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Modeling and Simulation of the Power Amplifier for the RHIC 28 MHz Accelerating Cavity

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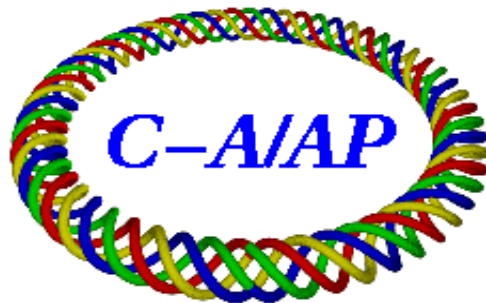
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MODELING AND SIMULATION OF THE POWER AMPLIFIER FOR THE RHIC 28 MHZ ACCELERATING CAVITY

Sanbao Zheng and John Keane

Abstract-A detailed model for 4cw150000 Tetrode is developed. This model is implemented with PSPICE and verified by design curves from the manufacturer. A power amplifier using this Tetrode is designed and simulation results agree with the design expectations. A simulation model of the RHIC 28 MHz PA system is developed and simulation results are presented. Possible improvement of the PA is explored.

1 Introduction

28 mHz RF Power Amplifiers (PA) are used in the RHIC for particle accelerating. The most complete record available on this PA is an overall description given in [1]. To set a foundation for the maintenance and future improvement of the PA, many details need to be clarified and a detailed computer model for the unit is desired. For this purpose, a model for the Tetrode used in this PA has been developed in this note. The simulation model for the PA unit is built with PSPICE and simulation results are presented and analyzed.

2 Tetrode Model

2.1 Modeling of the Tube

A Tetrode model modified from [2] is given below:

$$i_{sp} = \begin{cases} K(\mu_g v_g + \mu_s v_s + v_p)^x, & \text{if } \mu_g v_g + \mu_s v_s + v_p \geq 0 \\ 0, & \text{if } \mu_g v_g + \mu_s v_s + v_p < 0 \end{cases} \quad (1)$$
$$i_p = a i_{sp}$$
$$i_s = (1 - a) i_{sp}$$

where i_{sp} is the space current and a is the fraction of the space current flowing to the plate.

Coefficient a is a function of the voltages v_p and v_s , for which there is no specific formula reported yet. It was chosen to be a constant in [2]. This does not affect the accuracy of the model much as long as the plate voltage is always reasonably higher than the screen voltage. Since in high power PA the lower limit of the plate voltage is usually selected close to the screen voltage, it is desired to approximate the relation between a and tube voltages v_p and v_s with a specific equation. After fitting the design curves, the following equation is used in the modeling presented in this note:

$$a = A(1 - \exp(-\frac{v_p}{Bv_s})) \quad (2)$$

where ‘ A ’ and ‘ B ’ are constants. ‘ A ’ is usually close to 1 and B determines the range of the plate voltage that influences the plate current. The relation is selected such that ‘ a ’ approaches a constant ‘ A ’ when v_p goes much higher than v_s and ‘ a ’ drops down when v_p get closer to v_s . This agrees with the operational characteristic of a Tetrode.

Another consideration is that when the plate voltage is lower than the screen voltage, the plate current drops down drastically. When the plate voltage goes down to zero, there will be no plate current. To take into account this effect, ‘ a ’ is further modified to:

$$a = \begin{cases} A(1 - \exp(-\frac{v_p}{Bv_s})) & \text{when } v_p \geq v_s; \\ A \frac{v_p}{v_s} (1 - \exp(-\frac{v_p}{Bv_s})) & \text{when } v_p < v_s; \end{cases} \quad (3)$$

In [2], x is assumed to be 1.5 for all tubes. This constant turned out to be not satisfactory for the tube used in our PA. Therefore, it is taken as a parameter to be determined.

The parameters in the above model have been found for the tube 4cw150000 by fitting the model to the design curves from manufacturer. The fitting procedure is given in Appendix I, and the parameters found are:

$$x = 2.1, \mu_s = 147, \mu_g = 546, K = 3 \times 10^{-10}, A = 0.98, B = 0.5.$$

2.2 PSPICE Implementation

The model is implemented in PSPICE sub-circuit as shown in Fig. 1. Besides the two current sources described above, a diode and resistance branch is used to model the grid. Tube capacitances are added to the model. The procedure to find the capacitances from datasheet is given in Appendix II, and the SPICE code for the model implementation is given in Appendix III. A PSPICE symbol as shown in Fig.2 is created for the tube.

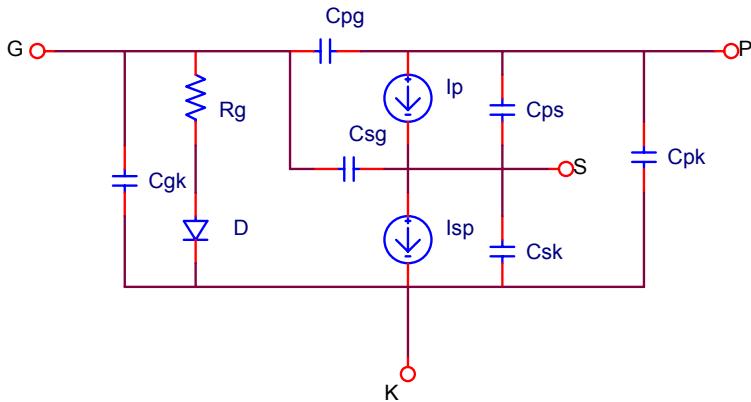


Fig. 1 PSPICE sub-circuit of the Tetrode model.

