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Requested Systematic Body b_5 Multipoles in RHIC Triplet Quadrupoles

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Abstract

In this report, we summarize the compensation methods of the allowed magnetic multipole b_5 in the interaction region (IR) triplet magnet that consists of body-ends compensation, tuning shimming, and local corrections. From the experience gained so far with the on-site production of Q1 magnets of series number less than 8, the amount of b_5 in the body is requested to be -1.2 unit in order to compensate for the effects caused by the strong b_5 at the lead and return ends. This body-ends compensation allows for the tuning shims to be adequately used only for the correction of random errors in each magnet.

1. Introduction

During the storage of heavy-ion beam in RHIC, the magnetic field quality in the triplet quadrupoles crucially determines the dynamic aperture and the beam lifetime when the β^* is lowered to 1 meter. Define the magnetic multipole in terms of the quadrupole "prime" units,

$$B_y + iB_x = G_0(x + iy) \left[1 + 10^{-4} \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{R_0} \right)^{n-1} \right].$$
(1)

and the integrated multipole

$$B_n=\int b_n ds,$$

where the reference radius $R_0 = 40.625$ mm and the nominal quadrupole gradient $G_0 = 47$ T/m for the 130 mm diameter triplet quadrupoles. Table 1 shows the expected values of magnetic multipole harmonics in the body, lead end, and return end of the triplet quadrupole at the current 5000 Amps for storage.

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Expected values of body harmonics (Unit):

n	$\langle b_n \rangle$	$d(b_n)$	$sig(b_n)$	$\langle a_n \rangle$	$d(a_n)$	$sig(a_n)$
1	0	0	10	0	0	0
2	0.5	0	2.4	0.1	0	1.2
3	0	1.0	0.6	0.3	0	0.7
4	0.3	0	0.6	0.1	0	0.5
5	-1.2	1.5	0.5	-0.4	0	0.6
6	0.12	0	0.11	-0.09	0	0.12
7	-0.1	0.05	0.05	-0.03	0	0.12
8	-0.04	0	0.05	0.05	0	0.09
9	0.0	0.2	0.03	0.03	0	0.03

Expected values of harmonics in lead end (Unit-m):

n	$\langle B_n \rangle$	$d(B_n)$	$sig(B_n)$	$\langle A_n \rangle$	$d(A_n)$	$sig(A_n)$
1	0	0	0	0	0	0
2	-0.1	0	0.7	-1.	0	2.
3	-0.3	0	0.3	0.4	0	0.8
4	0.1	0	0.3	0.3	0	0.4
5	4.6	0.5	0.3	-1.5	0.5	0.2
6	0.01	0	0.04	-0.06	0	0.06
7	0.04	0	0.05	-0.02	0	0.01
8	0.04	0	0.05	-0.02	0	0.02
9	-0.5	0.05	0.02	0.2	0.05	0.03

Expected values of harmonics in return end (Unit-m):

n	$\langle B_n \rangle$	$\mathrm{d}(B_n)$	$sig(B_n)$	$\langle A_n \rangle$	$\mathrm{d}(A_n)$	$sig(A_n)$
1	0	0	0	0	0	0
2	0.3	0	1.8	0.7	0	1.
3	-0.1	0	0.2	-0.1	0	0.3
4	0	0	0.25	0.2	0	0.2
5	1.	0	0.6	-0.1	0	0.1
6	0.06	0	0.03	0.06	0	0.02
7	-0.01	0	0.02	-0.02	0	0.05
8	0.03	0	0.03	-0.01	0	0.02
9	-0.1	0	0.03	0.04	0	0.01

Table 1: Expected values of harmonics in body, lead end, and return end of the 130 mm insertion quadrupoles at 5000 A. Here, $\langle b_n \rangle = \text{mean}$, $d(b_n) = \text{uncertainty in mean}$, $sig(b_n) = sigma$ for b_n .

The allowed magnetic multipoles in the quadrupole configuration are b_1, b_5, b_9, \cdots . The effect of b_1 errors can be easily compensated by the tuning quadrupoles during the operation. The correction of b_5 errors consists of body-ends compensation on systematic errors, tuning shimming on random errors, and additional local correction by triplet correctors. Since there is no correction on multipoles of higher order than 5, the tolerable amount of b_9 errors is determined by tune-spread analysis and dynamic aperture studies.

Based on the measurements of the RHIC triplet quadrupole magnet Q1 of serial numbers less than 8, the lead and return ends of the magnets have significant amount of systematic b_5 multipole component. The integrated b_5 is equal to 4.6 unit m at the lead end and 1.0 unit m at the return end, respectively. The integrated b_9 is equal to 0.6 unit m at the lead end and 1.0 unit m at the return end, respectively. Preliminary studies show that these b_5 errors produce significant tune spreads when the beam is stored in the 1 meter β^* lattice.

