:

$$\frac{-\delta\omega_0}{\omega_0} = \frac{3\epsilon_0 \frac{\epsilon_1 - \epsilon_0}{\epsilon_1 + 2\epsilon_0} E_0 E_0^*}{4U} \Delta V$$

Since a perfectly conducting metal can be considered as having  $\mu_1=0$  and  $\epsilon_1=\infty$ , the frequency shift produced by a metal sphere is:

$$\frac{-\delta\omega_0}{\omega_0} = \frac{-\frac{3}{2}\mu_0H_0H_0^* + 3\epsilon_0E_0E_0^*}{4U}\Delta V$$

It should be noted that the frequency shift is proportional to the magnitude of the field strength and differs in sign for electric and magnetic fields. In order to determine magnetic field properties, it is necessary to use both dielectric and metallic spheres of equal size and subtract the data sets. Solving for the electric field of the ceramic sphere gives:

$$E = \left[\frac{4U}{3\epsilon_0 \Delta V} \frac{\epsilon_r + 2}{\epsilon_r - 1} \frac{\delta \omega_0}{\omega_0}\right]^{1/2}$$

For a cavity of length l at power P,

$$R = \frac{\left(\frac{1}{I}\int_{0}^{I} Edz\right)^{2}}{2P}$$

Since 
$$Q = 2\pi$$
 (stored energy)  $= \omega_0 W$   
energy loss/cycle P

then R/Q for the ceramic sphere can be found with the following equation:

$$\frac{R}{Q} = \frac{2}{3\epsilon_0 \omega_0^2 I \Delta V} \frac{\epsilon_r + 2}{\epsilon_r - 1} \left( \int_0^I \sqrt{\delta \omega_0} dI \right)^2$$

#### Setup

The beadpull test on the cavity was done once with a metal sphere and again with a dielectric sphere. The sphere was brought through the cavity fields on a nylon monofilament which was suspended in a loop over four small reels. The tension in the monofilament was kept very taut in order to minimize sagitta and the amplitude of vertical vibrations. A very important fact to note is that this monofilament does not affect the fields in the cavity. One of the reels was driven by a motor in order to keep the velocity of the sphere constant. The bead would move through the entire gap, stop, and then return to its original position along the same center axis. The resonant frequency of the cavity was

found using a network analyzer. In the case of our test cavity, the resonant frequency was found to be 141.39Mhz. This frequency is entered into a signal generator whose output is coupled to the RF cavity. The pickup signal from the other end of the cavity is amplified and fed into a mixer with the signal from the generator. The diagram of the bead perturbation setup is shown in Appendix 3. The beadpull test set uses a double balanced mixer (DBM) as a phase error detector to phase lock the synthesized frequency source to the cavity.<sup>2</sup> This is done by comparing a sample of the drive signal to the pickup from the cavity. The two signals entering the mixer are adjusted, with a phase shifter, so that the reading on the output of the mixer is 0 volts DC when there is no perturbation to the cavity. The output is then used to drive the voltage controlled oscillator (VCO) to maintain a zero phase error at the DBM. The voltage required to do this is proportional to the frequency shift of the cavity due to the perturbation introduced. This voltage is read by an oscilloscope via Labview. This voltage is directly proportional to the frequency to which the VCO in the signal generator was driven to maintain zero phase error at the mixer. In order to directly relate this change in voltage with a shift in frequency, a calibration sequence programmed a set of three frequency steps (5kHz, 10kHz, 15kHz) to the signal generator. See Figure 1 for an example of the calibration sequence of the metal sphere. The resulting oscilloscope reading is then stored in memory.

#### Calculations

The output data from Labview was arranged in two columns, consisting of time(position) and voltage(frequency) data, and entered into MATHCAD where the remaining calculations

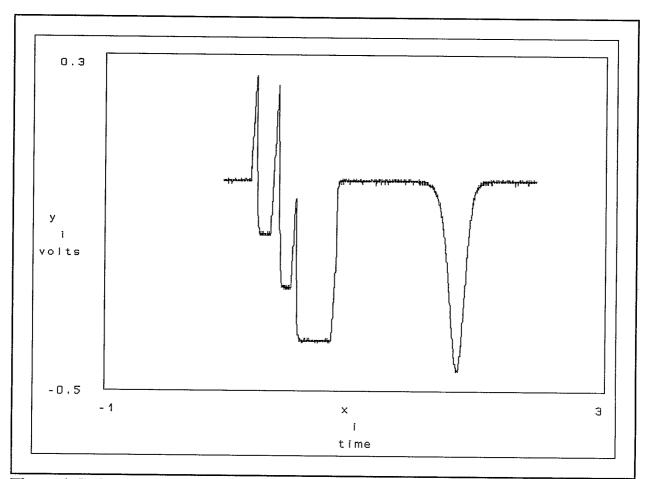


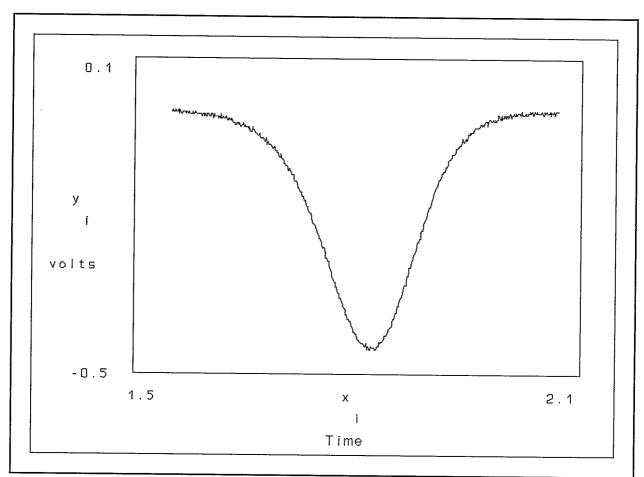
Figure 1 Calibration Sequence of Metal Sphere

were done. See Figure 2 for the graph of output data for the metal sphere.

