# STUDY OF A NEW EXTRACTION SCHEME 

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Accelerator Division<br>Alternating Gradient Synchrotron Department BROOKHAVEN NATIONAL LABORATORY Associated Universities, Inc. Upton, New York 11973<br>Accelerator Division<br>Technical Note<br>AGS/AD/Tech. Note No. 280<br>STUDY OF A NEW EXTRACTION SCHEME

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Recent measurements of the efficiency of the AGS slow extraction give a result of $97 \pm 1 \%$. The increase in intensity expected from the future use of the Booster makes it desirable to improve this efficiency. This note presents the summary of studies on possible more efficient new extraction schemes for the AGS. All these results have been obtained using a program initially written for the HP 9845 desk computer, now available on IBM PC, ${ }^{2}$, and described in Appendix I.

## Present Extraction

Figure 1 shows the phase plane at the electrostatic septum (ES) straight section (bump not taken into account).

When the four sextupoles are powered, extraction can start, driven by a negative slope of the flattop. This pushes the beam from its stable position slightly inside the machine, toward the resonance region near the center. For each energy, there is a set of three separatrices, forming a triangle within which particles are stable. The lower the energy, the larger the stable triangle. Resonance occurs near the central orbit, when the triangle reduces to zero.

At any time during extraction particles escape on all separatrices between the zero emittance triangle and the nominal emittance one, the corresponding energy being higher for the zero and lower for the nominal emittance.

For a $2 \pi \mathrm{~mm}$ mrad emittance,

$$
\frac{\Delta p}{p} \simeq 2 \times 10^{-4}
$$

*Visitor from CERN.

Particles move outward along each of the three separatrices, one after the other, at an increasing velocity in the horizontal phase plane. They eventually jump across the ES, and are kicked toward the outside. They now follow trajectories outside the separatrices, with a different velocity, so that after almost three revolutions they reach the thin septum magnet (TSM) at F5. The part of the beam being extracted has then become wider, and is separated from the circulating beam by a gap wide enough to accommodate the 0.8 mm septum at F 5 , as can be seen in Figure 2 showing the horizontal phase space in $F 5$.

F5 gives the beam another kick to the outside, creating a hole at Fl0, wide enough to accept the 16 mm thick extraction magnet (EM), which deflects the beam to the outside into the extracted beam transfer line (Figure 3).

New Possibilities

There are two ways to improve efficiency:

1. decrease the ES effective thickness (Ti-alloy wires being tested), ${ }^{3}$
2. increase the spiral pitch at the ES.

We will concentrate on this second approach.

We must obviously drop the idea of using the non-linear effect to create the gap at the thin septum magnet, and we choose to use the ES deflection directly.

Unfortunately, the hole one can create at the TSM is small and emittance dependent (two examples in Figures 4 and 5). The phase of the extracted beam at the EM is also a problem. Figures 6 and 7 show cases in which the extractor magnet comes too early or too late in betatron phase around the machine. It is also possible that straight sections may not be available, as in the case of Figure 7, which would require that the ES be located in A20 in order to keep the EM in F10.

We, therefore, propose to enhance the kick produced at ES with a quadrupole to increase the clearance at the TSM. An additional quad of equal strength and opposite polarity will roughly cancel the tune shift due to the first quad and can be used to help adjust the phase at the EM.

A further gain can be obtained from the quads，since they modulate the dispersion functions around the machine．If the dispersion func－ tion is increased at the ES and decreased at the TSM，then the holes at the TSM created by the ES kick at various energies tend to move closer together．A careful choice of the quad locations can give this result． This effect becomes stronger if the chromaticity is reduced，but the instantaneous $\Delta \mathrm{p} / \mathrm{p}$ is then increased．

Three tentative schemes are presented here，as examples，following these principles．

1．ES in A20，TSM in F 5 ，and EM in F10 with quads in A 5 and L 5 normal chromaticity（Figures 8，9，and 10）．

2．Same as 非1 with reduced chromaticity（Figures 11，12，and 13）．

3．ES in F20，TSM in K5，and EM in F10 with quads in F5 and H5， normal chromaticity（Figures 14，15，and 16）．