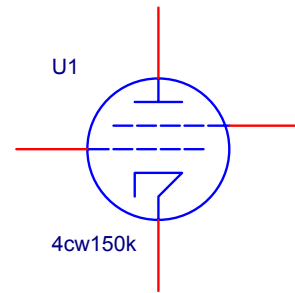


Fig. 2 PSPICE symbol for the Tetrode model

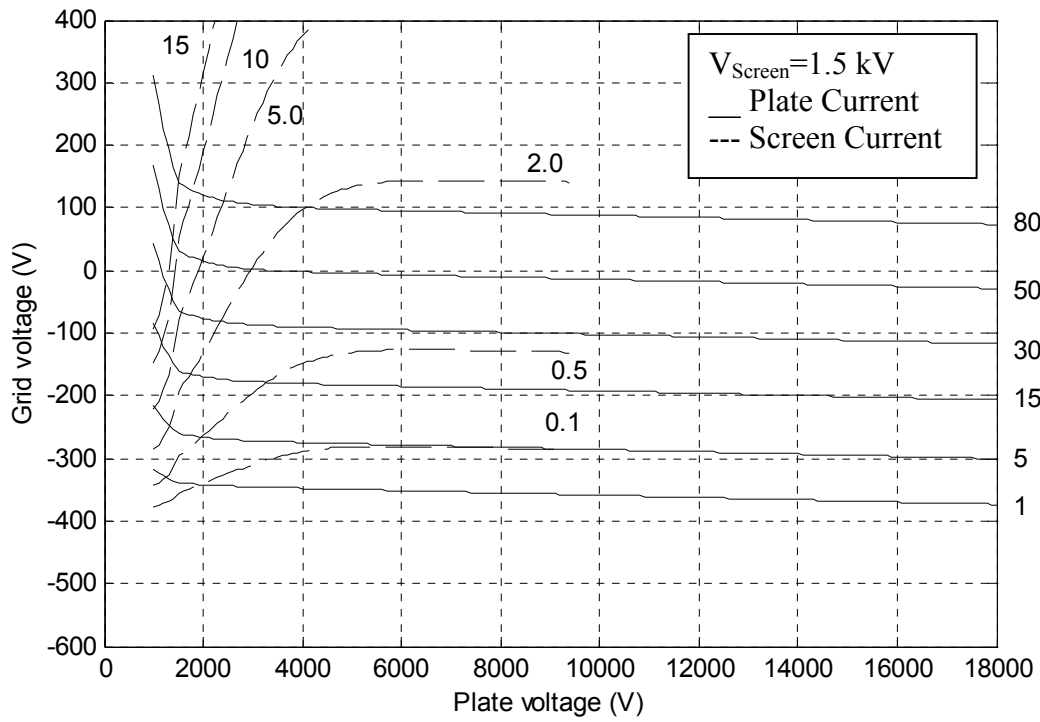


Fig. 3. Constant-current curves ($V_{\text{Screen}} = 1.5 \text{ kV}$) from the Tetrode model.

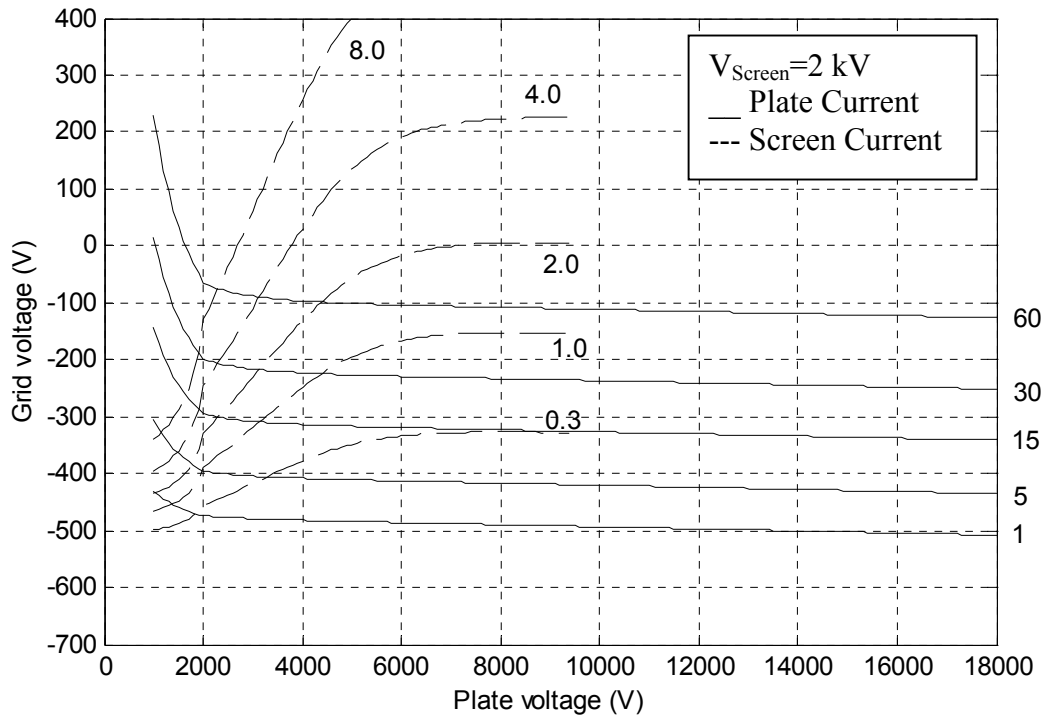


Fig. 4. Constant-current curves ($V_{\text{Screen}} = 2 \text{ kV}$) from the Tetrode model