The value of  $\epsilon_r$  for the ceramic sphere was found to be 9.7. In the case of the metal sphere,  $(\epsilon_r+2)/(\epsilon_r-1)$  drops out of the equation. The beadpull was done on axis for the fundamental mode and it was assumed that the magnetic field is zero in the gap. Thus the equation for  $\delta\omega_0/\omega_0$  of the metal sphere reduces to:

$$\frac{\delta\omega_0}{\delta\omega_0} = \frac{3\epsilon_0 E_0 E_0^*}{4U} \Delta V$$

The perturbing volume, $\Delta V$ , for the ceramic sphere equals the volume of the entire sphere minus the volume of the hole. However, the volume of the hole in the metal sphere was



### Figure 2 Output Data for Metal Sphere

neglected because the electric field goes to zero inside a hollow metal sphere. The length, l, of the cavity, refers to the length of all the field regions over which the integration is performed. Since the data is taken as a function of time, and must be converted to dimensions of length, l was found by taking the number of seconds per reading set on the scope and multiplying it by the number of readings in the beadpull data, and then multiplying it by the speed in which the sphere was moving. The accuracy of this measurement is maintained by using a stepper motor with a constant and highly repeatable number of steps per second.

As can be seen from the MATHCAD calculations in Appendix 4, the R/Q value for the ceramic sphere was 70.137 $\Omega$ . Similar calculations were performed for the metal sphere resulting in an R/Q value of 70.22 $\Omega$ . Therefore, the metal sphere differs from the reference value of 69.02 $\Omega$  in SUPERFISH by only 1.7%, while the ceramic sphere data differs by 1.6% which demonstrates that the bead perturbation results are in excellent agreement with our computational results. If the magnetic field in the gap was non-zero, a value of R/Q less than SUPERFISH would have resulted. A non-zero magnetic field could be caused by a beadpull that is not exactly on axis, thereby causing a reduction in the measured frequency shift.

The quality factor, Q, of the system was found on a network analyzer. Two methods were employed to find the value of Q. A Smith Chart(Appendix 5) was utilized to find the unloaded Q of the cavity. The unloaded  $Q_0$  includes only those losses in the cavity alone. A log magnitude scale(Appendix 6), on the other hand, was used to find the loaded  $Q_L$ , which includes all sources of dissipation. The relation between the various Q's is:

$$\frac{1}{Q_L} = \frac{1}{Q_0} + \frac{\beta}{Q_0}$$

Since the cavity was found to be undercoupled, the value of  $\beta < <1$ . From this, the value of  $Q_L$  should be comparable with that of  $Q_0$ , but slightly smaller. Usually it is the value of  $Q_0$  that is used to find the shunt impedance, but since our measured value of  $Q_0$  was very similar to  $Q_L$  but still smaller, we took the average of the two(1,891) as our overall value of Q. As a result, the shunt impedance of the cavity was found to be 133k $\Omega$ . This departure from the theoretical value is due to additional losses in the test cavity that are not taken

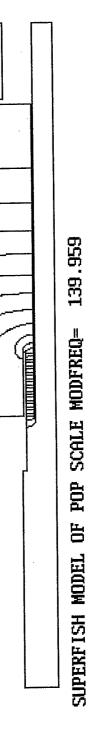
into account by SUPERFISH. These losses are due to the cavity's rf joints and to the substitution of brass for copper in many sections of the cavity which lowers the conductivity. For the actual 26MHz accelerating cavity, the measured Q is  $\approx 85\%$  of the theoretical value and a closer agreement between calculated and measured shunt impedance is expected.

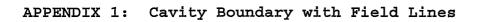
#### Conclusion

R/Q of an rf cavity was measured using the bead perturbation technique and compared with computational (SFISH) results. The agreement, to within 2% confirms the reliability of the approach for measuring R/Q of high Q structures. Future work will include automation of the data reduction utilizing Labview, a program development application which uses a graphical programming language to create programs in block diagram form. Another task will be designing a low-pass filter on the output of the DBM in order to reduce noise to provide a better signal to noise ratio in larger cavities where the frequency shifts to be measured are smaller.

### **<u>References</u>**

- 1. S.C. Slater, Microwave Electronics, March 1950.
- 2. C.H. Papas "On Perturbation Theory of Electromagnetic Cavity Resonators" California Institute of Technology, March 1954, Pasadena, California.
- 3. L.C. Maier Jr. "Field Strength Measurements in Resonant Cavities" Massachusetts Institute of Technology, November 2, 1949.
- 4. James Rose, "Radio Frequency Quadrupole Accelerator", Polytechnic University, June 1990.