This report describes the compensation of b_5 multipole in the triplets. In Section 2, we generally discuss the compensation method based on the minimization of the tune shift and local "kick". In Section 3, we investigated the effectiveness of the body-ends systematic b_5 compensation for the RHIC triplet and compare several alternative compensation schemes. The correction of random b_5 errors is discussed in Section 4. The additional b_5 correction by using two local correctors per triplet is discussed in Section 5. Conclusions and discussion are given in Section 6.

2. Tune Spread and Kick Minimization

The amplitudes of the betatron oscillations reach their maximum values when the particle passes the triplets. On the other hand, the dispersion at the triplet is relatively small. We therefore only consider the amplitude effects on the particle motion from the nth-order magnetic multipole error. In the following, we discuss the compensation schemes based on the minimization of the transverse tune spreads and the local kicks at each triplet.

2.1. Kick minimization

We minimize the multipole kick using the horizontal plane as an example. The analysis for the vertical plane is similar. The change of transverse momentum $p_x \equiv dx/ds$ for the on-momentum particle produced by the magnetic multipole b_n is

$$\frac{dp_x}{ds} = -\left(\frac{10^{-4}G_0}{B_0\rho R_0^{n-1}}\right)b_n x^n \tag{2}$$

where $B_0\rho$ is the momentum of the particle. The change of the momentum results in a change in the action J_x , which is otherwise a constant of motion. The action J_x can be written as

$$J_x = \frac{1}{2\beta_x} \left[x^2 + (\alpha_x x + \beta_x p_x)^2 \right]$$
(3)

where

$$x = \sqrt{2J_x\beta_x}\cos\chi, \quad p_x = -\sqrt{\frac{2J_x}{\beta_x}}(\sin\chi_x + \alpha_x\cos\chi_x)$$
 (4)

with χ_x the betatron phase in the absence of perturbation. Here, $2\pi R$ is the circumference, and α_x and β_x are the Courant-Snyder lattice functions. In the presence of the multipole error b_n , the change of the action can be derived from Eq. 2,

$$\frac{\Delta J_x}{J_x} = \left(\frac{10^{-4}G_0}{B_0\rho R_0^{n-1}}\right) b_n L\beta_x^{\frac{n+1}{2}} (2J_x)^{\frac{n-1}{2}} (2\sin\chi_x\cos^n\chi_x) \tag{5}$$

where L is the length of the magnet. Typically, the total length (e.g. about 10 meters for RHIC) of each triplet is much smaller that the value of the amplitude function β (e.g. from 600 to 1400 meters for RHIC 1 $m \beta^*$ operation). Therefore, there is essentially no betatron phase advance within the triplet. Consequently, the quantity $\Delta J_x/J_x$ can be minimized if the quantities

$$K_{nx} = \int_{\text{trip}} \frac{G}{G_0} \beta_x^{\frac{n+1}{2}} b_n ds, \quad \text{and} \quad K_{ny} = \int_{\text{trip}} \frac{G}{G_0} \beta_y^{\frac{n+1}{2}} b_n ds \tag{6}$$

are both minimized. Here, the integrals extend over all the elements within one triplet. The quadrupole gradients G of the RHIC triplet quadrupoles Q1, Q2, and Q3 at storage are given by Table 2, where DFD and FDF denote polarity of the magnets Q1, Q2, and Q3 of the triplet pair near the interaction point (IP). The nominal gradient G_0 is chosen to be 47 T/m.

2.2. Tune spread minimization

In order to accommodate the independent adjustment of each IP, we minimize the tune spread generated by the pair of triplets located near each IP. In the case that the multipole

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of interest produces first-order tune shifts, we use the well-known tune-shift formula (e.g. Eq. 7 in Ref. 1)

$$\Delta \nu_{x} = \frac{10^{-4}G_{0}}{B_{0}\rho R_{0}^{n-1}} \oint \frac{\beta_{x}ds}{2\pi} \left\{ C_{1} + 3C_{2}\beta_{x}J_{x} - 6C_{2}\beta_{y}J_{y} + \frac{15}{2}C_{3}\beta_{x}^{2}J_{x}^{2} - 45C_{3}\beta_{x}\beta_{y}J_{x}J_{y} + \frac{45}{2}C_{3}\beta_{y}^{2}J_{y}^{2} \right\}$$

$$\Delta \nu_{y} = \frac{10^{-4}G_{0}}{B_{0}\rho R_{0}^{n-1}} \oint \frac{\beta_{y}ds}{2\pi} \left\{ -C_{1} + 3C_{2}\beta_{y}J_{y} - 6C_{2}\beta_{x}J_{x} - \frac{15}{2}C_{3}\beta_{y}^{2}J_{y}^{2} + 45C_{3}\beta_{x}\beta_{y}J_{x}J_{y} - \frac{45}{2}C_{3}\beta_{x}^{2}J_{x}^{2} \right\}$$
(7)

where the integrals are performed along the ring, and

$$C_{1} = -\frac{1}{2}b_{1}\delta + b_{2}\Delta_{x} - a_{2}\Delta_{y} + \frac{3}{2}(b_{3}\Delta_{x}^{2} - a_{3}\Delta_{y}^{2})$$

$$C_{2} = \frac{1}{4}b_{3} + b_{4}\Delta_{x} - a_{4}\Delta_{y}$$

$$C_{3} = \frac{1}{6}b_{5} + b_{6}\Delta_{x} - a_{6}\Delta_{y}.$$
(8)