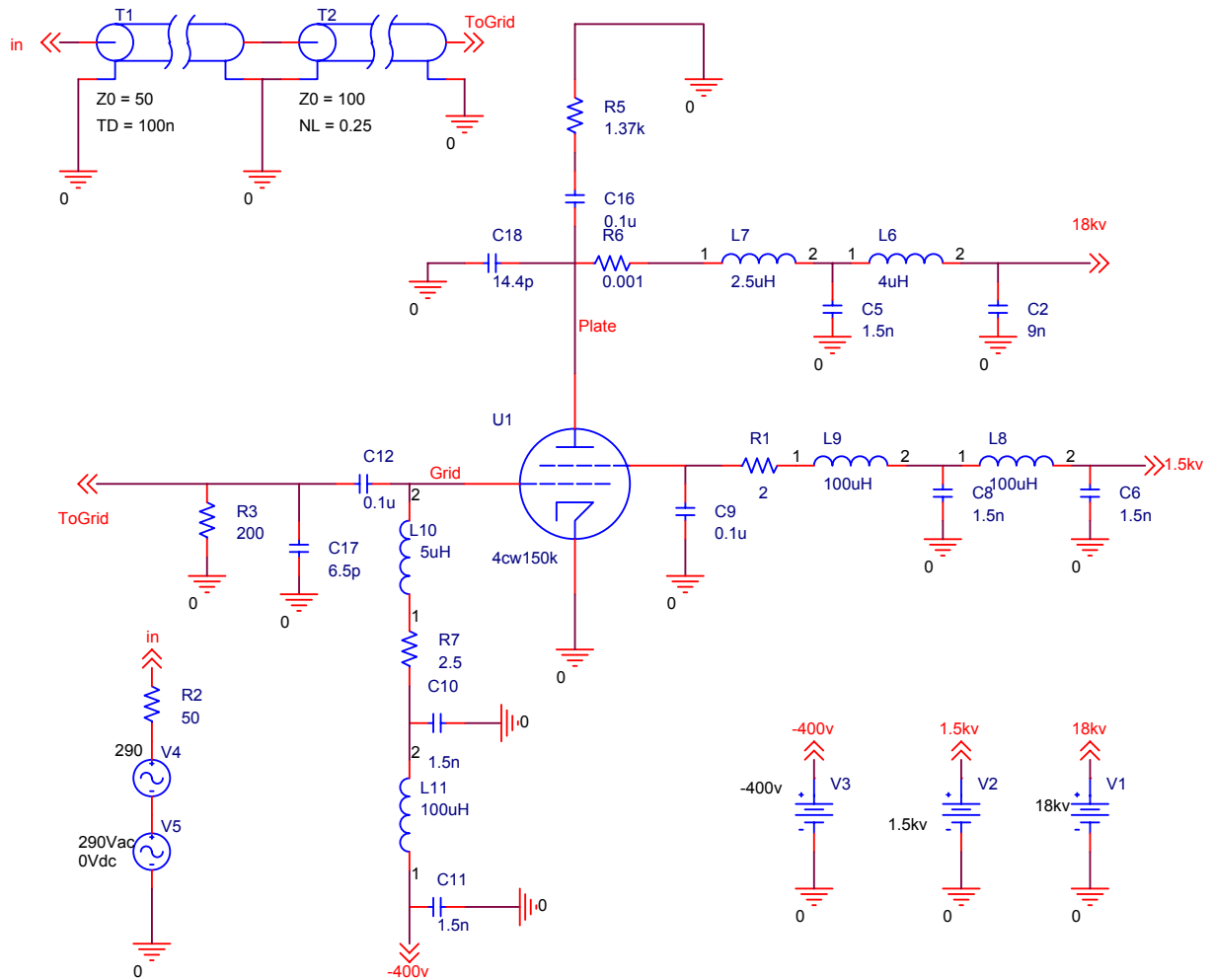


Fig. 5 PSPICE model used for the tube model verification

3 Model Verification

3.1 Verification by the Design Curves

A MATLAB program has been written to generate constant-current curves from the model developed in the previous section. The curves for 1.5 kV and 2 kV screen voltages are shown in Figs. 3-4. Comparison of these curves with those given by manufacturer shows a good agreement in a reasonable operating range of the tube.

3.2 Design of a PA Using 4cw15000 Tube

An 85 kw, grounded cathode, class B PA using 4cw150000 has been designed. The design procedure is given in Appendix IV. Table 1 gives the operating parameters expected by the design.

Table 1. Designed operating parameters of a PA

Plate bias V_{dc}	Plate dc current I_{dc}	Peak plate current I_{pk}	Output voltage V_{rf}	Output current I_{rf}	Output resistance R_o	Input voltage V_{in}	RF
18 kV	7.0 A	25.2 A	16 kV	11.7 A	1.37 k Ω	290 V	

3.3 Verification by the Design

A simulation model of a PA designed above is built in PSPICE, as shown in Fig. 5. Since the design has not considered the effects of the tube capacitances, they are removed from the tube in this simulation. The RF input is 290 volts and the dc bias are: $V_g=-400$ V, $V_s=1500$ V, $V_p=18$ kV. The bias voltages are connected to the tube through RF filters with parameters given in [1]. These filters change the grid and anode impedances. Capacitances are added in parallel to them to tune this effect out at resonant frequency. The transient analysis results, including plate current i_p , plate voltage v_p , screen current i_s , and plate supply current i_{dc} are shown in Fig. 6. It can be seen that the circuit is operating close to the design expectations listed in table 1.

