An orbit fit program for localizing errors in RHIC

C. Liu,

November 2011

Collider Accelerator Department

Brookhaven National Laboratory

U.S. Department of Energy

USDOE Office of Science (SC)

Notice: This technical note has been authored by employees of Brookhaven Science Associates, LLC under Contract No. DE-SC0012704 with the U.S. Department of Energy. The publisher by accepting the technical note for publication acknowledges that the United States Government retains a non-exclusive, paid-up, irrevocable, world-wide license to publish or reproduce the published form of this technical note, or allow others to do so, for United States Government purposes.
DISCLAIMER

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or any third party’s use or the results of such use of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof or its contractors or subcontractors. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.
An orbit fit program for localizing errors in RHIC

C. Liu, M. Minty, V. Ptitsyn

Collider-Accelerator Department
Brookhaven National Laboratory
Upton, NY 11973

Notice: This document has been authorized by employees of Brookhaven Science Associates, LLC under Contract No. DE-AC02-98CH10886 with the U.S. Department of Energy. The United States Government retains a non-exclusive, paid-up, irrevocable, world-wide license to publish or reproduce the published form of this document, or allow others to do so, for United States Government purposes.
An orbit fit program for localizing errors in RHIC

C. Liu∗ and M. Minty, V. Ptitsyn
BNL, Upton, NY, U.S.A.
(Dated: October 18, 2011)

Many errors in an accelerator are evidenced as transverse kicks to the beam which distort the beam trajectory. Therefore, the information of the errors are imprinted in the distorted orbits, which are different from what would be predicted by the optics model. In this note, we introduce an algorithm for fitting the orbit based on an on-line optics model. By comparing the measured and fitted orbits, we first present results validating the algorithm. We then apply the algorithm and localize the location of the elusive source of vertical diurnal variations observed in RHIC.

I. INTRODUCTION

The difference of two trajectories (linear accelerator) or closed orbits (storage ring) should match exactly a betatron oscillation, which is predictable by the optics model, in an ideal machine. However, in the presence of errors, the measured trajectory deviates from prediction since the model is imperfect. Comparison of measurement to model can be used to detect such errors. To do so the initial conditions (phase space parameters at any point) must be determined which can be done by comparing the difference orbit to prediction using only a few beam position monitors (BPMs). The fitted orbit can be propagated along the beam line based on the optics model. Measurement and model will agree up to the point of an error. The error source can be better localized by additionally fitting the difference orbit using downstream BPMs and back-propagating the solution. If one dominating error source exist in the machine, the fitted orbit will deviate from the difference orbit at the same point [1, 2].

II. ALGORITHM

In either a transport line or a storage ring, the beam trajectory in either transverse plane (neglecting coupling) can be expressed by the transfer matrix and initial conditions,

\[
\Delta z(s) = \sqrt{\beta_s \beta_i} \left( \cos (\phi_s - \phi_i) + \alpha_i \sin (\phi_s - \phi_i) \right) \cdot z_i + \sqrt{\beta_s \beta_i} \sin (\phi_s - \phi_i) \cdot z_i',
\]

(1)

where \( \beta_s, \beta_i, \phi_s, \phi_i \) are the beta functions and phase advances at position \( s \) and initial position \( i \); \( \alpha_i \) is the initial alpha and \( z \) represents either the horizontal \((x)\) or vertical \((y)\) motion. The following algorithm may be applied to both beam trajectory in linear machine and closed orbit in storage ring, which afterwards we will refer to as “orbit”.

The difference of two orbits comply with

\[
\Delta z = M_{11} \cdot \Delta z_i + M_{12} \cdot \Delta z_i',
\]

where \( M_{11} = \sqrt{\frac{\beta_s}{\beta_i}}(\cos (\phi_s - \phi_i) + \alpha_i \sin (\phi_s - \phi_i)) \), \( M_{12} = \sqrt{\beta_s \beta_i} \sin (\phi_s - \phi_i) \).