Here, $\Delta_x = D_x \delta + x_c$, $\Delta_y = D_y \delta + y_c$, D_x and D_y are the dispersions, δ is the fractional momentum deviation, and x_c and y_c are the closed-orbit displacement from the magnet center. Because β_x and β_y achieve their maximum values at different location, it can be verified that the major effect of the *n*th multipole on particles of constant total action $J_x + J_y$ is from the two leading terms proportional to $J_x^{(n-1)/2}$ and $J_y^{(n-1)/2}$, respectively. Therefore, the tune spread due to one pair of triplets can be minimized when the quantities

$$K_{nxIR} = K_{nxFDF} + K_{nxDFD} \quad \text{and} \quad K_{nyIR} = K_{nyFDF} + K_{nyDFD} \tag{9}$$

are minimized over each IR.

3. Body-Ends Compensation of b_5 Multipole

The systematic multipole b_5 in the lead and return ends of the triplet quadrupole can be compensated by the systematic b_5 in the quadrupole body. The compensation is based on the following three principles. Firstly, both the tune shift over the triplet pair near each IP and the local kicks in each triplet should be minimized. Secondly, the net amount of body b_5 should be made as small as possible in order not to "introduce" undesired errors when the compensation is made imperfect by the lattice deviation from the ideal design. Furthermore, the choice of b_5 should be technically simple and flexible for the magnet manufacturing.

The analysis on the triplet multipole compensation is based on the simulation study of the so called "ideal" lattice where both misalignment errors and magnetic errors are excluded. β^* is equal to 1 meter at six and eight o'clock interaction points (IP), and is equal to 10 meter at the rest four IP's. The sextupole magnets are adjusted so that both horizontal and vertical chromaticities are equal to 2. Tables 3a and 3b list the lattice functions at positions where the DFD and FDF triplets are located, respectively. As shown in Figure , the lead ends of Q3 are towards IP, while the lead ends of Q1 and Q2 are away from IP. This arrangement of lead-end locations makes the errors from the lead ends relatively less important (as shown by the relative coefficients in Eq. 14).

3.1. Compensation scheme

The best way to compensate for b_5 in the lead and return ends is to adjust the amount of requested body b_5 , identically in all triplet quadrupoles, to minimize the quantities K_{5xIR} and K_{5yIR} in Eq. 9 of each IR. Notice that among the triplet pair near each IP, both the kicks and tune shifts are mainly produced by the F quadrupoles where the amplitude function $\beta_{x,y}$ reaches its maximum either Q2 in the DFD or Q3 in the FDF triplet. Therefore, the body b_5 of these F quadrupole must be of the opposite sign of that of their ends. For engineering convenience, we assume that the body b_5 is the same for all the magnets Q1, Q2, and Q3. Due to the optical anti-symmetry of the x and y plane over DFD and FDF triplet,

$$K_{5x\text{DFD}} \approx -K_{5y\text{FDF}}, \text{ and } K_{5y\text{DFD}} \approx -K_{5x\text{FDF}},$$
 (10)

the condition for the quantities of Eq. 9 to be equal to zero is

$$D_{\rm FDF} + D_{\rm DFD} + b_5 L_{eff} = 0 \tag{11}$$

	Q1	Q2	Q3
G(FDF) (T/m)	48.4	-47.0	47.3
G(DFD) (T/m)	-48.4	47.0	-47.3

Table 2: Gradients of triplet quadrupoles at storage.

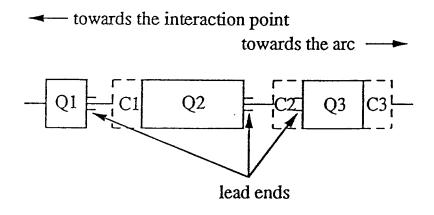


Figure 1: Schematic layout of the RHIC triplet, showing the quadrupoles, the orientation of the quadrupole lead ends, and the local correctors C1, C2, and C3.

