# THREE DIMENSIONAL FIELD ANALYSIS FOR THE AGS COMBINED FUNCTION MAGNETS 

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## Introduction

The design of the AGS new fast extraction beam (NewFEB) system for the g-2 experiment and RHIC injection ${ }^{[1]}$ requires detailed magnetic field knowledge about the AGS main magnets, so that one may predict the trajectories of $29 \mathrm{GeV} / \mathrm{c}$ protons in the fringe field region during the extraction (Fig.1). 2d and 3d magnetic field computations have been done by using POISSON code and TOSCA programs. Partial results are described in this note. The comparisons between calculated field values and measured field maps show that if one properly handles the TOSCA program, high accuracy can be achieved. Further studies will show that particle tracking by using the post process of the TOSCA program is feasible ${ }^{[2]}$.

## POISSON Calculations

The pole surface of the AGS magnets was well designed many years ago, based on a constant magnetic scalar potential surface. The material of the magnets is the Electrical Grade M-36 Steel which contains $1.80 \%$ silicon and $0.03 \%$ carbon. The packing factor of the laminations is about $0.98^{[3]}$. To simulate the magnets in 2 d calculation, 51 points are used to define the curve of the pole surface (Fig.2), according to the final design ${ }^{[4]}$. The B-H data of the POISSON input is based on a measured magnetization curve. It was interporated in order to ensure the smoothness of its first derivatives and the continuity of its second derivatives.

Figure 3 and 4 are the plots of the computed vertical component of the magnetic induction $B_{y}$ and its gradient on the median plane versus the transverse coordinate $x$, for the "open" and "closed" types AGS magnets respectively.

Table 1 is the list of the data; table 2 is the harmonic content. The origin of the coordinates is located at the central orbit, so that it is $\pm 2$ inches deviated from the geometrical center of the pole, depending on the "closed" or the "open" type of magnets. The positive $x$ direction is pointing the ring center.

In principle, 2d computations should be comparable with the measurements near the middle of the magnet. Figure 5 shows the absolute comparison between the POISSON results and the measured data, in the case of feeding 41000 ampere per coil. The measurement ${ }^{[5]}$ was performed at the location of 27 inch into the magnet from the end face. One can hardly recognize that there are two curves in the figure; the measured curve is superimposed on the computed curve, from $x=-20 \mathrm{~cm}$ to $x=18 \mathrm{~cm}$. The disagreement is less than 2 part per thousand.

## TOSCA Calculations

The advent of relatively inexpensive and powerful computers has inspired the development of the large scale three dimensional codes. TOSCA is one of the most well known commercial codes which is widely used in the industry and accelerator field.

Based on the reference [4], a finite element model of one-quarter of the "open" type AGS magnet was constructed. Figure 6 only shows the steel part. The origin of the coordinate system of the TOSCA calculations is in the middle of the magnet and also at the beam center. The positive $x$ direction is pointing the ring center.

Figure 7 shows the landscape plot of the vertical components of $B$-field on the median plane, around the edge of the magnet. The base area 1-2-3-4 stands for the part of the median plane. The cartesian and polar coordinates of these four corners are listed on the right side of the figure. The vertical height of the surface stands for the magnitude of the component $B_{y}$ at particular position on the median plane. On the base area, there is a family of curves which represents the equal-height contours (or constant $B_{y}$ lines).

Figure 8(a) is the same subject but from different view point. Using a set of $\boldsymbol{x}=$ const.
planes to cut this surface, one gets a set of curves which represents the variations of $B_{y}$ along the axial direction $z$, at different transverse location $x$; that is shown in Figure 8(b).

