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Transversely driven coherent beam oscillations and specifications for high-frequency ESR dipole power supply current ripple

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I. ABSTRACT

We study coherent transverse beam oscillations in the EIC electron storage ring (ESR), to specify the tolerance for high-frequency ripple of the dipole magnet power supplies. To avoid unacceptable proton emittance growth from the oscillating beam-beam kick from the electrons, the amplitude of these oscillations at the proton betatron frequency needs to be limited to about 1e-4 fraction of the beam size at the interaction point. We show that the oscillations potentially caused by the ESR magnet dipole power supply ripple could be substantial, but still tolerable, if we account for the eddy current shielding in the vacuum chamber.

II. INTRODUCTION

The ESR has very tight tolerances for the beam position and size stability at the interaction point (IP). The oscillations at the proton betatron frequency and its harmonics are the most dangerous because they could lead to unacceptable proton emittance growth from the oscillating beam-beam kick from the electrons at the amplitude of the positional oscillations as low as 10^{-4} of the rms beam size [1, 2].

These oscillations may have many different causes, including the dipole power supply (PS) ripple, the phase noise in the main [3] or crab RF systems [4], and some collective instabilities (e.g. [1]). The dipole PS is our focus here.

A dipole rippling at low frequency causes closed orbit oscillations. However, if the ripple frequency is close to the fractional part of the betatron tune or its harmonics, then, for the same ripple amplitude, beam oscillations of much larger magnitude around the (fixed) closed orbit can be resonantly excited. This effect is the main subject of this note.

For the ESR revolution frequency f_0=78.2 kHz and the lowest possible value of the fractional part of the betatron tune of $\sim$0.1, these oscillations can be caused by driving sources in the range of $\sim$[8-40] kHz (the frequencies above $f_0/2$ are folded back for once-per-turn beam sampling).

For the usual switching type DC power supplies, narrow-band switching frequency harmonics as well as some wide-band noise could be present in this frequency range.

In this note, we present an analytical study of the effects of these two types of noise.

To make the problem tractable, we make several simplifying assumptions and conservative approximations so that our conclusions can be used to specify the ESR dipole PS high-frequency ripple and noise with some safety margin.

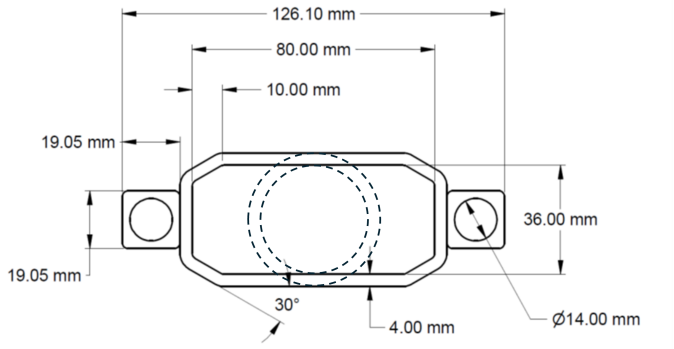


FIG. 1. ESR vacuum chamber cross section. Dashed profile shows the axially-symmetric approximation used in [5, 6].

Preliminary results of this analysis were presented in [5, 6]. In this note, we present a more detailed derivation and update the final PS ripple specifications in two key ways.

First, when calculating the field ripple attenuation due to the vacuum chamber, we incorporate the recently adopted chamber cross-section, replacing the previously used axially symmetric approximation (both sketched in Fig. 1). This adjustment relaxes the high-frequency ripple specification by approximately a factor of four in amplitude units.

Second, we account for the recently adopted ESR dipole powering scheme [7], which accommodates switching between 5, 10, and 18 GeV operating energies by tapping the coils in each dipole magnet while adjusting the dipole PS current by only a factor of 2.6[1]. This approach differs from the original scheme, in which the current for most dipoles was proportional to the beam energy, thus varying by a factor of 3.6. Consequently, the new powering scheme further relaxes the ripple specifications[2] by an additional factor of 1.4.

III. MAXIMUM AMPLITUDE AT THE IP

There are generally two types of fast oscillations in DC magnets, predictable baseline shifts due to things like power supply switching and 60 Hz harmonics ripple, and true noise.

[1] Main Bus current values are 391.4 A (18 GeV), 214.5 A (10 GeV), and 556 A (5 GeV), see Fig. 4-2 of [7].