where the drive D comes from both the lead (L) and the return (R) ends

$$D = \frac{B_{5L}}{G_0} \sum_{i=1}^3 G_i \beta_{xi}^3 \bigg|_L + \frac{B_{5R}}{G_0} \sum_{i=1}^3 G_i \beta_{xi}^3 \bigg|_R,$$
(12)

the subscripts i = 1, 2, 3 represent the quadrupoles Q1, Q2, and Q3, and the effective length is defined as

$$L_{eff} = \frac{1}{G_0} \sum_{i=1}^3 \int G_i \beta_{xi}^3 ds \bigg|_{\text{FDF}} + \frac{1}{G_0} \sum_{i=1}^3 \int G_i \beta_{xi}^3 ds \bigg|_{\text{DFD}}.$$
 (13)

Using the lattice function from Table 3, the desired b_5 in the body is obtained as

$$b_5 = -0.17 \ B_{5L} - 0.35 \ B_{5R} = -1.2 \ \text{(unit)}.$$
 (14)

On the other hand, if the local kicks are to be minimized to zero, the required b_5 in the body becomes, respectively,

$$b_{5} = \begin{cases} -0.31 \ B_{5L} - 0.59 \ B_{5R} = -2.0 \text{ (unit)} & \text{for } K_{5x} = 0 \text{ in FDF or } K_{5y} = 0 \text{ in DFD} \\ -0.078 \ B_{5L} - 0.19 \ B_{5R} = -0.54 \text{ (unit)} & \text{for } K_{5y} = 0 \text{ in FDF or } K_{5x} = 0 \text{ in DFD} \\ (15) \end{cases}$$

The desired b_5 value given by Eq. 14 is, by chance, about the average of the values in Eq. 15.

Figure 2 shows the tune footprint for on-momentum particles produced by the b_5 multipole error at the lead and return ends of one pair of triplet (6 o'clock). The mesh of points represents a spectrum of particles launched with initial amplitudes between 0 to 5σ in each plane individually, or along several contours of constant total action $(J_x + J_y)$ where the ratio (J_x/J_y) of horizontal and vertical action is smoothly varied. The normalized 95% emittance is assumed to be 40π mm·mr. The energy of the particle is 100 GeV/u ($\gamma = 107$). Figure 3 shows the similar diagram when the body b_5 is set to be equal to -1.2 unit. The correction in tune spread is obviously satisfactory.

3.2. Comparison with alternative schemes

Several alternative schemes have been explored to determine the optimum compensation method. Table tab:4 lists the possible 9 schemes denoted A1 through A9. The one discussed in Section 3.1 is denoted A7. In Table 1, the notation Q, T, and IR indicates that the

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3a: lattice parameters near DFD triplet:

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e 1	ement seque	ance i		:	hori	zont	a 1		1				tica		-	
#.	name	dist i [m] i		alfax	nux [2pi]	x(co) [mm]	x' (co) [mrad]		dx'i i		alfay	nuy [2p1]	y(co) [mm]	y' (co) [mrad]	[m]	đy'
 1	mcr	0.000	0.976	0.010	0.000	0.000	0.000	0.005	0.028		-0.009	0.000	0.000	0.000	0.000	0.000
	bpmv	8.974	83.317	-9.185	0.234	0.000	0.000	0.254	0.028	82.517		0.231	0.000	0.000	0.000	0.000
3	bpmh	8.974	83.317	-9.185	0.234	0.000	0.000	0.254	0.028	82.517		0.231	0.000	0.000	0.000	0.000
4	exxbo6	9.800	99.190-	10.031	0.236	0.000	0.000	0.276	0.028	98.201		0.233	0.000	0.000	0.000	0.000
5	dx bo6	11.650	139.829-	11.920	0.238	0.000	0.000	0.328	0.018	138.334-		0.235	0.000	0.000	0.000	0.000
6	eaxbo6	13.500	187.401-	13.814	0.240	0.000	0.000	0.344	0.009	185.384-		0.237	0.000	0.000	0.000	0.000
7	d0bp6	22.302	510.157-	22.828	0.245	0.000	0.000	0.421	0.016	503.421-		0.242	0.000	0.000	0.000	0.000
8	bpmv	25.069	644.201-		0.245	0.000	0.000	0.488	0.024	635.674-		0.242	0.000	0.000	0.000	
9	bpmh	25.069	644.201-		0.245	0.000	0.000	0.488	0.024	635.674-		0.242	0.000	0.000	0.000	0.000
10	ex1bo6	25.361	659.262-		0.245	0.000	0.000	0.495	0.024	650.531-		0.242	0.000	0.000	0.000	0.000
11	g106	25.433	663.003-	29.457	0.245	0.000	0.000	0.496	0.027	654.220-		0.242	0.000	0.000	0.000	0.000
12	q106	25.625	675.697-	36.726	0.245	0.000	0.000	0.502	0.032	661.482-		0.243	0.000	0.000	0.000	0.000
13	q106	25.817	691.236-		0.246	0.000	0.000	0.509	0.037	666.134		0.243	0.000	0.000	0.000	0.000
14	g1 06	26.009	709.744-		0.246	0.000	0.000	0.516	0.042	668.137		0.243		0.000	0.000	0.00
15	q106	26.153	725.932-		0.246	0.000	0.000	0.523	0.048	667.641		0.243	0.000	0.000	0.000	0.000
16	q106	26.345	750.743-		0.246	0.000	0.000	0.532	0.053	664.320		0.243	0.000	0.000	0.000	0.00
17	q106	26.537	779.020-		0.246	0.000	0.000	0.543	0.059	658.366		0.243		0.000	0.000	0.00
18	q1 06	26.729	810.987-		0.246	0.000	0.000	0.555	0.064	649.826		0.243	0.000	0.000	0.000	0.00
19	ealbo6	26.801	824.364-		0.246	0.000	0.000	0.560	0.067	645.668		0.243	0.000	0.000	0.000	0.00
20	kickh		1059.700*		0.246		0.000	0.640	0.067	579.301		0.243	0.000	0.000	0.000	0.00
21	ml2bo6		1059.700*		0.246	0.000	0.000	0.640	0.067	579.301		0.243	0.000	0.000	0.000	0.00
22	ex2bo6		1165.877*		0.246		0.000	0.673	0.067	552.853		0.243		0.000	0.000	0.00
23	g206		1203.897-		0.246		0.000	0.684	0.059	543.822		0.243	0.000	0.000	0.000	0.00
24	g206	29.097	1281.303-	71.444	0.246		0.000	0.707	0.043	531.653		0.243	0.000	0.000	0.000	0.00
25	g206		1332.750-		0.246		0.000	0.723	0.026	531.035		0.244	0.000	0.000	0.000	0.00
26	g206		1356.021		0.246		0.000	0.730		541.942		0.244	0.000	0.000	0.000	0.00
27	g206	30.343	1351.591	22.607	0.246		0.000		-0.009	559.075		0.244	0.000		- 0.000	0.00
28	g206		1316.727		0.246		0.000		-0.026	594.723		0.244	0.000	0.000	0.000	0.00
29	g206		1254.411		0.246		0.000		-0.043	644.777		0.244	0.000	0.000	0.000	0.00
30) q206		1167.3251		0.246		0.000		-0.060	711.406		0.244	0.000	0.000	0.000	0.00
31	ea2bo6		1126.1723		0.246		0.000		-0.068	743.113		0.244		0.000	0.000	0.00
32	ml3xbo6	33.132	844.4651		0.247		0.000		-0.068	999.359		0.244	0.000	0.000	0.000	0.00
33	sq3xbo6	33.132	844.4651		0.247		0.000		-0.068			0.244		0.000	0.000	0.00
34	ex3bo6	33.730	724.762		0.247		0.000			1134.440		0.244		0.000	0.000	0.00
	5 q306	33.835	704.695		0.247		0.000			1159.033		0.245		0.000	0.000	0.00
36	5 q306	34.115	658.184		0.247		0.000			1216.058				0.000	0.000	0.00
37	/ q3o6	34.395	618.530		0.247		0.000			1264.172		0.245		0.000	0.000	0.00
38	g3o6	34.675	585.076		0.247		0.000			1302.578		0.245		0.000	0.000	0.00
39	9 q3o6	34.885	564.156		0.247		0.000			1323.597		0.245			0.000	0.00
40) g3o6	35.165	541.420		0.247		0.000			1340.837		0.245		0.000	0.000	0.00
41	L q306	35.445	523.549		0.247		0.000			1347.044					0.000	0.00
	g306	35.725	510.246		0.247		0.000			1342.114		0.245		0.000	0.000	0.00
	ea3bo6	35.830			0.247		0.000			1336.109		0.245		0.000	0.000	0.00
	kickv	36.320			0.247		0.000			1308.262					0.000	0.00
4 5	5 m13abo6	36.320	491.312	15.760	0.247	0.000	0.000	0.460	-0.010	1308.262	28.264	0.245				
41	5 bpmv	37.608	451.577	15.106	0.248	0.000	0.000	0.448	-0.010	1236.504	27.477	0.245	0.000		0.000	0.00
	7 bpmh	37.608			0.248		0.000			1236.504		0.245			0.000	0.00
	B bpmv	73.200		-2.959	0.686		0.000	0.108	-0.010	55.075	5.716	0.267			0.000	0.00
	9 bpmh	73.200		-2.959	0.686		0.000	0.108	-0.010	55.075	5.716	0.267			0.000	0.00
	0 q4ot6	73.500		-3.040	0.688		0.000		-0.010		5.358	0.268	0.000	0.000	0.000	0.00

3b: lattice parameters near FDF triplet

.