Followings are part of the comparisons between the TOSCA results and the measured data.
(a) Compare with the low field measurements:

Measured data file AGBU01.MPA ${ }^{[5]}$ is the field map with the applied current 2880 ampere per coil. The center field is about 815 gauss, corresponding to $2 \mathrm{GeV} / \mathrm{c}$ protons. Figure 9 shows the comparison between the measured data and the calculation, on the median plane, near the center of the magnet. The difference is about $0.6 \%$. Figure 10 shows the comparison along the central beam line; the difference is about $0.7 \%$. Figure 11 shows the comparison in the fringe field region ( 6 inch away from the center); the difference is about $0.3 \%$.
(b) Compare with the high field measurements:

Measured data file B5150A.MPA ${ }^{[5]}$ is the field map of a open type AGS magnet; the applied current is 41000 ampere per coil ( 5150 ampere per pair), corresponding to 29 $\mathrm{GeV} / \mathrm{c}$ protons.

Measured data file A5150A.MPA ${ }^{[5]}$ is again the field map of a open type AGS magnet, except it measured only in the fringe field region along the open side of the magnet.

Figure 12 shows the comparison between the above two measured field maps and the TOSCA calculated results. The measured data B5150A.MPA covers from $x=0 \mathrm{~cm}$ to $x=18 \mathrm{~cm}$. The difference between this measured data and the calculation is about $0.5 \%$.

The measured data A5150A.MPA covers from $x=-40 \mathrm{~cm}$ to 0 cm , It is noticed that near the point $x=-9.14 \mathrm{~cm}$, the second order derivative shows some discontinuity. Accordingly one may estimate that the measurements error could be about $1.1 \%$. These prossibly arose from relocating the equipment and remaining magnetization in the steel core during the measurements.

Authors like to comment the TOSCA program and computations on the following points.
(a)Time Consumption. The time cost for constructing the finite element model depends on the problem size, complexity and the experience of the user. The computer CPU time has reduced tremendously since softwares are available on the UNIX machine (IBM RISC System.). General speaking, to obtain a field map with a reasonable accuracy, it takes less man power by using TOSCA program than by carrying out a measurement. Nevertheless measurements are always indispensable, since it is the most important way to examine the computed results, as long as the magnet is existing and accessible.
(b)The Accuracy of the TOSCA program. The local error at a field point is determined by (1) the size of the elements surrounding the point; (2) the types of these elements (linear or quadratic); (3) the method required to calculate the field value from the potential array (differentiation of shape function, interpolation of nodal averaged values, or integration of magnetization and currents); (4) the far boundary conditions and the potential types. From first glance, one could say that the accuracy is strongly linked to the size of the elements which is limited by the capacity of the program, but this is not the only factor. By making correct choices from factors (2), (3) and (4), reasonablely high accuracy is achievable. According to the results presented in this note, the error of the TOSCA computation is within the error of the measurements.

## Acknowledgment

Authors appreciate the AGS initiator G. Danby for his instructive guidance and discussion.

Authors appreciate $R$. Thern who reserves useful measured data files about the AGS magnets.
[1] M. Tanaka and Y.Y. Lee, BNL-45344.
[2] W. Meng and M. Tanaka, to be published.
[3] Alternating Gradient Synchrotron Project Construction Completion Report, December 1966.
[4] Engineering Drawing D03-M-666-5, D03-M-667-5.
[5] R. Thern, private communication.