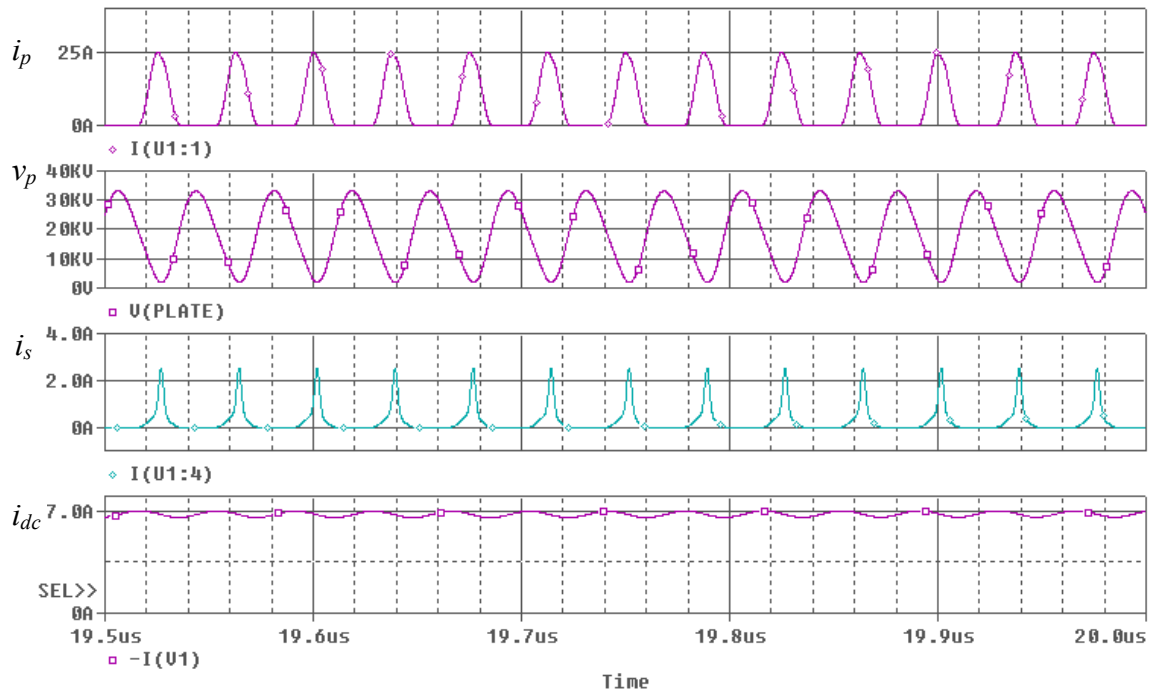


Fig. 6. Simulation results of the designed PA with a resistance load.

4 Simulation of the 28 MHz PA

4.1 PSPICE Model of the PA

A PSPICE model for the 28 MHz PA has been built as shown in Fig. 7. The tube model developed in Section 1 is used in this PA model. The tube capacitances C_{ps} and

C_{gp} are taken out from the tube and connected externally for convenience of current measurements. A resistor is added in parallel to each filter inductance to model the loss in the coil.

In Fig. 7, the cavity model and the neutralization circuit model are those given in [1]. The cavity model is comprised of a piece of transmission line, a coupling loop and an equivalent series resonant circuit for the cavity itself. The neutralization model consists of a short piece of transmission line, an inductance caused by the outer conductor of the transmission line, and a notch filter that intends to provide a short circuit at 28 MHz and a 50 Ω termination at other frequencies.

The load comprised of the cavity and the tube output capacitance (65 pf) has an impedance of about 1500 Ω at resonance. It was found that the RF filter in the anode blocking circuit reduces the load impedance at resonance to around 1200 Ω . If all other operating conditions keep unchanged, a small load impedance means a lower output voltage. To compensate this effect, a capacitor in parallel to the load may be added or a redesign of the filter might be necessary.

4.2 Simulation Results

The simulation in this section uses the same RF input and dc bias as those in Section 2.

AC sweep simulation results are shown in Fig. 8. It can be seen that at the resonant frequency, the load impedance is about 1.2 k Ω . The plate current, the plate voltage and the cavity voltage are a little smaller than expected. This is because the AC sweep is a linear analysis, and only the fundamental harmonic is analyzed. The high non-linear characteristic of the tube has not been considered. The hump on the plate current curve is caused by the parasitic capacitances of the tube.

If the AC sweep range is expanded a little beyond the cavity resonant frequency, a noticeable phenomenon comes into the picture as shown in Fig. 9: a resonance much bigger in magnitude exists at around 37 MHz. It is introduced by the coupling loop and was very possibly the cause for the trouble of oscillation which occurred before.

To see the detailed waveforms of the circuit, transient analysis of the circuit operating at the cavity resonance frequency has been performed. Fig. 10 shows the simulation results after the circuit reached its steady state. It's evident that the actual magnitude of the quantities are bigger than those obtained from ac sweep analysis. The last two curves in Fig. 10 show the current flowing through the feed-through capacitance C_{pg} of the tube, which can not be measured in real circuit, and the current flowing through the outer conductor of the short piece of cable used for neutralization. It is evident that these two current are equal in magnitude and in phase. This means the feedback current through C_{pg} is bypassed from the grid circuit by the neutralization cable and hence miller's effect is reduced.

The Fourier analysis results for the plate current, plate voltage, and cavity voltage are shown in Fig. 11, from which all the harmonics of the operational waveform can be seen.