					hori				i				tica			
8.		quence 1 dist i [m] i	betax [m]	alfax	nux [2pi]	x(co) [mm]	x'(co) [mrad]		dx' 1 1	betay [m]	alfay	nuy [2pi]	(со) [mm]	y' (co) [mrād]		đy'
								-0.277	-0.012	20.701	2.987	28.493	0.000	0.000	0.000	0.00
2615 q4		3760.528			27.923	0.000		-0.281		18.912	2.907	28.496	0.000	0.000	0.000	0.00
616 br	van	3760.828		-5.794	27.924	0.000		-0.281		18.912		28.496	0.000	0.000	0.000	0.00
2617 br		3760.828		-5.794	27.924	0.000		-0.738		445.120		28.932	0.000	0.000	0.000	0.00
2618 br	pmv	3796.421	1254.563	-27.889	27.945	0.000		-0.738		445.120		28.932	0.000	0.000	0.000	0.00
2619 br		3796.421			27.945	0.000		-0.755		484.264		28.933	0.000	0.000	0.000	0.00
2620 ki		3797.708			27.945	0.000		-0.755		484.264		28.933	0.000	0.000	0.000	0.00
2621 ml		3797.708			27.945	0.000		-0.755		499.600		28.933	0.000	0.000	0.000	0.00
2622 88		3798.198			27.945	0.000				502.917		28.933	0.000	0.000	0.000	0.00
2623 Q		3798.303	1361.757	-18.995	27.945	0.000		-0.762	0.004	516.024		28,933	0.000	0.000	0.000	0.00
2624 0		3798.583	1366.764	1.149	27.945	0.000		-0.763	0.004	533.634		28.933	0.000	0.000	0.000	0.00
2625 q		3798.863	1360.472	21.275	27.945	0.000		-0.760		556.039		28.933	0.000	0.000	0.000	0.00
2626 q		3799.143	1342.986	41.048	27.945	0.000		-0.754	0.026		-53.792	28.933	0.000	0.000	0.000	0.00
2627 q		3799.353	1321.663	60.331	27.946	0.000		-0.747	0.038		-64.194	28.933	0.000	0.000	0.000	0.00
2628 q		3799.633	1282.700	78.534	27.946			-0.735	0.049		-75.660	28.933	0.000	0.000	0.000	0.00
2629 q		3799.913	1233.887	95.438	27.946			-0.720	0.059		-88.379	28.933	0.000	0.000	0.000	0.00
2630 Q		3800.193	1176.031	110.764	27.946			-0.702			-94.833	28,933	0.000	0.000	0.000	0.00
2631 e		3800.298	1151.080	118.179	27.946	0.000		-0.694			******	28.934		0.000	0.000	0.0
2632 m			1014.030	110.921	27.946	0.000		-0.649	0.075		******	28.934	0.000	0.000	0.000	0.04
2633 B			1014.030	110.921	27.946	0.000		-0.649	0.075	832.278	*******	28.934		0.000	0.000	0.0
2634 e		3802.155	754.044	95.649	27.946	0.000		-0.555		1109.896	*******	28.934		0.000	0.000	0.0
2635 Q		3802.325		84.989	27.946	0.000		-0.542		1150.453		28.934		0.000	0.000	0.0
		3802.778		64.934		0.000		-0.514		1236.272		28.934		0.000	0.000	0.0
2636 q		3803.232		47.691		0.000		-0.491		1297.680	-53.090	28.934		0.000	0.000	0.0
2637 q 2638 q		3803.685		32.514		0.000		-0.474		1332.032	-22.2/2	28.934			0.000	0.0
		3804.025		18.809		0.000		-0.465		1336.393		28.934		0.000	0.000	0.0
2639 g		3804.478		5.717		0.000	0.000	-0.458	0.010	1313.451	L 40.837	28.934			0.000	0.0
2640 q		3804.932		5 -7.128		0.000	0.000	-0.456	-0.001	1262.741	L 70.417	-			0.000	0.0
2641 q		3805.385	551 884	-20.281	27.947	0.000	0.000	-0.458	-0.011	1186.450	96.964	28.934			0.000	
2642 q				2-27.077		0.000	0.000	-0.461	0.017	1148.978	3109.326	28.934				
2643 e		3805.555	501.002	3-27.718			0.000	-0.470	-0.017	1044.333	3104.228	28.934				
2644 k		3806.045		3-27.718		-	0.000	-0.470	-0.017	1044.333	3104.228	28.934				
2645 m		3806.045		1-29.265			0.000	-0.490	-0.017		3 91.927	28.935				
2646 e				2-25.933					-0.014	799.21	0 87.026	28.935				
2647 q		3807.299		3-19.183			0.000	-0.493	-0.009		3 77.234	28.935				
2648 q		3807.491		0-12.279					-0.004	739.83	5 68.060	28.935				
2649 9		3807.683		4 -5.278				0.49		715.38	1 59.429	28.93				
2650 q	1116	3807.875						0.494			6 51.453	28.935				
2651 q		3808.019		0 1.76				0 -0.49		681.18	4 43.652					
2652 9		3808.211		1 8.792				0 -0.49		665.86	8 36.199					
2653 0		3808.403		5 15.750		-		0 -0.48		. 653.35	5 29.036					
2654 0	g116	3808.595		8 22.58				0 -0.48		649.66	8 25.569	28.93				
2655 •	ex1b16			4 25.95				0 -0.47			2 25.274	28.93				
2656 1	bpmv	3808.959		2 25.65	-			0 -0.47			2 25.274	28.93				
2657 3	bomh	3808.959		2 25.65				0 -0.41			2 22.486		6 0.000			
2658	d0bm6	3811.727		1 22.84				0 -0.33	-		4 13.624		0 0.000	0.000	0.000	0.0
2659	eaxbi	3820.528	187.92	4 13.83	4 27.95								2 0.000	0.000	0.000) 0.1
2660	arhif	3822.378	140.28	1 11.94	27.95			0 -0.31			7 11.763					
2660 0				9 10.05		7 0.000		0 -0.26								
2661		3825.054						0 -0.24								
						9 0.000		0 -0.24	3 0.02	3 62.21	2 9.059	28.94	n u.uuu	,	,	