Table I. Vertical Field Components for AGS Main Magnets

| $x[\mathrm{~cm}]^{j}$ | Open Magnets <br> By ( $x, y$ ) [gauss] |  |  | ClosedMagnets $\mathrm{By}(\mathrm{x}, \mathrm{y})$ [gauss] |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{y}=0.0 \quad[\mathrm{~cm}]$ | $y=1.0$ [cm] | $y=2.0$ [cm] | $\mathrm{y}=0.0$ [ cm$]$ | $y=1.0$ | $y=2.0[\mathrm{~cm}]$ |
| 35.00 | 244.632 | 239.466 | 223.925 | 785.695 | 776.259 | 747.850 |
| 34.00 | 301.328 | 295.228 | 276.931 | 932.274 | 922.617 | 893.768 |
| 33.00 | 370.183 | 363.271 | 342.328 | 1098.166 | 1088.256 | 1058.721 |
| 32.00 | 452.818 | 445.266 | 422.320 | 1283.912 | 1273.492 | 1242.769 |
| 31.00 | 550.472 | 542.569 | 518.569 | 1490.450 | 1479.323 | 1446.348 |
| 30.00 | 663.821 | 655.869 | 631.774 | 1719.414 | 1707.091 | 1670.726 |
| 29.00 | 793.047 | 785.235 | 761.674 | 1973.055 | 1959.154 | 1917.877 |
| 28.00 | 937.913 | 930.268 | 907.438 | 2254.800 | 2238.668 | 2190.938 |
| 27.00 | 1098.095 | 1090.578 | 1068.228 | 2569.028 | 2549.987 | 2493.833 |
| 26.00 | 1273.259 | 1265.804 | 1243.546 | 2921.500 | 2898.770 | 2831.697 |
| 25.00 | 1463.405 | 1455.820 | 1433.186 | 3319.617 | 3292.221 | 3211.361 |
| 24.00 | 1668.807 | 1660.932 | 1637.478 | 3772.779 | 3739.449 | 3641.404 |
| 23.00 | 1889.943 | 1881.671 | 1856.988 | 4292.803 | 4252.244 | 4132.332 |
| 22.00 | 2127.637 | 2118.876 | 2092.660 | 4894.441 | 4844.593 | 4697.530 |
| 21.00 | 2382.887 | 2373.563 | 2345.599 | 5596.369 | 5535.019 | 5353.894 |
| 20.00 | 2656.780 | 2646.880 | 2617.183 | 6421.036 | 6345.638 | 6122.979 |
| 19.00 | 2950.410 | 2939.995 | 2908.684 | 7396.535 | 7305.250 | 7032.310 |
| 18.00 | 3264.814 | 3253.994 | 3221.423 | 8552.403 | 8447.557 | 8122.647 |
| 17.00 | 3600.770 | 3589.685 | 3556.330 | 9915.666 | 9807.535 | 9451.888 |
| 16.00 | 3958.753 | 3947.593 | 3914.042 | 11481.799 | 11407.714 | 11102.826 |
| 15.00 | 4338.768 | 4327.813 | 4294.694 | 13175.547 | 13210.624 | 13199.825 |
| 14.00 | 4740.682 | 4730.146 | 4698.153 | 14768.125 | 15007.391 | 15820.633 |
| 13.00 | 5163.292 | 5153.606 | 5124.052 | 15909.600 | 16280.121 | 17715.729 |
| 12.00 | 5605.211 | 5596.860 | 5571.313 | 16384.783 | 16657.109 | 17498.480 |
| 11.00 | 6063.407 | 6056.943 | 6037.325 | 16328.815 | 16453.025 | 16730.533 |
| 10.00 | 6534.635 | 6530.239 | 6517.411 | 16007.716 | 16048.703 | 16120.461 |
| 9.00 | 7014.367 | 7012.097 | 7005.739 | 15587.454 | 15599.275 | 15617.825 |
| 8.00 | 7498.847 | 7498.239 | 7496.838 | 15136.125 | 15140.246 | 15147.791 |
| 7.00 | 7985.068 | 7985.333 | 7986.693 | 14674.849 | 14677.166 | 14683.707 |
| 6.00 | 8470.950 | 8471.586 | 8473.793 | 14207.441 | 14209.338 | 14214.270 |
| 5.00 | 8955.844 | 8956.468 | 8958.577 | 13737.682 | 13738.977 | 13742.769 |
| 4.00 | 9439.421 | 9440.046 | 9441.787 | 13265.366 | 13266.585 | 13269.677 |
| 3.00 | 9921.684 | 9922.247 | 9923.905 | 12791.472 | 12792.308 | 12794.375 |
| 2.00 | 10402.404 | 10402.954 | 10404.606 | 12316.388 | 12316.983 | 12318.443 |
| 1.00 | 10882.283 | 10882.765 | 10883.952 | 11840.263 | 11840.775 | 11843.048 |
| 0.00 | 11361.619 | 11362.159 | 11363.499 | 11362.364 | 11362.851 | 11364.327 |
| -1.00 | 11840.651 | 11841.078 | 11843.138 | 10882.892 | 10883.339 | 10884.604 |
| -2.00 | 12318.153 | 12318.751 | 12320.903 | 10402.511 | 10402.805 | 10403.710 |
| -3.00 | 12794.440 | 12794.876 | 12796.305 | 9921.133 | 9921.553 | 9922.514 |
| -4.00 | 13268.961 | 13269.594 | 13271.661 | 9439.495 | 9439.985 | 9441.522 |
| -5.00 | 13740.710 | 13742.242 | 13746.963 | 8956.825 | 8957.482 | 8959.596 |
| -6.00 | 14209.702 | 14210.975 | 14215.276 | 8473.038 | 8473.546 | 8475.479 |
| -7.00 | 14675.072 | 14677.305 | 14682.614 | 7988.221 | 7988.239 | 7988.880 |
| -8.00 | 15136.611 | 15141.147 | 15149.455 | 7503.607 | 7502.634 | 7500.334 |
| -9.00 | 15587.577 | 15600.431 | 15620.565 | 7021.134 | 7018.613 | 7011.376 |
| -10.00 | 16007.016 | 16048.773 | 16123.991 | 6544.021 | 6539.447 | 6525.798 |