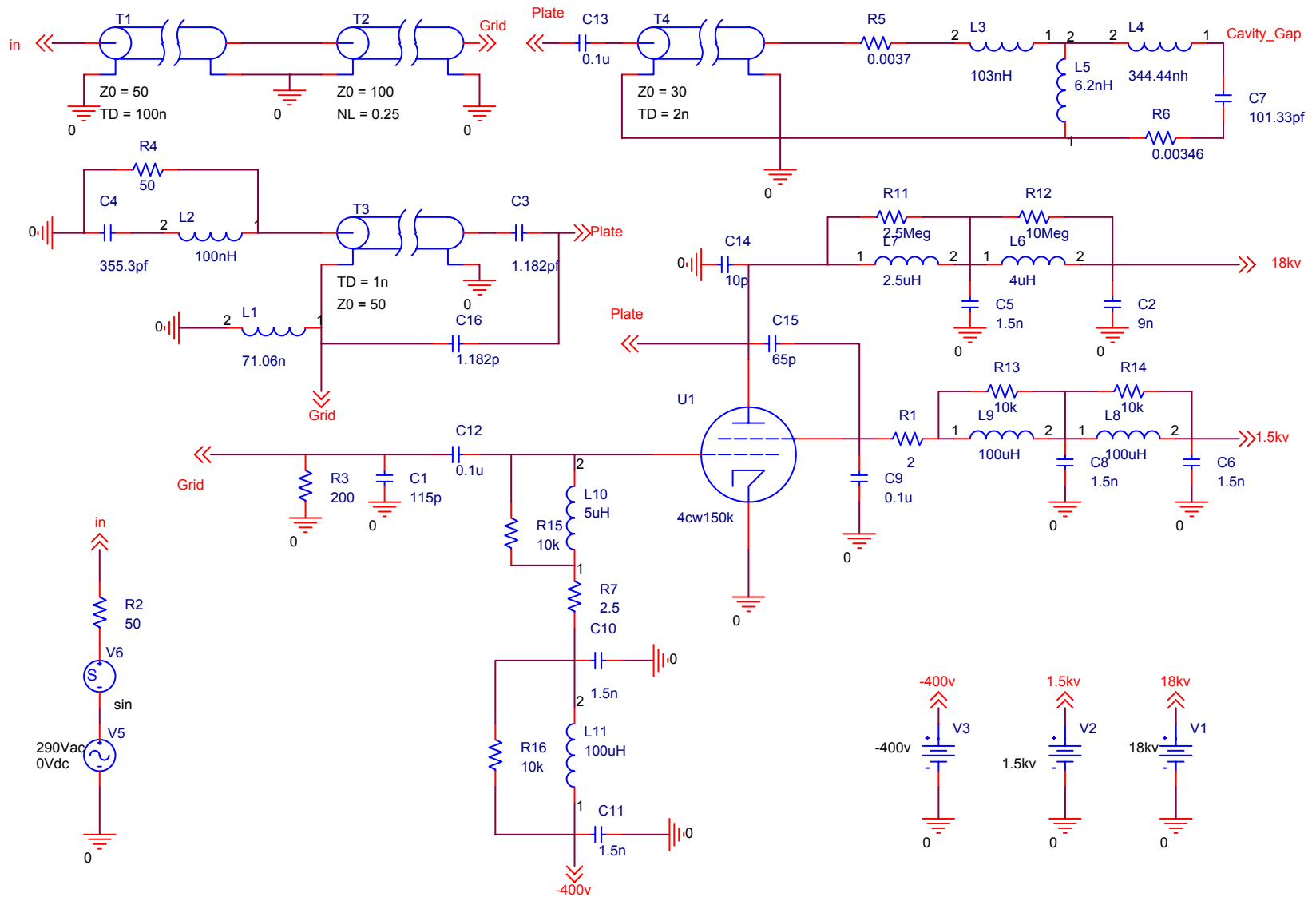


Fig. 7 A PSPICE model of the 28 MHz PA for the accelerating cavity.