[2] In amplitude units, normalized to the maximum operating dipole PS current.

The net field at a given location in the vacuum chamber is then written

$$B(t) = B_0 + B_p(t) + B_n(t). \tag{1}$$

The net fluctuating field is $B_1(s,t) = B_p + B_n$, where s is the longitudinal Serret-Frenet coordinate which updates by the circumference, C, each turn.

Consider horizontal motion of a single electron bunch subjected to dipole field errors

$$\frac{d^2x}{ds^2} + K(s)x = \frac{B_1(s,t)}{(B\rho)} - \frac{2}{s_d}\frac{dx}{ds}, \tag{2}$$

where $(B\rho)$ is the magnetic rigidity, $s_d = c\tau_d$ is the total damping distance and $K(s)$ is the net focusing. The solution is

$$x(s) = \int_0^s ds_1 \frac{B_1(s_1,t_1)}{(B\rho)} \sqrt{\beta(s)\beta(s_1)}\sin[\psi(s) - \psi(s_1)] \times \exp[(s_1 - s)/s_d]. \tag{3}$$

Since $s_d \gg C$, the details of beta function weighting have been ignored. The motion of the electron bunch is due to the summation of many independent kicks. On a given turn the motion is basically a free oscillation, so we can understand the statistics of the process by focusing on a fixed location in the ring. For simplicity assume that we have $s = 0$ at this location and that $d\beta/ds = 0$ there. Then

$$(x + i\beta x')_{n+1} = (x + i\beta x')_n \exp(-i2\pi\nu - C/s_d) + F(n),$$
$$F(n) = \int_0^C ds_1 \frac{B_1(s_1, s_1/c + nT_0)}{(B\rho)} \sqrt{\beta(0)\beta(s_1)} ie^{-i(\psi(s_1) - 2\pi\nu)},$$

where $\psi(0) = 0$, ν is the betatron tune, $T_0 = C/c$ is the revolution period.

Now suppose there are M independent magnet strings. An exact representation appears difficult but to a reasonable approximation take

$$\frac{B_1(s,t)}{(B\rho)} = \sum_{k=1}^{M} b_k(s) n_k(t - \tau(s)), \tag{4}$$

where $b_k(s) = b_k(s+C)$ describes the spatial extent of the string and $\tau(s) = \tau(s+C)$ describes the effect of voltage travel time within the magnet string. At this point, we temporarily ignore the B_p term in Eq. (1) and consider true noise with unit standard deviation and

correlation function $\langle n_k(t_1)n_k(t_2)\rangle = \rho_k(t_1 - t_2)$. Since everything is linear, we may write $F(n) = \sum_{1\le k\le M} F_k(n)$ with

$$F_k(n) = \int_0^C ds_1 b_k(s_1) n_k(nT_0 + s_1/c - \tau(s_1))\sqrt{\beta(s)\beta(s_1)}$$
$$\times\, i\exp[-i(\psi(s_1) - 2\pi\nu)]. \tag{5}$$

The $F_k(n)$s are discrete random variables. Since the change in amplitude will involve many thousands of kicks we may assume the noise is Gaussian so that only the rms value and the frequency spectrum are needed.

Without more information, it is difficult to evaluate these expressions. If we assume the worst case where all errors add coherently then

$$F(n) = \sum_k F_k(n) \approx 2\pi\sqrt{\bar\beta\beta_0}\frac{\delta B(n)}{\bar B}, \tag{6}$$

where the overbar denotes the ring average. The spectrum associated with $F(n)$ is

$$S_F(\phi) = \lim_{N\to\infty}\langle\frac{1}{N}\left|\sum_{n=1}^{N} F(n)e^{in\phi}\right|^2\rangle. \tag{7}$$

While $F(n)$ is complex, the error with taking it to be real is small since it takes many kicks to change the amplitude appreciably.