By selecting a fitting range from the \( m \)th BPM to the \( n \)th BPM, a set of linear equations follows,

\[
\begin{align*}
\Delta z_m &= M_{11}^m \cdot \Delta z_i + M_{12}^m \cdot \Delta z_i' \\
\Delta z_{m+1} &= M_{11}^{m+1} \cdot \Delta z_i + M_{12}^{m+1} \cdot \Delta z_i' \\
&\vphantom{= M_{11}^{m+1} \cdot \Delta z_i} \vdots \\
\Delta z_n &= M_{11}^n \cdot \Delta z_i + M_{12}^n \cdot \Delta z_i'
\end{align*}
\]

(2)

Using a least-square fit (minimizing the merit function \( f = \sum_{k=m}^{n} (\Delta z_k - M_{11}^k \cdot \Delta z_i + M_{12}^k \cdot \Delta z_i')^2 \)), we obtain the

∗cliu1@bnl.gov
Initial conditions as

\[
\begin{align*}
\Delta z_i &= \frac{\sum_{k=m}^{n} \Delta z_k M_{11}^{k} \sum_{k=m}^{n} M_{11}^{k} M_{12}^{k} - \sum_{k=m}^{n} \Delta z_k M_{11}^{k} \sum_{k=m}^{n} (M_{11}^{k})^2}{\sum_{k=m}^{n} (M_{11}^{k})^2 - \sum_{k=m}^{n} (M_{12}^{k})^2 - \sum_{k=m}^{n} (M_{11}^{k})^2} \\
\Delta z_i' &= \frac{\sum_{k=m}^{n} \Delta z_k M_{11}^{k} \sum_{k=m}^{n} (M_{12}^{k})^2 - \sum_{k=m}^{n} \Delta z_k M_{12}^{k} \sum_{k=m}^{n} M_{11}^{k} M_{12}^{k}}{\sum_{k=m}^{n} (M_{11}^{k})^2 - \sum_{k=m}^{n} (M_{12}^{k})^2 - \sum_{k=m}^{n} M_{11}^{k} M_{12}^{k}}
\end{align*}
\]

(3)

Once the initial conditions are so determined, the fitted orbit along the ring can be computed based on Eqs. 1.

### III. APPLICATION VERIFICATION

This algorithm was integrated into RhicOrbitDisplay. As a demonstration, we use orbit data acquired during measurements made to check the BPM polarities. In RHIC, there is a possibility of BPM cable swaps following maintenance which would cause problems for orbit feedback which is now used for each acceleration cycle. The BPM polarity check works in this way. First the closed orbits before and after making a strength change of a corrector are recorded. The difference between those measurements, the so called difference orbit, is then formed. The difference is also predicted by the on-line model with knowledge of the corrector strength. A BPM polarity error can be identified when signs of the measured and predicted difference orbit do not agree.

As an after-fact test, we applied the algorithm and try to localize an error source, which in this case was due to the intentionally varied dipole corrector. The following horizontal orbit data was taken in the Blue ring, on Mar. 14th, 2011 (fill number: 15290). Shown in Fig. 1 are the measured horizontal difference orbit (blue) and the fitted orbit (cyan) by forwards propagation.

![FIG. 1. Measured horizontal difference orbit (blue) versus the fitted orbit (cyan) by forwards propagation](image1)

The region (by zooming in Fig. 1) where the fitted orbit starts to deviate from the difference orbit.

![FIG. 2. The region (by zooming in Fig. 1) where the fitted orbit starts to deviate from the difference orbit](image2)

![FIG. 3. Measured horizontal difference orbit (blue) versus the fitted orbit by backwards propagation](image3)
FIG. 4. The region (by zooming in Fig. 3) where the fitted orbit starts to deviate from the difference orbit orbit (cyan). The fit range was 200 to 800 m and the fitted orbit was propagated forward. The agreement between measurement and fit is very good upstream of the BPM at 2686 m. The expanded range shown in Fig. 2 reveals that the two orbits begin to deviate between BPMs located at 2683 and 2740 m, which is in agreement with the longitudinal coordinate (2713 m) of the dipole magnet (bo2-th10) that was used. In order to confirm this result, a different region (3000 to 3600 m) was selected for fitting and the resulting fitted orbit was propagated backwards for the same set of data. The result (Fig. 3) agrees with that in Fig. 1.

In the vertical plane with separation bumps, this algorithm works equally as well. The following vertical orbit data were taken in Yellow, on Jan. 17th, 2011 (fill number: 14822). Fig. 5 shows the fitted orbit (fitting range: 200 to 800 m) versus measured difference orbit, which start to deviate from one another in between 2710 and 2740 m (in Fig. 6). The backwards propagated fitted orbit versus difference orbit (in Fig. 7) confirms the finding in Fig. 5. This agrees with the fact that the dipole magnet being used (yi2-tv10) was at 2713 m.