JIST 3365 3410 07-14-93 17:04 OUTSF1.LIS Full cavity length [2L] = 122.7354 cm Diameter = 15.2400 cmMesh problem length [L] = 61.3677 cm Full drift-tube gap [2g] = 40.0000 cm = 0.5729926Beta Proton energy = 206.567 MeV Frequency [f] (starting value = 139.000) = 139.958710 MHz Eo normalization factor (CON(74)=ASCALE) for 1.000 MV/m = 90136.5 Stored energy [U] for mesh problem only = Power dissipation [P] for mesh problem only = 3101.72217 mJ 477180.28 W Q (2.0\*pi\*f(Hz)\*U(J)/P(W)) =5716 Transit time factor [T] = 0.33053 Shunt impedance [Z] mesh problem only, ((Eo\*L)\*\*2/P) = 0.78922 Mohm Shunt impedance per unit length [Z/L] = 1.286 Mohm/m Effective shunt impedance per unit length [Z/L\*T\*T] = 0.140 Mohm/m Magnetic field on outer wall = 23926 A/m Hmax for wall and stem segments at z = 53.60, r = 2.06 cm = 75036 A/m Emax for wall and stem segments at z = 24.91, r = 2.00 cm = 156.513 MV/m Т Тр S Sp g/L Z/L Beta 0.325904 0.57299262 0.33053 0.18483 0.94014 0.06382 1.286049

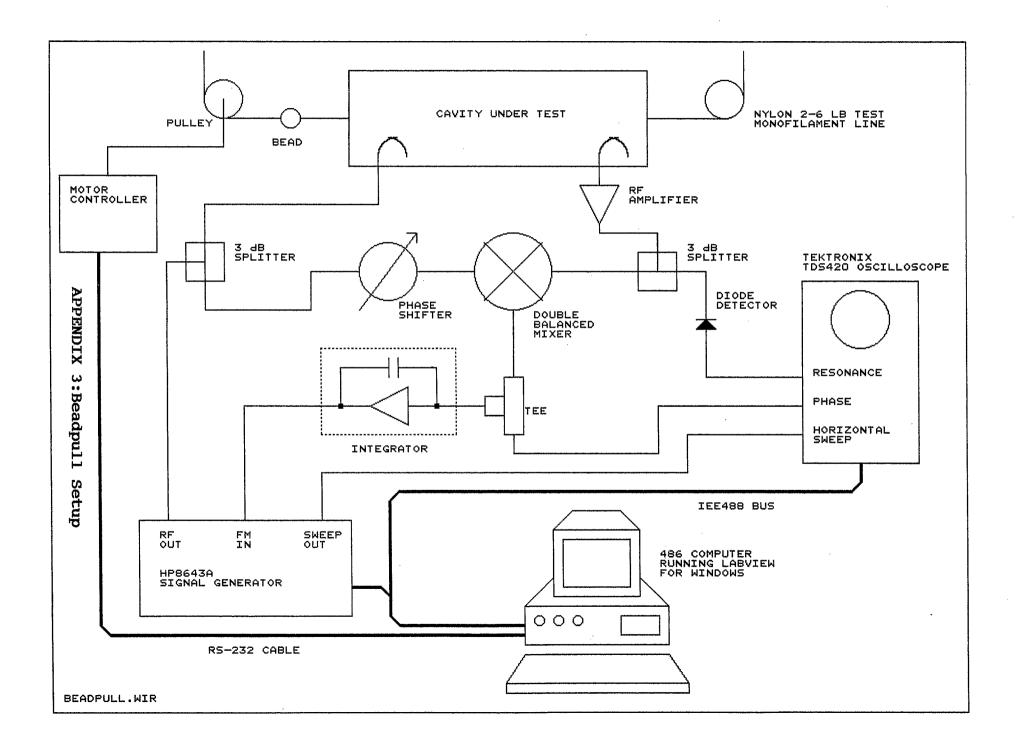
ISEG	zbeg	rbeg	zend	rend	Emax*epsrel	Power	df/dz df/dr
	(cm)	(cm)	(cm)	(cm)	(MV/m)	(W)	(MHz/mm)
Command					St: d8kMpcwT	Keys: arro	ows X=exit ?=Help