4．Same as $⿰ ⿰ 三 丨 ⿰ 丨 三 一 2$ with reduced chromaticity and quad strength （Figures 17，18，and 19）．

Appendix II shows the main characteristics of these schemes together with those of the existing one，as calculated from the com－ puter program．Standard present strengths of the ES and TSM have been used．

None of these can be implemented as such due to the unavailability of many straight sections．There are obviously other interesting schemes，but no real good one has been found until now that fits in the present machine without requiring straight sections which are necessary for other uses．

However，the A20 straight section will no longer be used when the AGS is injecting through the Booster．Schemes 非1 and \＃2 would become possible．The second is particularly interesting as it offers small beam sizes for the circulating beam as well as in both magnetic septa for a 10 mm spiral pitch at the electrostatic septum．The clearances for both magnetic septa are large and relatively independent of emit－ tance．It is an attractive and simple design with apparently good performances，which could potentially halve the losses at extraction．

At this stage, one can list some of the further questions to be answered before one can talk of implementing the scheme:

- Make sure the A20 straight section is really available, and so are A5 and L5 for the quadrupoles.
- A current of 600 A is assumed for the quadrupoles, as well as the sextupoles. Is this possible, or should special elements be designed? The chromaticity will have to be decreased too.
- It may not be impossible to find a sextupole arrangement using still available straight sections in 5 , so that those in 13 would be freed for chromaticity corrections.
- The electrostatic septum gap and its voltage should be doubled, to increase the useful width and keep the field to its present value. Does this raise big problems?
- The instantaneous momentum dispersion is equal to about 8 x $10^{-4}$ for $1.5 \pi \mathrm{~mm}$-mrad ( 5 times bigger than at present for the same circulating beam emittance). Is this acceptable?
- The vertical phase optics should be checked.
- Last but not least, the next step should be a more realistic simulation with a sophisticated tracking program including the full machine non-linearities.

The author wishes to thank all the AGS people who have helped him in this work, one way or another, and particularly E. Bleser, C. Gardner, J.W. Glenn, D. Lowenstein, Th. Sluyters, A. Soukas, M. Tanaka, R. Thern, and W. van Asselt.

## References

1. M. Tanaka, Extraction Group Physics Note \#001.
2. R. Thern, Private Communication.
3. L. Repeta, Private Communication.

## COMPUTER PROGRAMME

The tracking programme, written in Basic, uses the interactive and plotting possibilities of the HP 9845 desk computer.

A set of data describes the machine. These are the values of the betatron wave number $Q$ in both planes and the horizontal chromaticity for the bare machine.

The number of straight sections taken into account is limited to those where a relevant element is installed: septum, dipole, quadrupole or sextupole. The data describing each section of the bare machine are:

- the phase angle as counted from the last section $\Delta \varphi_{i}$ for both planes,
- the Twiss parameters $\alpha_{i}, \beta_{j}$ for both planes,
- the dispersion parameter $\alpha_{p i}$ and its derivative $\alpha_{p i}^{\prime}$,
- the strength of the element located in the section,
- in the case of a septum, its radial position.

The elements are all considered as thin and placed in the centre of the straight section. The $2 x 2$ matrix, referring to the closed orbit as origin, between two sections labelled 1 and 2 is ${ }^{5}{ }^{6}$ :

$$
\left|\begin{array}{ll}
A_{11} & A_{12} \\
A_{21} & A_{22}
\end{array}\right|=\left|\begin{array}{lr}
\sqrt{\frac{\beta_{2}}{\beta_{1}}}\left(\cos \Delta \varphi_{2}+\alpha_{1} \sin \Delta \varphi_{2}\right) & \sqrt{\beta_{1} \beta_{2}} \sin \Delta \varphi_{2} \\
\frac{-1}{\sqrt{\beta_{1} \beta_{2}}}\left[\left(1+\alpha_{1} \alpha_{2}\right) \sin \Delta \varphi_{2}+\left(\alpha_{2}-\alpha_{1}\right) \cos \Delta \varphi_{2}\right] & \sqrt{\frac{\beta_{1}}{\beta_{2}}}\left(\cos \Delta \varphi_{2}-\alpha_{2} \sin \Delta \varphi_{2}\right)
\end{array}\right|
$$