A significant danger of these electron oscillations is that they will drive emittance growth in the hadron beam. Let x_n denote the time series of electron centroid offsets at the IP. The proton un-normalized rms emittance will grow in a random walk according to [1]

$$\frac{d\epsilon}{dn} = \frac{(4\pi\Delta\nu_{bb})^2}{2\beta^*}\sum_{m=-\infty}^{\infty}\langle x_{m+n}x_n\rangle\cos(2\pi m\nu_p), \tag{8}$$

where $\Delta\nu_{bb}$ is the beam-beam tune shift, β^* is the proton beta function at the IP and ν_p is the proton tune. The horizontal emittance of the protons is of order 10^{-8} m. Assume this doubles in 10 hours. The beam-beam tune shift is limited to 0.015. The horizontal $\beta^* \sim 80$ cm. Taken together this implies the sum on the right of Eq. (8) is $1.6\times10^{-16}\,\mathrm{m}^2$. For white noise this implies $\langle x_{m+n}x_n\rangle = \delta_{m,0}\langle x^2\rangle = \delta_{m,0}(0.00012\sigma)^2$ with σ the horizontal rms size.

More sophisticated estimates using multiparticle tracking for various noise models give a similar constraint [2]. Below this will be rounded off to

$$x_{\mathrm{rms}} = 10^{-4}\sigma. \tag{9}$$

IV. MAXIMUM DIPOLE NOISE AND RIPPLE

A. MAXIMUM RANDOM NOISE

To calculate $\langle x_{m+n}x_n\rangle$ we assume $F(n)$ is white noise and we will also assume $\nu = \nu_p$. Assume that s_d corresponds to many turns. All the sums can be done in closed form and to a good approximation one finds

$$\sum_{m=-\infty}^{\infty} \langle x_{m+n}x_n\rangle \cos(2\pi m\nu_p) = \frac{\langle F^2\rangle}{4}\left(\frac{s_d}{C}\right)^2. \tag{10}$$

For actual noise one makes the replacement $\langle F^2\rangle \to S_F(2\pi\nu)$.

To proceed we take a worst-case estimate for F. Suppose all the dipole errors add in phase. Then one has

$$\langle F^2\rangle \approx 4\pi^2\bar{\beta}\beta^* S_{\delta B/B}(2\pi\nu). \tag{11}$$

Combining everything one finds

$$(10^{-4}\sigma)^2 = \pi^2\bar{\beta}\beta^* S_{\delta B/B}(2\pi\nu)\left(\frac{s_d}{C}\right)^2. \tag{12}$$

We postpone numerical estimates for the maximum allowable noise until after we discuss the maximum ripple.

B. MAXIMUM RIPPLE

Here we assume a sinusoidally-varying field ripple that causes resonant transverse oscillations when the frequency of the B_p term in Eq. (1), is close to the betatron tune. This problem was treated before, e.g. for AC-dipoles in hadron rings or for the swept-sine excitation tune measurement in electron rings. We will follow [8] below.

First, assume a single thin dipole at $s = 0$ with the kick

$$\theta(t) = \theta_0\cos(\omega t + \phi). \tag{13}$$

Also, assume that the damping rate, $\alpha = 1/\tau_d$, comes from the synchrotron radiation as well as from the betatron tune spread

$$\alpha = \alpha_R + \delta\omega_\beta, \tag{14}$$

where the betatron frequency distribution is taken to be Lorentzian with the half-width $\delta\omega_\beta$. The resulting positional oscillations in complex notation are given by

$$x(s,t) = -\frac{\theta_0}{4}\sqrt{\beta(0)}\sqrt{\beta(s)}e^{i(\omega t+\phi)}e^{-i(\omega-i\alpha)s/c}e^{i\alpha T_0/2} \times(\pm)\frac{e^{\pm i\psi(s)}e^{i\pi(\nu_d\mp\nu_\beta)}}{\sin[\pi(\nu_d\mp\nu_\beta)-i\alpha T_0/2]}, \tag{15}$$

where $\psi(s)$ is the phase advance, $\psi(0)=0$, $\nu_d=\omega T_0/(2\pi)$ is the driving tune, and summation over $(\pm)$ is assumed.

At resonance, $\nu_d-\nu_\beta=n$, for some integer n, this simplifies to

$$x(s,t) = \frac{\theta_0\sqrt{\beta(0)}\sqrt{\beta(s)}}{4\sin(i\alpha T_0/2)}e^{i(\omega t+\phi-(\omega-i\alpha)\frac{s}{c}+\alpha\frac{T_0}{2}+\psi(s))}. \tag{16}$$

Taking the real part, and assuming that $\alpha T_0 \ll 1$, we get the peak amplitude of the oscillations in physical space

$$\hat{x}(s) = \frac{\theta_0\sqrt{\beta(0)}\sqrt{\beta(s)}}{2\alpha T_0}. \tag{17}$$

From linearity, the same relation holds between the rms amplitude, $x_{\rm rms}(s)$, and the rms kick, $\theta_{0,\rm rms}$.