JIST	3388	3410	07-14-93	17:04	OUTSF1.L	IS		T.T. 7 7
Wall								Wall
1	0.0000	0.0000	0.0000	3.1686	0.0000	0.0000	0.0000	0.0000
2	0.0000	3.1686	20.0000	3.1686	0.1433	0.0018	0.0000	0.0000
3	20.0000	3.1686	20.0000	2.7241	0.3567	0.0010	0.0000	0.0000
4	20.0000	2.7241	30.9690	2.7243	105.4048	8765.9063	0.0002	5.8327
5	30.9690	2.7243	30.9690	3.0162	94.6344	1169.9579	0.4215	0.0000
6	30.9690	3.0162	25.0000	3.0162	38.9049	26456.7930	0.0000	-0.1528
7	25.0000	3.0162	25.0000	7.6200	1.3865	12684.8428	-0.1172	0.0000
8	25.0000	7.6200	61.3677	7.6200	30.6048	99416.7813	0.0000	-0.4806
9	61.3677	7.6200	61.3677	4.7333	0.5631	15241.3057	-0.1410	0.0000
10	61.3677	4.7333	54.3150	4.7333	1.5684	47118.2891	0.0000	-0.4334
11	54.3150	4.7333	54.3150	7.4150	24.7467	13812.3125	-0.0652	0.0000
12	54.3150	7.4150	53.7710	7.4150	37.0998	1993.1312	0.0000	0.2884
13	53.7710	7.4150	53.7710	2.0638	24.2711	29881.9375	-0.2080	0.0000
14	53,7710	2.0638	32.0000	2.0638	41.1049	202982.7340	0.0000	-1.3085
15	32.0000	2.0638	31.5000	2.0002	51.4568	2928.4282	0.0159	0.1252
16	31.5000	2.0002	24.8247	2.0002	156.5135	14723.4805	0.0000	7.9571
17	24.8247	2.0002	24.8247	1.8414	153.7094	2.6982	0.4522	0.0000
18	24.8247	1.8414	61.3677	1.8414	65.8864	1.7341	0.0000	0.1138
19	61.3677	1.8414	61.3677	0.0000	0.0000	0.000	0.0000	0.0000
Wall					Total =	477180.3130	*	Wall

Command \*\*\* End-of-file \*\*\*

St: d8kMpcwT Keys: arrows X=exit ?=Help

APPENDIX 2: SUPERFISH Output



#### BEAD.MCD :BEADPULL ANALYSIS 6/22/93 CERAMIC BEAD

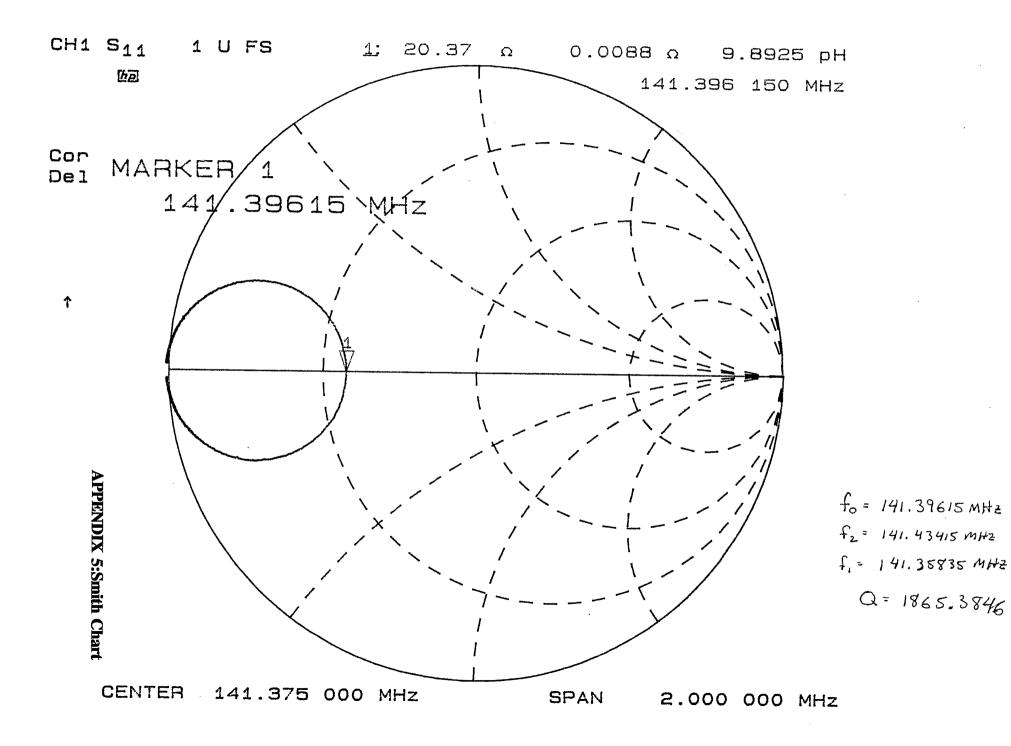
A := READPRN(cerpull) Measure :=  $A^{<1>}$ Calibration := 4.09167 · 10<sup>4</sup> · 2 ·  $\pi$ · Measure