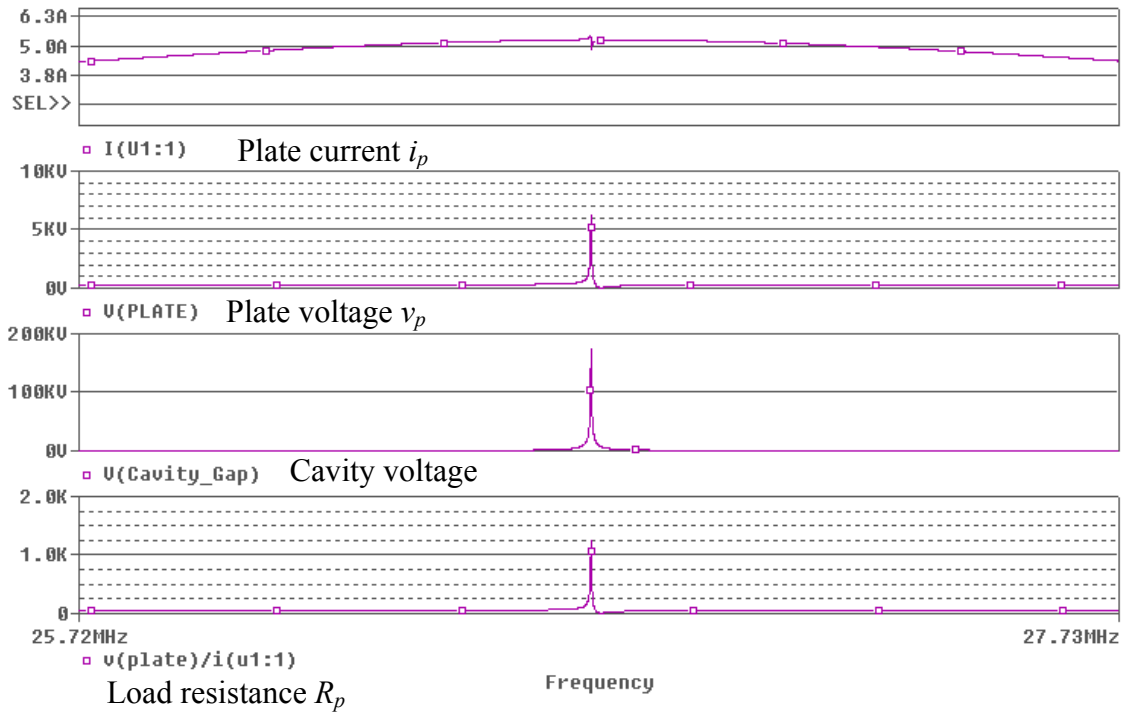


Fig.8 Frequency sweep results of the PA

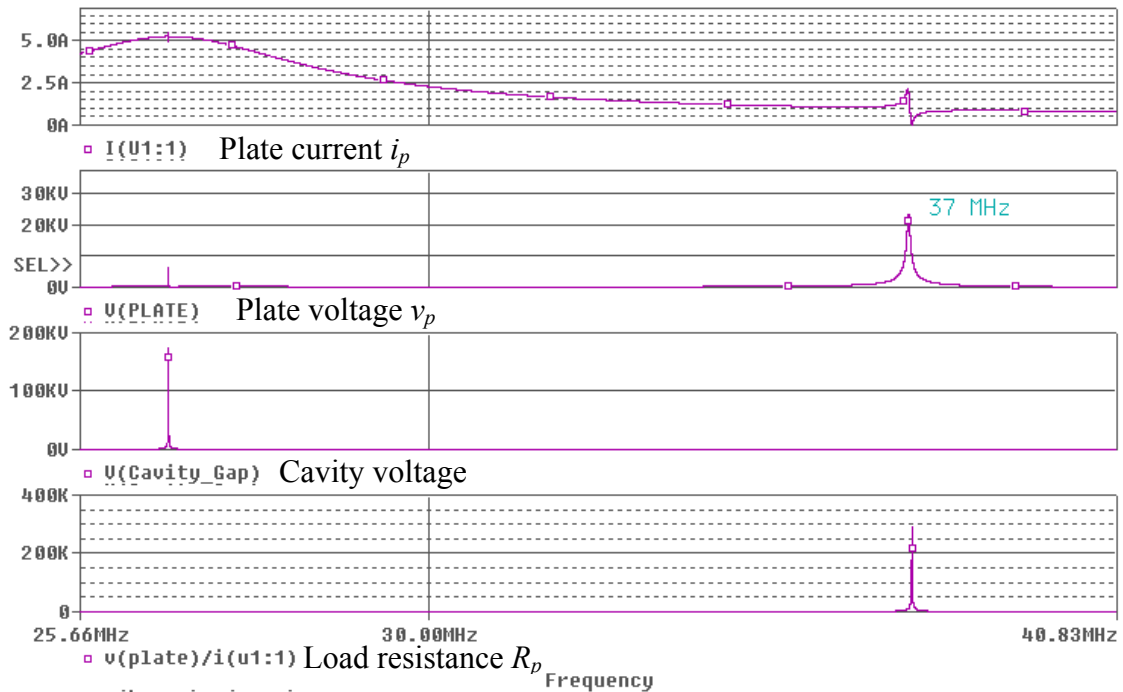


Fig. 9 Frequency sweep showing the high-Q resonance at the coupling loop frequency.

