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Simulation of Polarized Electron Bunch Acceleration in EIC RCS Bunch and Spin Densities at Extraction

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Abstract

This Tech. Note reports numerical methods and outcomes regarding the simulation of polarized bunch acceleration in the EIC RCS [1], from injection (or bunch merge) energy to ESR store energy, including bunch densities and polarization at the end of the acceleration ramp, ready for transfer to the ESR. This work is based on earlier code developments and similar studies regarding CESR RCS injector [2].

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1 Introduction

The EIC electron-hadron collider project, currently in its conceptual design stage, includes an electron rapid cycling synchrotron (RCS), as the full energy injector to the electron storage ring (ESR).

This Tech Note summarizes simulations of full acceleration cycles in the RCS, their outcomes include final bunch densities and polarization at the end of the acceleration ramp, ready for transfer to the ESR. Tracking simulation hypotheses are detailed, including some of the input data to the tracking code. Some developments specific to EIC RCS simulations, including RF management, are outlined, for clarity.

Specimen of the simulation input data files resorted to here, are available at

<https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/EIC/RCS/>

Similar studies have been performed in the past for a similar energy (greater repetition rate) RCS, namely, CESR injector at Cornell. Reference [2] can be referred to for comparison of both the methods and results, including polarization preservation. Simulation data files can be found at

https://sourceforge.net/p/zgoubi/code/HEAD/tree/trunk/exemples/Cornell_rings/RCS_injector/

2 EIC RCS Parameters

Table 1 lists RCS parameters considered for the setup of the polarization transport simulation files. Figure 1 shows the orbit hypotheses (zero orbit), Figure 2 shows the optical functions, lattice parameters (MADX style “Twiss file” header) are given in Tab. 2.

Detailed statistics from Monte Carlo synchrotron radiation at 0.4, 1, 5, 10 and 18 GeV are given in page 5, they are summarized in Tab. 4. The latter also gives the SR integrals in ESR and RCS.

Table 1: RCS parameters in the tracking simulations.

Initial energy	GeV	1
Top energy	GeV	5, 10, 18
Circumference \mathcal{C}	m	3841.35
Bend radius	m	235.000
<i>Lattice</i>		
Arc β_x, β_y , max.	m	≈ 80
Q_x, Q_y (frac.)		0.8329, 0.7543
ξ_x, ξ_y		few units
<i>Bunch parameters, at injection</i>		
$\beta\gamma\varepsilon_{x,y}$	($\pi\mu\text{m}$)	26
Length, total	ps	180
dE/E, rms		$2.5 10^{-3}$
<i>Longitudinal, RF</i>		
f_{rev}	kHz	78.1
h		7560
voltage	MV	up to 60
<i>SR partition numbers</i>		
$J_x = 1 - \mathcal{D}$		≈ 1
J_y		1
$J_l = 2 + \mathcal{D}$		≈ 2

Optical functions

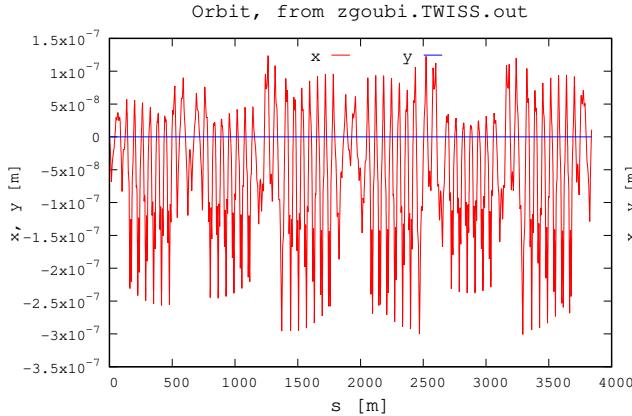


Figure 1: In the defect free lattice simulated here, the design orbit is zero around the ring.

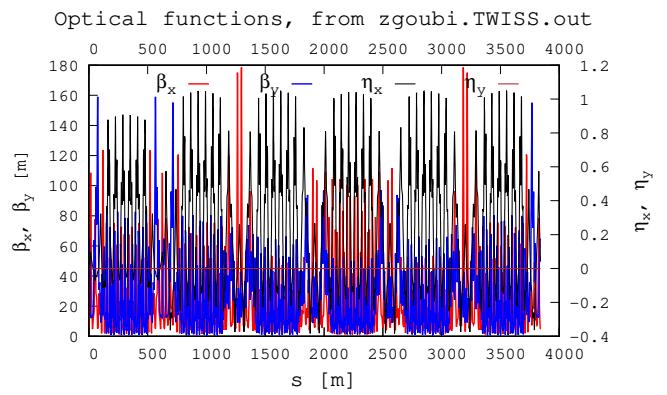


Figure 2: Betatron functions and dispersion.