and the $3 x 3$ matrix applying to the horizontal phase plane coordinates relative to the centre of the machine and to $\Delta p / p$ may be written ${ }^{7}$ :

$$
\left|\begin{array}{ccc}
A_{11} & A_{12} & \alpha_{p_{2}}-A_{11} \alpha_{p_{1}}-A_{12} \alpha_{p_{1}}^{\prime} \\
A_{21} & A_{22} & \because \alpha_{p_{2}}^{\prime}-A_{21} \alpha_{p_{1}}^{\prime}-A_{22} \alpha_{p_{1}}^{\prime} \\
0 & 0 & 1
\end{array}\right|
$$

A choice of actions allows the study of the extraction as defined by the programme data. Among, the possibilities, let us- point out:

- the program performs, on request, calculations of the $\beta$ fonctions as perturbed by the quadrupole in both planes for all odd straight sections.
- A " mountain climbing " routine finds out the horizontal closed orbit and $\Delta p / p$ of particles just on resonance, which allows tracking of the extraction from the centre of the emittance.
- Starting from an initial particle that can be changed at any time, tracking is performed and followed continuously on the plot of any of the straight section phase plane.
- The beam emittance enclosed in any stable phase plane trajectory can be calculated on request.
- A final plot of the horizontal phase plane, almost normalized, can be obtained from any of the sections. It shows the separatrices for the two energies corresponding to the nominal emittance and its centre, and the part of the beam being extracted. This is the way the figures presented in this paper were obtained.


## Compared Calculated Performances of Various Schemes

| Scheme | Spiral Pitch <br> mm | Clearance at 1st Mag. Septum <br> mm | Clearance at Extraction Mag. mm | Instantaneous $\Delta p / p$ | Beam Width <br> at F10 <br> mm | Corresponding Circulating Beam Emittance $\pi \mathrm{mm}$ mrad |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Present | 5.8 | $1.9{ }^{(1)}$ | 16.9 | $2.3 \times 10^{-4}$ | 14 | 2.5 |
| 非1 | 9.5 | 2.4 | 18.7 | $6 \times 10^{-4}$ | 10.4 | 2.5 |
| \#2 | 10.9 | 3.9 | 18.9 | $12 \times 10^{-4(2)}$ | 11 | 2.5 |
| \#3 | 10.4 | 4.3 | 23.0 | $2.3 \times 10^{-4}$ | 16 | 2.3 |
| \# ${ }^{\text {4 }}$ | 11.2 | 3.8 | 19.5 | $9 \times 10^{-4}$ | 20 | 2.8 |

(1) becomes 3.2 for a $1.5 \pi \mathrm{~mm}$ mrad emittance.
(2) becomes $8 \times 10^{-4}$ for a $1.5 \pi \mathrm{~mm}$ mrad emittance.

MOMENTF:


Zero emittance momentum : . 0 gagi
Hominal emittance momentum:-.06022

| 15.09 | 15.60 | 15.10 | 15.10 |
| :--- | :--- | :--- | :--- |
| 1.51 | 1.18 | 1.94 | 1.61. |

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$\left.\begin{array}{cc}20.82 & 18.31 \\ 2.49 & 1.92\end{array}\right\}$ condinats of herme Ato f on figue

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| XY1． | XF1 | $x y 2$ | YF2 | XY ${ }^{\text {Y }}$ | XF． | XYEI | XFC1 | XYCz | YFC |
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| 13.000 | 13.000 | $-17.578$ | $-13.946$ | $-8.715$ | -16.084 | 13.050 | 13.050 | 23.722 | 18.127 |
| 1.677 | 1.513 | $-1.47$ | -6.70 | $-1.711$ | $-2.25$ | 2.163 | 1.958 | 3. 387 | 2 |

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