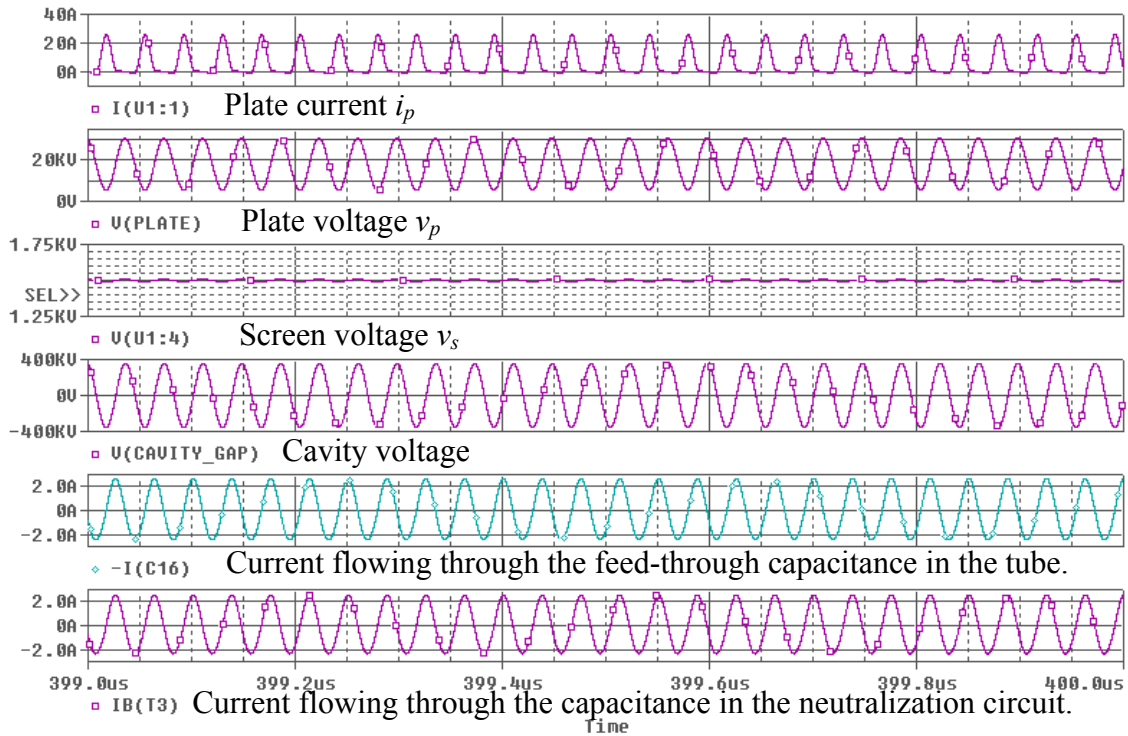


Fig. 10 Transient analysis of the PA

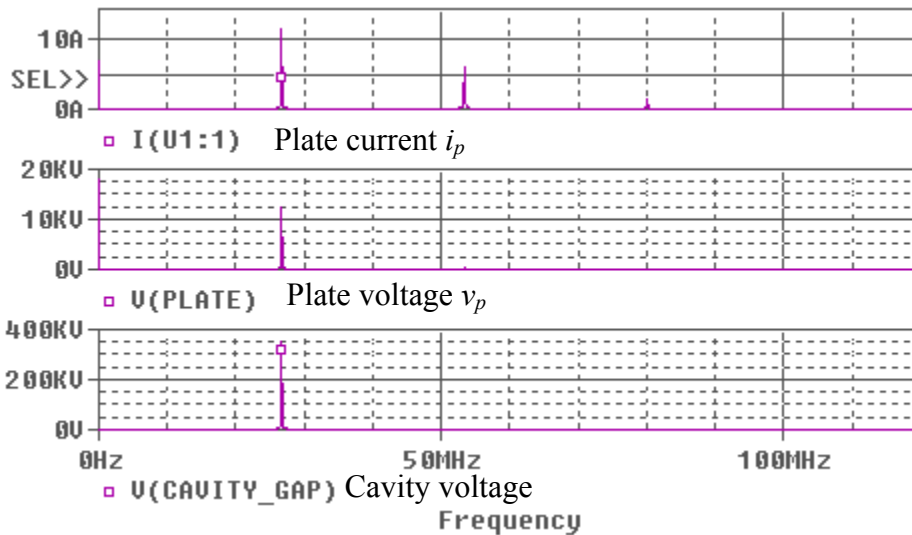


Fig. 11 Fourier analysis of the simulation results.

5 Conclusion

A PSPICE model for Tetrode 4CW150000 has been developed. The procedure of this model development can be used in other tubes. Simulation model for the 28 MHz accelerating PA has been built. A lot of information can be obtained from this PA model.

The plate dc blocking filter lowers down the impedance of the tube load at the operating frequency and hence decreases the output voltage. If a higher output voltage is

desired, the filter may need to be redesigned or a capacitor may be used for compensation.

A resonant frequency of about 37 MHz is introduced by the coupling loop in the cavity. The tube plate sees a very big impedance (about 300 k Ω) at this frequency. A big voltage will be produced if the stimulus at this frequency exists. If this is the case, self-sustaining oscillation might happen because of the feed-through capacitance of the tube provide a positive feedback to the grid circuit. This should be further investigated in the future.

Acknowledgements

We would like to thank Joseph M. Brennan for providing the literatures on Vacuum Tube modeling and RF power amplifier design, and thank Richard Spitz, John Butler, and Alexander Zaltsman for their helps on understanding the RF accelerating system.

Appendix I Finding the Model Parameters From the Tube's Constant-current Curves

1) Finding μ_g

It can be seen from (1) that μ_g is the slope of a constant plate current curve. From the design curve with $v_s=1.5$ kV, $i_p=5$ A, and $v_p=8$ to 18 kV, it was found that:

$$\mu_g = \left. \frac{\partial v_p}{\partial v_g} \right|_{v_s = 1.5kV, i_p = 5A} = \frac{10kV}{18.3V} = 546$$

2) Finding μ_s

Like the case with μ_g , μ_s can be found by calculating the derivative of v_p with respect to v_s while keeping i_p and v_g constant. This was done by using two design curves with $v_s=1.5$ kV and 2.0 kV:

$$\mu_s = \left. \frac{\partial v_p}{\partial v_s} \right|_{v_g = 423V, i_p = 5A} = \frac{(-285 + 420)V \times 546}{500V} = 147$$

Because the resolution on the design curve is not very high, here the curve was extended beyond the page to get a measurement for Δv_p .

3) Finding x

Non-unity x is the major source for the non-linearity of the tube. It was found by taking the ratio of two points on the constant current curve:

$$\left. \frac{i_{p1}}{i_{p2}} \right|_{v_s = 1.5kV, v_p = 10kV} = \frac{5(A)}{15(A)} = \frac{1}{3} = \left(\frac{10kV + 147 \times 1.5kV + 546 \times (-285)}{10kV + 147 \times 1.5kV + 546 \times (-190)} \right)^x$$

thus: $x=2.1$

4) Finding A, B, and K

A is arbitrarily chosen to be 0.98. By fitting one point ($v_s=1.5$ kV, $v_p=10$ kV, $i_p=5$ A) on the constant current curve to the plate current equation, K was found to be $3e-10$.

It has been found that $B=0.5$ is a good approximation of the plate voltage effect after several trials and errors on the curves.

Appendix II Finding the Capacitances Between the Grids of the Tube

From the datasheet, the input, output, feed-through capacitances with grounded cathode configuration are:

$$C_{in}=370 \text{ pf}$$

$$C_{out}=60 \text{ pf}$$

$$C_{pg}=1.0 \text{ pf}$$

Those with grounded grid configuration are:

$$C_{in}=175 \text{ pf}$$

$$C_{out}=60 \text{ pf}$$

$$C_{pk}=0.35 \text{ pf}$$

Fig. 12 shows the capacitance model for these two configurations. From this model and the data given on the data sheet, the capacitances between all the electrodes can be found.