We conclude from this analysis that the online orbit fit algorithm correctly localized an intentionally introduced perturbation. The localization was accurate with a range given by the distance between the two closest BPMs.
IV. LOCALIZATION OF DIURNAL DISTURBANCES IN RHIC

Diurnal variations in the beam trajectory have long been observed at RHIC [3]. Using turn-by-turn BPM data [4], the source for vertical deviations was localized to near the IR at the vicinity of the accelerating cavities (IR4). The source was thought to originate near the cryogenic feed lines located there. As a test, these feed lines were mechanically decoupled from the roof of the accelerator tunnel [5], however, this did not seem to mitigate the diurnal perturbation to the beam trajectories.

To confirm this locale of diurnal variations, we applied the orbit fit algorithm to two sets of data. We took two orbit measurements at store (fillno: 15808, optics: Au11v1, time: 7:35:00 AM, 08:02:08 AM) and applied the orbit fit algorithm to the vertical difference orbit. First we used a range from 2000 to 2800 m for the fitting, and forward propagated the fitted orbit along the ring. The difference orbit and the fitted orbit were seen to deviate from one another near the 3 o’clock side of IR4. The details are clearer in Fig. 10 and Fig. 11 which shows the difference of the original difference orbit and the fitted orbit.

Then, a different range (from 3400 to 3800 m) was used for the fitting, and the fitted orbit was backward propagated. The result from forward propagation was confirmed by the backward propagation since the orbits start to deviate in the same region.

In this example the orbit fit program confirmed that the source of diurnal variation of RHIC orbit is in IR4 region, which is suspected to be the cryogenic pipe, however, further narrow down of the longitudinal position of the source is needed. The precision of localizing error sources by orbit fit program is limited by the spacing of BPMs, which is tens of meters at RHIC.
FIG. 11. The difference of original difference orbit and forward propagated fit orbit

FIG. 12. The vertical difference orbit (blue) vs fitted orbit (black) using range from 3400 to 3800 m and backward propagation

FIG. 13. Expanded view of Fig. 12 showing that the deviation originating from IR4

FIG. 14. The difference of original difference orbit and backward propagated fit orbit

V. POSSIBLE FUTURE APPLICATION

In principle the algorithm given here could be applied on a much faster time scale using as input data from the BPMs acquired turn-by-turn.

As a case in point, some errors in RHIC could degrade the beam emittance seriously and take hours, sometimes days to be found or never being found. The blue abort kicker and yellow spontaneous debunching are the two most notorious problems in Run-11, of which the first one was eventually found by turning off element by element, the latter one disappeared before the source could be found. With the new orbit fit function, the hunting for error sources could be much easier.

What makes the search for the error source difficult for the two mentioned cases is, the sources are intermittent
Instead of static. This is clear from the fast BPM measurement (Fig. 15), taken while the bunch lengthening was present. Fortunately, the turn-by-turn BPMs can be configured to take measurements with spacing other than 1 turn. By varying the spacing of two consecutive measurements, one would be able to record orbits with and without the error source kicking the beam. Then, one could locate the error source by following the demonstrated procedure.

VI. CONCLUSION

An orbit fit algorithm for both transport lines and storage rings was presented. The algorithm has been implemented into RhicOrbitDisplay. Offline tests using BPM polarity check data validated its potential for hunting error sources in RHIC. Its application supported previous analysis suggesting that the motion of quadrupole magnets near the cryogenic feed pipe in IR4 are responsible for the diurnal drift seen in RHIC. A short user’s guide is given in Appendix.

ACKNOWLEDGMENTS

C. Liu would like to thank J. Kewisch and Ted D’Ottavio for the help on programming, R. Michnoff on turn-by-turn BPM configuration and M. Blaskiewicz for discussions.

We would also like to acknowledge P. Emma (SLAC)’s initial application at the SLC.

We thank also A. Marusic for raising the question of possible “moving magnets” and for clarifying the actions taken years ago (decoupling of the cryogenic lines from the roof versus full and complete decoupling).

Appendix: User’s guide

In RhicOrbitDisplay, clicks orbit in the menu bar. A pull down menu appears which has the new Fit Orbit at the bottom (Fig. 16).

Clicking on Fit Orbit leads to the Orbit Fit window (Fig. 17), which resembles the Orbit Correction window.
FIG. 16. RhicOrbitDisplay pull down menu

FIG. 17. Orbit fit window