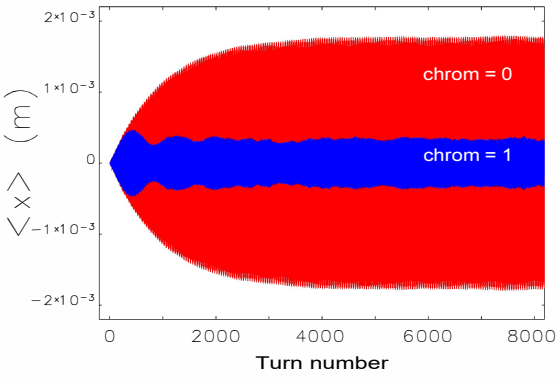


FIG. 2. Centroid of the bunch driven at ν_x.

We checked Eq. (17) against Elegant [9] tracking simulations and found good agreement. For instance, for the parameters used for the red trace in Fig. 2 (E=18 GeV, αT_0=1/1000 at zero chromaticity and no beam-beam, θ_0=1 μrad, $\beta(0)$=32 m, $\beta(s)$=0.4 m), Eq. (17) gives the peak value of $\hat{x}(s)$=1.8 mm which is virtually the same as in Fig. 2.

Note that for the ESR the coherent damping mainly comes from the tune spread due to beam-beam interaction, which is illustrated in Fig. 3. While the beam-beam parameters

$\xi_{x,y}$ vary between different colliding configurations, a 100-turn damping, αT_0=1/100, is a reasonable conservative choice to be used below.

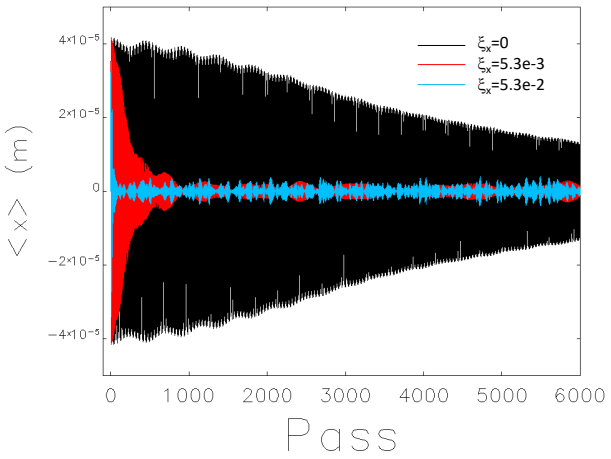


FIG. 3. Damping with beam-beam at 5 GeV.

To add the kicks from multiple dipoles driven at the same frequency, one can sum up the contributions from each as given by Eq. (16). In contrast to the single-kick case, Eq. (17), the resulting amplitude will additionally depend on the betatron phase advances, the electrical phases (through $e^{i\phi}$ factors), and the magnet s-locations.

In the worst case, the contributions from all rippling dipoles, each given by Eq. (16), will add in phase at the IP. Dividing the resulting rms kick by the total bend angle and using Eq. (9), we get for the rms field ripple,

$$\delta B/B = \frac{\theta_{0,\mathrm{rms}}}{2\pi} = 10^{-4}\sigma\frac{\alpha T_0}{\pi\sqrt{\bar{\beta}}\sqrt{\beta^*}}. \tag{18}$$

V. DIPOLE PS HIGH-FREQUENCY RIPPLE SPECIFICATIONS

We first note that Eq. (18) is identical to Eq. (12) with replacements $\delta B/B = \sqrt{S_{\delta B/B}}$ and $(s_d/C)\,\alpha T_0 = 1$. The fact that both estimates— one assuming stochastic noise and the other sinusoidally driven motions—yield the same result, instills confidence in our comprehensive consideration of noise contributions of any type. Below we will use "ripple" to denote "noise and ripple" for short, because the two were found equivalent.

Substituting σ=100 μm, β^*=0.4 m, and $\bar{\beta}$=30 m in Eq. (18) we finally get $\delta B/B$=9.2e-12 rms.