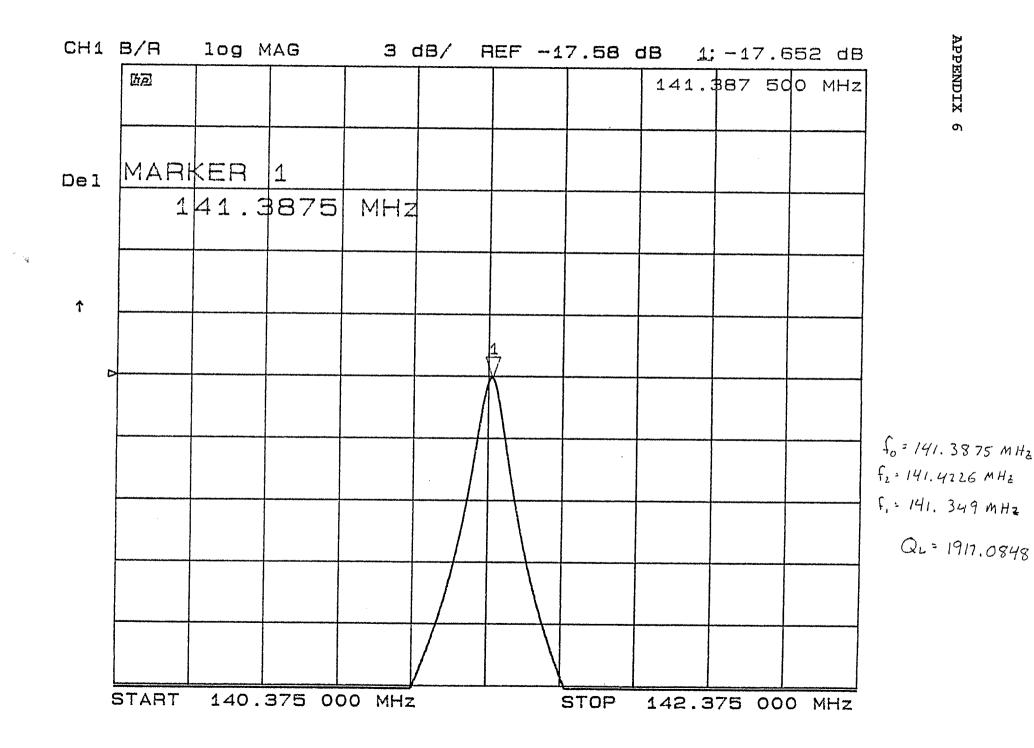
:Voltage Matrix

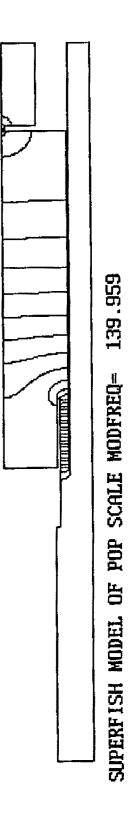
:Calibration to Frequency

Sqrtvolt :=  $\sqrt{|\text{Calibration}|}$  :Square root of each Frequency sumsqrt :=  $\sum (\text{Sqrtvolt} \cdot .72870 \cdot 10^{-4})$  :Sum of the square roots sumsqrt = 8.172

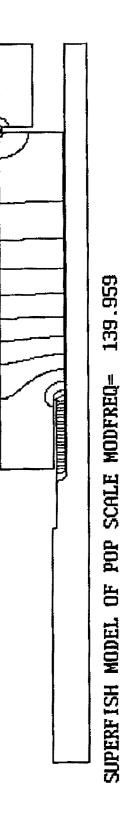
Radcer :=  $\frac{.1245 \cdot 2.54}{100}$ Radcer = 0.003:Radius of the Ceramic Bead (m)Fullbeadvol :=  $\frac{4 \cdot \pi \operatorname{Radcer}^3}{3}$ Fullbeadvol =  $1.325 \cdot 10^{-7}$ :Volume of entire<br/>Bead (m)Radhole :=  $\frac{.04 \cdot 2.54}{100}$ Volhole :=  $\pi \operatorname{Radhole}^2 \cdot \operatorname{Radcer}$ Volhole =  $1.026 \cdot 10^{-8}$ :Volume<br/>of holeNewbeadvol := Fullbeadvol - VolholeNewbeadvol =  $1.222 \cdot 10^{-7}$ :Corrected volume<br/>of Beadlength :=  $\frac{50}{1000} \cdot \frac{100}{5000} \cdot 1108 \cdot .072870$ length = 0.081:Length of gapRespermeter :=  $\frac{4}{6 \cdot 8.85 \cdot 10^{-12} \cdot (2 \cdot \pi \cdot 141.39 \cdot 10^6)^2 \cdot \operatorname{Newbeadvol \cdot length}} \cdot \frac{11.7}{8.7} \cdot \operatorname{sumsqrt}^2$ :R/Q in<br/>ohms/meterRespermeter = 868.682<br/>Shunt := Respermeter \cdot length<br/>Shunt = 70.137:R/Q in ohms