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correction is applied by minimizing the undesired effect in each quadrupole, triplet, and IR, respectively.

In scheme A1 and A2, each quadrupole magnet is compensated independently. The fact that the weight in A1 is equal to 1 indicates that the integrated b_5 over each quadrupole is made to be zero. These methods result in a relatively large b_5 in the body of each magnet, which is against the second principle for b_5 compensation.

Because of the large variation of β_x and β_y over the quadrupole body, the minimization of the kicks and tune spreads is not good when the weight is taken to be 1. The desired values of b_5 body are also different when β_x^3 and β_y^3 are used as weight. The optimum schemes are found when both the triplet in each IR are taken into account (A7, A8, and A9). In scheme A8, the amount of desired b_5 is large. In scheme A9, the sign of the body b_5 is allowed to vary for different magnet. Obviously, the amount of body b_5 can be made smaller if the effective length L_{eff} is made longer. In this case, the amount of b_5 required for tune-spread minimization is

$$|b_5| = |-0.13 \ B_{5L} - 0.26 \ B_{5R}| = 0.9 \ \text{(unit)}$$
(16)

which is about 75% of the amount given by the original method (Eq. 16). However, the complication caused by the sign flipping makes this method less attractive (against the third principle for b_5 compensation). Therefore, the scheme one should adopt is A7, as discussed in Section 3.1.

4. Tuning Shimming

Tuning shims have been used to make the integrated multipoles from order A_2 to A_5 , and from order B_2 to B_4 to be equal to zero[2] in each triplet quadrupole. On the other hand, due to the large value of b_5 in the triplet quadrupole ends, the available range of shim (about ± 3.2 mm in thickness) is not adequate for compensation.

The body-ends compensation on b_5 multipole allows for the tuning shims to be used only for the correction of random b_5 errors in each magnet. According to the correction scheme A7, the total b_5 in the body after shimming should be equal to -1.2 unit. The available range of shimming is adequate for the correction of the relatively small value of random b_5 , as shown in Table 1. Even if the systematic body b_5 of the Q1 quadrupoles first constructed on site is not equal to the desired value of -1.2, the tuning shims will still only respond to the random b_5 values around the new systematic mean. In this case, the requested systematic b_5 body will be slightly modified for Q2 and Q3 production.

5. Local Correction

As shown in Figure , there exists three multipole corrector packages C1, C2, and C3 in each triplet for local correction. Among the correctors $(a_1, b_2, and a_5)$ in the middle C2 package, only a_1 correctors are currently planned to be powered. Since the betatron phase advance from dipole D0 to triplet quadrupoles Q1, q2, and Q3 is very small (Table 3), the strength of the a_1 corrector at each C2 may be set to compensate for the a_1 on these elements using the relation

$$\sqrt{\beta_x \beta_y} a_1 L \Big|_{C2} = \int_{\text{D0,trip}} \sqrt{\beta_x \beta_y} a_1 ds, \qquad (17)$$

where L is the length of the corrector, and the integral extends over D0, Q1, Q2, and Q3.

The C1 and C3 packages consisting of b_3 , b_4 , and b_5 correctors are used to correct the residual b_3 , b_4 , and b_5 after the manufacture (with body-ends compensation and tuning shimming) and installation of the D0 and triplet magnets. The location of C1 and C3 are chosen such that the horizontal and vertical β functions are large at different correctors (i.e. β functions orthogonal at two locations). The strengths of the two correctors are adjusted according to the measurement of the multipole errors of triplet quadrupoles and D0 and the lattice functions such that the total kicks K_{nx} and K_{ny} (n=3,4,5) in both x and y planes from the triplet and D0 are independently adjusted to zero for each triplet and D0. The maximum amount of b_5 achievable in each corrector of 0.5 meter length with 50 Amp power supply corresponds to about 20 units b_5 (normalized to $G_0 = 47$ T/m). If body-ends compensation and shimming are performed within reasonable accuracy, the corrector strength is adequately for the compensation of residual b_5 errors.