[^1]
## TABLE 2. HARMONIC CONTENT



Closed Type

| N | $\mathrm{N}(\mathrm{AN}) / \mathrm{R}$ |
| ---: | ---: |
| 1 | $-1.1362 \mathrm{E}+04$ |
| 2 | $1.6035 \mathrm{E}+03$ |
| 3 | $6.1214 \mathrm{E}+00$ |
| 4 | $-1.3904 \mathrm{E}+00$ |
| 5 | $6.0634 \mathrm{E}-01$ |
| 6 | $1.7675 \mathrm{E}-01$ |
| 7 | $-5.5676 \mathrm{E}-01$ |
| 8 | $-4.6347 \mathrm{E}-01$ |
| 9 | $9.2682 \mathrm{E}-01$ |
| 10 | $-5.4988 \mathrm{E}-01$ |

N(BN)/R
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$

## Open Type

N(AN)/R
$-1.1362 \mathrm{E}+04$
$-1.6044 \mathrm{E}+03$
$5.4895 \mathrm{E}+00$
$1.2844 \mathrm{E}+00$
8.3096E-01
-8.6606E-01
-4.9661E-01
-1.8460E-01
4.6949E-01
2.3566E-01
$N(B N) / R$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$0.0000 \mathrm{E}+00$
$\operatorname{ABS}(N(C N) / R)$
$1.1362 \mathrm{E}+04$
$1.6035 \mathrm{E}+03$
$6.1214 \mathrm{E}+00$
$1.3904 \mathrm{E}+00$
6.0634E-01
$1.7675 \mathrm{E}-01$
$5.5676 \mathrm{E}-01$
4.6347E-01
9.2682E-01
5.4988E-01
$\operatorname{ABS}(N(C N) / R)$
$1.1362 \mathrm{E}+04$
$1.6044 \mathrm{E}+03$
$5.4895 \mathrm{E}+00$
$1.2844 \mathrm{E}+00$
8.3096E-01
8.6606E-01
4.9661E-01
1.8460E-01
4.6949E-01
2.3566E-01

Fig. 3 and 4 Field and Gradient


Fig. 3 Open Type

AGS Main Magnet (Closed)


Fig. 4 Closed Type


Fig. 5 Compare 2d Calculation with Measurement


Fig. 6 3d Módel (Elelments are not Shown)




Fig. 8(b) Field Profile


Fig. 9 Comparison along the Beam Line


Fig. 10 Comparison near the Center (Low Field)


Fig. 11 Comparison in the Fringe Field Region (Low Field)


Fig. 12 Comparison near the Center (High Field)


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