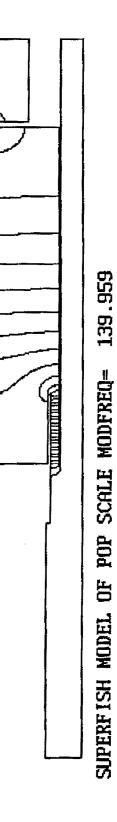




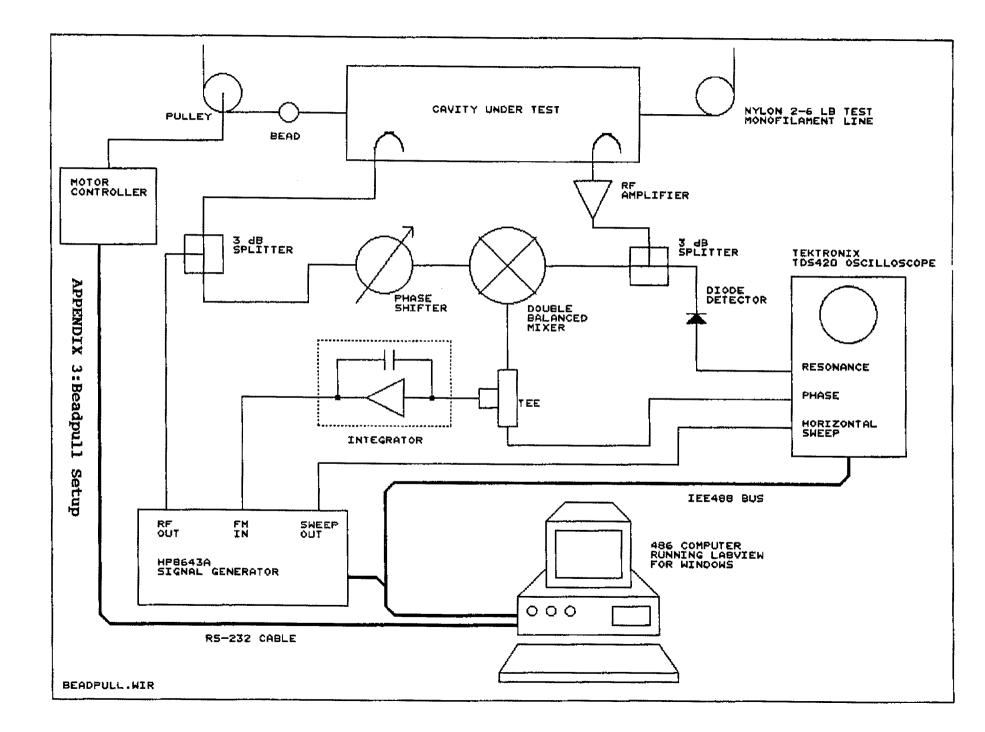
# APPENDIX 1: Cavity Boundary with Field Lines