6. Conclusions and Discussion

In this note, we have discussed the compensation of the allowed magnetic multipole b_5 in the IR triplet magnet where the amplitude of the transverse particle oscillation is the largest. From the experience gained so far with the on-site production of Q1 magnets of series number less than 8, the amount of b_5 in the body is requested to be -1.2 unit in order to compensate for the effects caused by the strong b_5 at the lead and return ends. If the actual value of b_5 in Q1 magnets differs significantly from its desired value of -1.2, further fine tuning might be requested in the later production runs of Q3 and Q2. This allows for the tuning shims to be used only for the correction of random errors in each magnet. Consequently, the tuning shim magnetic non-linear effects and the the "feed-up" effects (coupling desired body b_5 changes to undesired body b_9 changes) become less important.

Compared with the b_5 compensation, the systematic body compensation for b_9 from the ends is less effective partly due to the strong dependence of the b_9 kicks on the variation of the oscillation amplitude. Previous studies indicate that b_9 in Q2 and Q3 magnet ends should be made less than 0.3 unit-m for proper beam storage. The requested b_9 in the magnet body is thus zero.

Acknowledgements

We would like to thank R.Gupta and S.Tepikian for many helpful discussions.

References

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Method	Correction	Weight	Sign	Polarity	b5(Body)	b5(Body)	b5(Body)
	Unit	_	flip?		Q1	$\mathbf{Q2}$	Q3
A1	Q	1	-	-	-3.9	-1.7	-2.7
A2	Q	eta_x^3	-	F/D	-3.6/-5.1	-1.1/-3.0	-2.0/-4.3
A3	T	1	no	_	-40.0	-40.0	-40.0
A4	Т	1	yes	-	-0.8	0.8	-0.8
A5	Т	eta_x^3	no	FDF/DFD	-2.0/-0.5	-2.0/-0.5	-2.0/-0.5
A6	Т	$eta_x^{ ilde{3}}$	yes	FDF/DFD	-1.5/0.4	1.5/-0.4	-1.5/ 0.4
A7	IR	β_x^3 and β_y^3	no	\mathbf{both}	-1.2	-1.2	-1.2
A8	IR	β_x^3 and β_y^3	yes	both	5.2	-5.2	5.2
A9	IR	$eta_x^{ ilde{3}} ext{ and } eta_y^{ ilde{3}}$	yes	FDF/DFD	-0.9/0.9	0.9/-0.9	-0.9/0.9

Table 4: Possible body-ends compensation schemes for the b_5 multipole in the triplet quadrupoles.

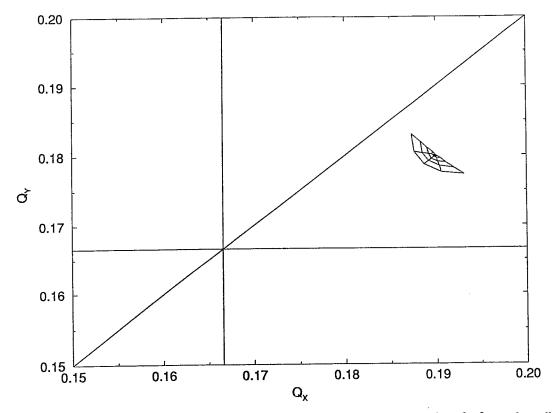


Figure 2: Tune shift of on-momentum particles with betatron amplitude from 0 to 5 σ with the 1 meter β^* storage lattice produced by one pair of triplet with lead end error $B_5 = 4.6$ unit m and return end error $B_5 = 1.0$ unit m. The horizontal and vertical integer tunes are 28 and 29, respectively.

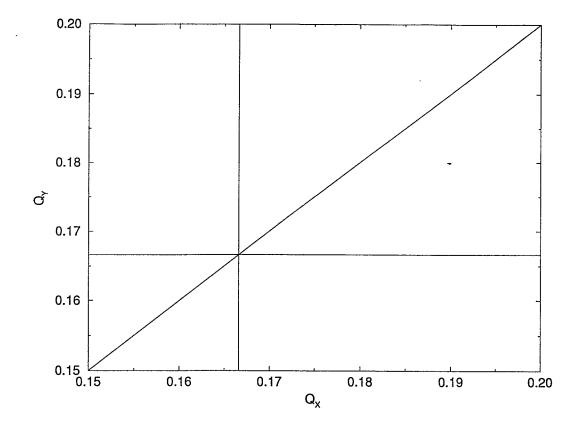


Figure 3: Similar to Figure 2, with $b_5 = -1.2$ unit in the body for compensation.