According to this very conservative estimate, 1 part-per-million (ppm) PS current ripple at[3] ν_x is acceptable, as long as 5 more orders of magnitude of attenuation are coming from elsewhere. According to the conservative estimates in [10, 11], this amount of attenuation does occur at frequencies exceeding ∼20 kHz due to eddy currents in the vacuum chamber.

In reality, even when all dipoles are powered by the same PS, as is effectively the case in the current powering scheme, their high-frequency ripples do not add in phase due to s-dependent factors in the exponent of Eq. (16). Consequently, a cancellation factor of at least $N_d^{-1/2}$ can be reasonably assumed, where $N_d \approx 700$ represents the total number of dipoles. Based on this assumption, and considering the relevant width of the tune line to be of the order of the beam-beam parameter ($\Delta\nu = 0.01$), the maximum power spectral density of the field ripple is given by

$$P_{\delta B/B} = \frac{T_0}{\Delta\nu}\left(10^{-4}\sigma\sqrt{N_d}\frac{\alpha T_0}{\pi\sqrt{\bar{\beta}\beta^*}}\right)^2. \tag{19}$$

Dividing this expression by the frequency-dependent attenuation factor caused by eddy currents in the vacuum chamber, quantitatively described in [11], yields the maximum allowable power spectral density of the dipole PS current ripple, $P_{\delta I/I}$. By derivation, this quantity is normalized to the dipole PS operating current at the given beam energy.

A more useful specification is to normalize the current ripple by I_{max} - the maximum operating PS current over all energies. As mentioned in the Introduction, the highest main bus dipole current, $I = I_{max} = 556$ A, occurs at 5 GeV, making the ripple specification at this energy the most restrictive. This final specification $P_{\delta I/I_{max}}$ is plotted in Fig. 4.

For completeness, the dashed line in Fig. 4 shows the corresponding specification from our earlier analysis [5, 6]. That earlier work, based on conservative assumptions, employed an axially symmetric approximation for the chamber cross-section and the scaling $I_{\text{dipole}} \propto E$, which was applicable to most dipoles in the original ESR magnet powering scheme. As noted in the Introduction, these two factors—expressed in amplitude units—restrict the ripple specification by factors of approximately 4 and 1.4, respectively, compared to the current specification. Thus, the updated specification is about 5.6 times less restrictive in

[3] More accurately, we must consider a band of frequencies which fall within the beam-beam tune-spread, so we take this bandwidth to be $\Delta\nu$=0.01.

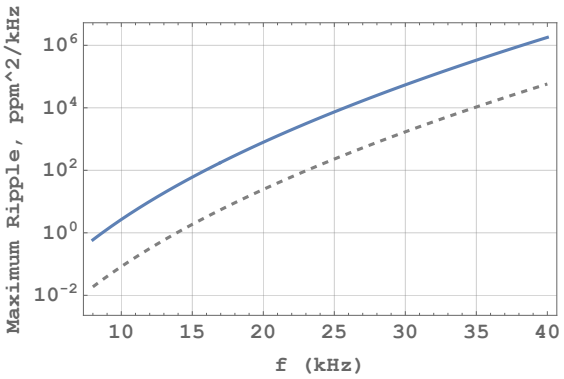


FIG. 4. (solid) Maximum allowable rms current ripple normalized to the maximum operating dipole PS current; (dashed) same for axially-symmetric chamber approximation and the (now obsolete) original powering scheme with $I_{\text{dipole}} \propto E$ for most dipoles.

amplitude (or 5.6^2 in power terms), offering significantly greater flexibility in the selection of the ESR dipole PS.

VI. CONCLUSION

The high-frequency dipole field ripple specifications for the ESR were derived, requiring $10^{-4}\sigma$ rms positional stability at the IP in the frequency range [8-40] kHz. We assumed the worst-case scenario of an external perturbation exciting the electron beam at the betatron tune. The field ripple specifications were propagated to the dipole PS current ripple, taking credit for the attenuation in the vacuum chamber. If the PS switching frequency exceeds ~20 kHz, the high-frequency ripple specification does not appear to be overly restrictive.

We emphasize that the conclusions above only apply to the resonant excitation, which may occur above ~8 kHz. Low-frequency orbit and beam size oscillations at the IP require a different analysis, which results in very tight magnet PS specifications (see e.g. [5]) and may also force us to consider some fast beam-based feedbacks at the IP. This work is still ongoing.

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