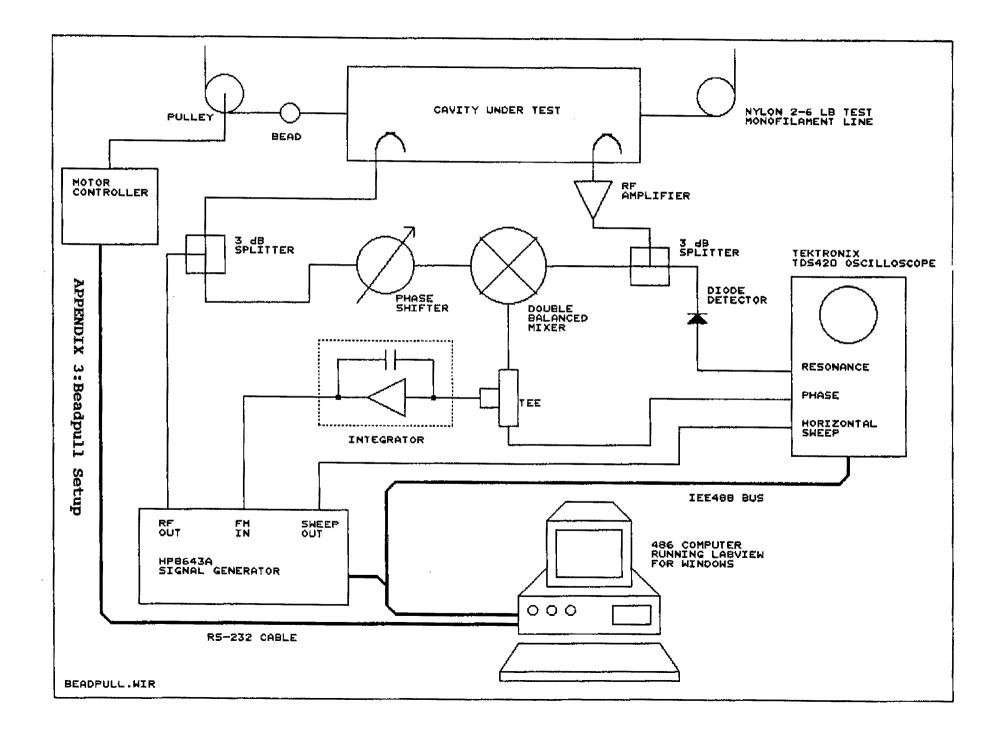


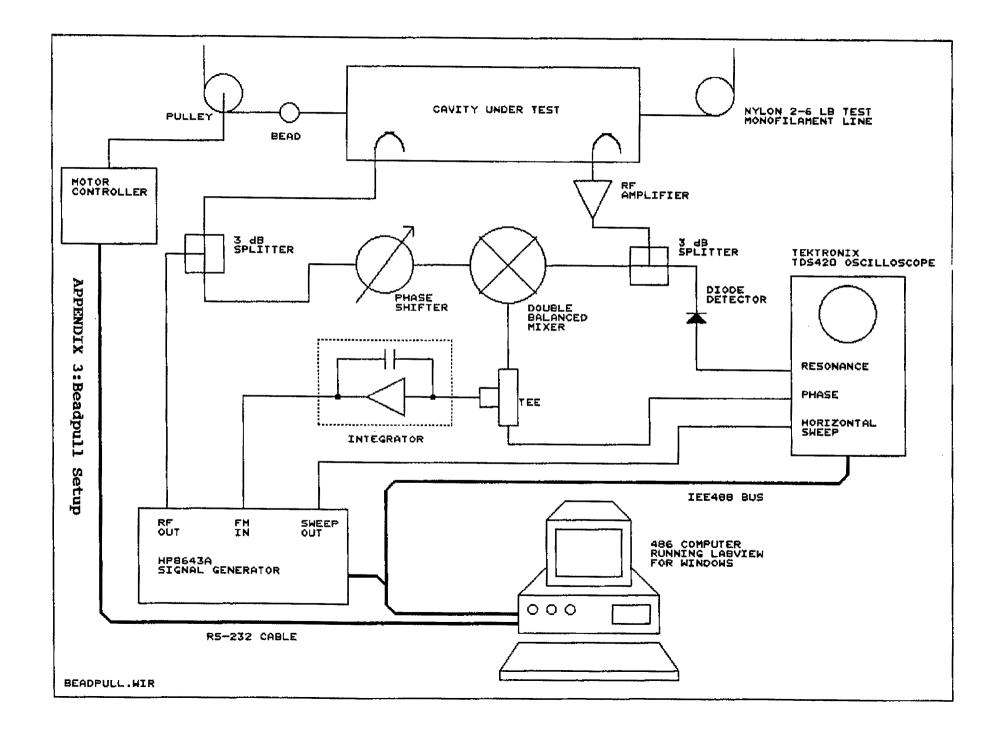
# APPENDIX 1: Cavity Boundary with Field Lines



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Full cavity length [2L] = 122.7354 cm Diameter = 15.2400 cmMesh problem length [L] = 61.3677 cmFull drift-tube gap [2g] = 40.0000 cmBeta = 0.5729926Proton energy = 206.567 MeVFrequency [f] (starting value = 139.000) = 139.958710 MHz Eo normalization factor (CON(74)=ASCALE) for 1.000 MV/m = 90136.5Stored energy [U] for mesh problem only = 3101.72217 mJ Power dissipation [P] for mesh problem only = 477180.28 W Q (2.0\*pi\*f(Hz)\*U(J)/P(W))= 5716 Transit time factor [T] =0.33053 Shunt impedance [Z] mesh problem only,  $((Eo^*L)^{**2/P}) =$ 0.78922 Mohm Shunt impedance per unit length [Z/L] =1.286 Mohm/m Effective shunt impedance per unit length [Z/L\*T\*T] =0.140 Mohm/m Magnetic field on outer wall = 23926 A/m Hmax for wall and stem segments at z = 53.60, r = 2.06 cm =75036 A/m Emax for wall and stem segments at z = 24.91, r = 2.00 cm =156.513 MV/m

Beta T Tp S Sp g/L Z/L 0.57299262 0.33053 0.18483 0.94014 0.06382 0.325904 1.286049

\_\_\_\_\_

ISE	G zbeg	rbeg	zend	rend	Emax*ep	srel Power	df/d	z df/dr
(cm)			(cm)					(z/mm)
Wall					Wall			
1	0.0000	0.0000	0.0000					0.0000
2	0.0000	3.1686	20.0000	3.1686	0.1433	0.0018 0	0000.	0.0000
3	20.0000	3.1686	20.0000	2.7241	0.3567	0.0010 (	0.0000	0.0000
4	20.0000	2.7241	30.9690	2.7243	105.4048			
5	30.9690	2.7243	30.9690	3.0162	94.6344	1169.9579	0.4215	0.0000
6	30.9690	3.0162	25.0000	3.0162	38.9049	26456.7930	0.0000	
7	25.0000	3.0162	25.0000	7.6200	1.3865	12684.8428	-0.1172	0.0000
8	25.0000	7.6200	61.3677	7.6200	30.6048	99416.7813	0.0000	-0.4806
9	61.3677	7.6200	61.3677	4.7333	0.5631	15241.3057	-0.1410	0.0000
10	61.3677	4.7333	54.3150	4.7333	1.5684	47118.2891	0.0000	-0.4334
11	54.3150	4.7333	54.3150	7.4150	24.7467	13812.3125	-0.0652	0.0000
12	54.3150	7.4150	53.7710	7.4150	37.0998	1993.1312	0.0000	0.2884
13	53.7710	7.4150	53.7710	2.0638	24.2711	29881.9375	-0.2080	
14	53.7710	2.0638	32.0000	2.0638	41.1049	202982.7340	0.0000	
15	32.0000	2.0638	31.5000	2.0002	51.4568	2928.4282	0.0159	0.1252
16	31.5000	2.0002	24.8247	2.0002	156.5135	14723.4805		
17	24.8247	2.0002	24.8247	1.8414	153.7094	2.6982	0.4522	0.0000
18	24.8247	1.8414	61.3677				0.0000	0.1138
19	61.3677	1.8414	61.3677	0.0000	0.0000			0.0000
WallWall = 477180.3130Wall								