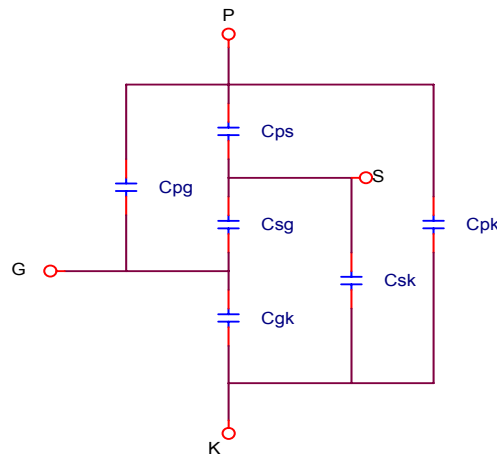


Fig. 12 Capacitance model of a tetrode

From the grounded cathode:

$$C_{in}=C_{gk}+C_{sg}+C_{pg} \cdot (C_{ps}+C_{pk}) / (C_{pg}+C_{ps}+C_{pk}) \approx C_{gk}+C_{sg}+C_{pg}=370 \text{ pf} \quad (\text{II.1})$$

$$C_{\text{feedthrough}}=C_{pg}=1.0 \text{ pf} \quad (\text{II.2})$$

$$C_{out}=C_{ps}+C_{pk}+C_{pg}=60 \text{ pf} \quad (\text{II.3})$$

From the grounded grid:

$$C_{in}=C_{gk}+C_{sk}+C_{pk}=175 \text{ pf} \quad (\text{II.4})$$

$$C_{\text{feedthrough}}=C_{pk}=0.35 \text{ pf} \quad (\text{II.5})$$

$$C_{out}=C_{ps}+C_{pk}+C_{pg}=60 \text{ pf} \quad (\text{II.6})$$

From (II.2), (II.3), and (II.5):

$$C_{pg}=1.0 \text{ pf}$$

$$C_{pk}=0.35 \text{ pf}$$

$$C_{ps}=60-1.35=58.7 \text{ pf}$$

The equation (II.6) is the same as (II.3). So only two equations left to find the rest 3 capacitances. Like C_{pg} , C_{sk} is a small capacitance formed by screen and cathode with another grid in between. 1 pf is a good guess for this capacitance. Thus:

Csk=1 pf
 Cgk=175-1-0.35≈173.7 pf
 Cgs=370-1-173.7=195.3 pf

Appendix III The SPICE Code for the Tube Model

```
.SUBCKT 4cw150k 1 2 3 4 ; P G1 C G2
+ PARAMS: MUs=147 MUg=546 EX=2.1 Kg=3e-10
+ Cgc=175P Cpg=1.2P Cpc=0.35P Cps=65p Csg=195p
+ Rg=1k
RE1 9 0 1k
ESP 6 0 VALUE=
+{V(1,3)+MUs*V(4,3)+MUp*V(2,3)};
E1 7 6 VALUE=
+{Kg*(PWRS(V(6),EX)+PWR(V(6),EX))/2}
E2 7 8 VALUE=
+{V(7,6)*V(1,3)/V(4,3)};
E3 9 8 VALUE=
+{(1-V(8,6))/(abs(V(8,6))+0.001))/2}
Gk 4 3 VALUE={V(7,6)}
Gp 1 4 VALUE=
+{0.98*(1-exp(-V(1,3)*2/V(4,3)))*(V(7,8)+V(8,6)*V(9,8))}
R3 2 5 {Rg}
*C1 1 2 {Cpg} ;Cpg & Cps are connected externally
C2 1 3 {Cpc}
*C3 1 4 {Cps}
C4 2 3 {Cgc}
C5 2 4 {Csg}
D3 5 3 DX ; FOR GRID CURRENT
.MODEL DX D(IS=1N RS=1 CJO=10PF TT=1N)
.ENDS
```

Appendix IV Design of a 85 kw PA Using 4cw150000 Tube

Pout=85 kW, assume a power efficiency of 75%, thus:
 Pin=85/0.75=113 kW, and
 Io=Pin/Vdc=113/18=6.3 A.
 Ipk≈4*6.3=25.2 A
 Pick up two points on the design curve to form the load line:
 Q point: Vp=18 kV and Vg=-400 V

Lowest-plate-voltage point: $V_p=2$ kV and $I_p=I_{pk}=25.2$ A, where V_{in} is read to be -110 kV.

On the load line, the plate currents are read at different point:

Points:	A	B	C	D	E	F
Degree:	0	15	30	45	60	75
I_p :	25.2	24	22	14.5	8.5	2.8

DC and RF currents are calculated:

$$I_{dc}=(0.5*25.2+24+22+14.5+8.5+2.8)/12=7.0 \text{ A}$$

$$I_1=(25.2+19.3*24+1.73*22+1.41*14.5+8.5+0.52*2.8)/12=11.7 \text{ A}$$

Therefore:

$$P_{dc}=V_{dc}*I_{dc}=18\text{kV}*7.0\text{A}=126 \text{ kW}$$

$$P_{rf}=0.5V_1*I_1=0.5*16*11.7=93.6 \text{ kW}$$

$$\text{Effeciency}=93.6/126=74\%$$

$$R_{out}=V_1/I_1=16/11.7=1.37 \text{ kOhms}$$

$$V_{in}=-110-(-400)=290 \text{ Volts}$$

$$\text{If } R_{in}=200 \text{ Ohms, } P_{in}=300^2/200/2=225 \text{ W}$$

Reference

- [1] S. Kwiatkowski, et al, "Power amplifier for RHIC 26.7 MHz accelerating Cavity", BNL Technical note RHIC/RF 28 Tech.
- [2] W. Marshall Leach, "SPICE models for vacuum-tube amplifiers," J. Audio Eng. Soc. Vol. 43, No.3 1995 March.
- [3] R. G. Carter, "Review of RF power sources for particle accelerators," CERN accelerator school proceeding, 1992.