Full cavity length [2L] = 122.7354 cm Diameter = 15.2400 cmMesh problem length [L] = 61.3677 cmFull drift-tube gap [2g] = 40.0000 cm= 0.5729926Beta Proton energy = 206.567 MeVFrequency [f] (starting value = 139.000) = 139.958710 MHz Eo normalization factor (CON(74)=ASCALE) for 1.000 MV/m = 90136.5Stored energy [U] for mesh problem only = 3101.72217 mJ Power dissipation [P] for mesh problem only = 477180.28 W Q (2.0\*pi\*f(Hz)\*U(J)/P(W)) =5716 Transit time factor [T] =0.33053 Shunt impedance [Z] mesh problem only,  $((Eo^*L)^{**2/P}) =$ 0.78922 Mohm Shunt impedance per unit length [Z/L] =1.286 Mohm/m Effective shunt impedance per unit length [Z/L\*T\*T] =0.140 Mohm/m Magnetic field on outer wall = 23926 A/m Hmax for wall and stem segments at z = 53.60, r = 2.06 cm =75036 A/m Emax for wall and stem segments at z = 24.91, r = 2.00 cm =156.513 MV/m Beta T Tp S Sp g/L Z/L 0.57299262 0.33053 0.18483 0.94014 0.06382 0.325904 1.286049 ISEG zbeg rbeg zend rend Emax\*epsrel Power df/dz df/dr (cm) (cm) (cm) (cm)(MV/m)(W) (MHz/mm) Wall--------Wall 0.0000 0.0000 0.0000 1 3.1686 0.0000  $0.0000 \quad 0.0000 \quad 0.0000$ 0.0000 3.1686 20.0000 2 3.1686 0.1433 0.0018 0.0000 0.0000 3 20.0000 3.1686 20.0000 2.7241 0.3567 0.0010 0.0000 0.0000 4 20.0000 2.7241 30.9690 2.7243 105.4048 8765.9063 0.0002 5.8327 5 30.9690 2.7243 30.9690 3.0162 94.6344 1169.9579 0.4215 0.0000 6 30.9690 3.0162 25.0000 3.0162 38.9049 26456.7930 0.0000 -0.1528 7 25.0000 3.0162 25.0000 7.6200 1.3865 12684.8428 -0.1172 0.0000 8 25.0000 7.6200 61.3677 7.6200 30.6048 99416.7813 0.0000 -0.4806 9 61.3677 7.6200 61.3677 4.7333 0.5631 15241.3057 -0.1410 0.0000 10 61.3677 4.7333 54.3150 4.7333 1.5684 47118.2891 0.0000 -0.4334 11 54.3150 4.7333 54.3150 7.4150 24.7467 13812.3125 -0.0652 0.0000 12 54.3150 7.4150 53.7710 7.4150 37.0998 1993.1312 0.0000 0.2884 13 53.7710 7.4150 53.7710 2.0638 24.2711 29881.9375 -0.2080 0.0000 14 53.7710 2.0638 32.0000 2.0638 41.1049 202982.7340 0.0000 -1.3085 15 32.0000 2.0638 31.5000 2.0002 51.4568 2928.4282 0.0159 0.1252 16 31.5000 2.0002 24.8247 2.0002 156.5135 14723.4805 0.0000 7.9571 17 24.8247 2.0002 24.8247 1.8414 153.7094 2.6982 0.4522 0.0000 18 24.8247 1.8414 61.3677 1.8414 65.8864 1.7341 0.0000 0.1138 19 61.3677 1.8414 61.3677 0.0000 0.0000 0.0000 0.0000 0.0000 Wall-----Wall = 477180.3130 ------Wall

#### BEAD.MCD :BEADPULL ANALYSIS 6/22/93 CERAMIC BEAD

A := READPRN(cerpull) Measure :=  $A^{<1>}$ Calibration := 4.09167 · 10<sup>4</sup> · 2 ·  $\pi$  Measure

:Voltage Matrix ;Calibration to Frequency

Sqrtvolt :=  $\sqrt{|\text{Calibration}|}$ :Square root of each Frequencysumsqrt :=  $\sum (\text{Sqrtvolt}.72870 \cdot 10^{-4})$ :Sum of the square rootssumsqrt = 8.172

Radcer :=  $\frac{.1245 \cdot 2.54}{100}$ Radcer = 0.003:Radius of the Ceramic Bead(m)Fullbeadvol :=  $\frac{4 \cdot \pi \cdot \text{Radcer}^3}{3}$ Fullbeadvol = 1.325 \cdot 10 7:Volume of entire<br/>Bead (m)Radhole :=  $\frac{.04 \cdot 2.54}{100}$ Volhole :=  $\pi \cdot \text{Radhole}^2 \cdot \text{Radcer}$ Volhole = 1.026 \cdot 10^{-8}:Volume<br/>of holeNewbeadvol := Fullbeadvol - VolholeNewbeadvol = 1.222 \cdot 10^{-7}:Corrected volume<br/>of Beadlength :=  $\frac{50}{1000} \cdot \frac{100}{5000} \cdot 1108 \cdot .072870$ length = 0.081:Length of gapRespermeter :=  $\frac{4}{6 \cdot 8.85 \cdot 10^{-12} \cdot (2 \cdot \pi \cdot 141.39 \cdot 10^6)^2 \cdot \text{Newbeadvol·length}} \cdot \frac{11.7}{8.7} \cdot \text{sumsqrt}^2$ :R/Q in<br/>ohms/meter

 $\frac{1}{6 \cdot 8.85 \cdot 10^{-12} \cdot (2 \cdot \pi \cdot 141.39 \cdot 10^6)^2}$  Newbeadvol·length 8.7 ohms/meter Respermeter = 868.682 Shunt := Respermeter-length

Shunt = 70.137

:R/Q in ohms