Table 2: “Twiss file” header, from raytracing

@ LENGTH	3841.351355		
@ ALFA	0.4688745367E-03		
@ ORBITS5	-0		
@ GAMMATR	46.18188718		
@ Q1	0.8328968821		
@ Q2	0.7543490456		
@ DQ1	0.8333740361		
@ DQ2	-0.3950533812		
@ DXMAX	1.04806880E+00	@ DXMIN	-3.83664534E-01
@ DYMAX	0.00000000E+00	@ DYMINT	0.00000000E+00
@ XCOMAX	1.23786225E-05	@ XCOMIN	-3.00842877E-07
@ YCOMAX	0.00000000E+00	@ YCOMIN	0.00000000E+00
@ BETXMAX	1.78264978E+02	@ BETXMIN	1.15867478E+00
@ BETYMAX	1.59288020E+02	@ BETYMIN	7.66285809E-01
@ XCORMS	9.23721890E-08		
@ DXRMS	3.39655418E-01		
@ TITLE	"Zgoubi model"		

Table 3: SR statistics, from Monte Carlo tracking, 10,000 particles, one pass around the RCS

- 400 MeV:

```
* Monte Carlo S.R. statistics, from beginning of structure,
10000 particles, a total of 1009740000 integration steps
Average energy loss per particle per pass : 9.7434685E-03 keV.           Relative to initial energy : 2.4358671E-08
Critical energy of photons (average) : 4.4571211E-04 keV
Average energy of radiated photon : 1.8806917E-04 keV
rms energy of radiated photons : 3.4444217E-04 keV
Smallest, BIGEST photon : 7.2548E-18 9.9407E+03 keV
Number of photons radiated - Total : 518079.0
- per particle per pass : 51.80790
- per particle, per step : 5.1308159E-04
```

- 1 GeV:

```
* Monte Carlo S.R. statistics, from beginning of structure,
10000 particles, a total of 1009740000 integration steps :
Average energy loss per particle per pass : 0.3791386 keV.           Relative to initial energy : 3.7913857E-07
Critical energy of photons (average) : 6.9642578E-03 keV
Average energy of radiated photon : 2.9287155E-03 keV
rms energy of radiated photons : 5.3711990E-03 keV
Smallest, BIGEST photon : 5.8038E-17 9.9746E+03 keV
Number of photons radiated - Total : 1294556.
- per particle per pass : 129.4556
- per particle, per step : 1.2820687E-03
```

- 5 GeV:

```
* Monte Carlo S.R. statistics, from beginning of structure,
10000 particles, a total of 1009740000 integration steps :
Average energy loss per particle per pass : 236.7804 keV.           Relative to initial energy : 4.7356087E-05
Critical energy of photons (average) : 0.8706135 keV
Average energy of radiated photon : 0.3656743 keV
rms energy of radiated photons : 0.6709560 keV
Smallest, BIGEST photon : 0.0000E+00 9.9915E+03 keV
Number of photons radiated - Total : 6475173.
- per particle per pass : 647.5173
- per particle, per step : 6.4127132E-03
```

- 10 GeV:

```
* Monte Carlo S.R. statistics, from beginning of structure,
10000 particles, a total of 1009740000 integration steps :
Average energy loss per particle per pass : 3790.037 keV.           Relative to initial energy : 3.7900375E-04
Critical energy of photons (average) : 6.969458 keV
Average energy of radiated photon : 2.923548 keV
rms energy of radiated photons : 5.376011 keV
Smallest, BIGEST photon : 0.0000E+00 9.9915E+03 keV
Number of photons radiated - Total : 1.2963827E+07
- per particle per pass : 1296.383
- per particle, per step : 1.2838777E-02
```

- 18 GeV:

```
* Monte Carlo S.R. statistics, from beginning of structure,
10000 particles, a total of 1009740000 integration steps
Average energy loss per particle per pass : 39725.17 keV.           Relative to initial energy : 2.2069537E-03
Critical energy of photons (average) : 40.79130 keV
Average energy of radiated photon : 16.93466 keV
rms energy of radiated photons : 31.27895 keV
Smallest, BIGEST photon : 0.0000E+00 9.9915E+03 keV
Number of photons radiated - Total : 2.3457908E+07
- per particle per pass : 2345.791
- per particle, per step : 2.3231632E-02
```

A summary of SR statistics data

Table 4 summarizes some of the statistics outcome detailed in page 5, as resulting from Monte Carlo SR simulation. Theoretical data are included for comparison.

Table 4: Summary of SR statistic data, from Monte Carlo tracking, 10,000 particles, one pass around the RCS. Curvature radius in tracking trials is $\rho = 235$ m (Tab 1). Theoretical values are given for comparison.

Energy (E_s)	(GeV)	0.4	1	5	10	18
SR loss (U_s) theory ^(a)	(MeV/turn)	9.74×10^{-6} 9.63×10^{-6}	3.79×10^{-4} 3.74×10^{-4}	0.2368 0.2352	3.790 3.764	39.725 39.517
damping time (E_s/U_s)	(turn)	41×10^6	2.64×10^6	21116	2642	453
rms energy loss theory ^(b)	(keV)	3.44×10^{-4} 3.38×10^{-4}	5.37×10^{-3} 5.28×10^{-3}	0.671 0.660	5.376 5.278	31.28 30.78

(a) Theor. $U_s = C_\gamma E_s^4/\rho = 88.46276 \times E_{s[GeV]}^4/\rho[m]$.

(b) Theor. rms energy loss = $\frac{\sqrt{211}}{15\sqrt{3}}\epsilon_c$, ϵ_c = energy of critical photon = $\frac{3}{2} \frac{\hbar\gamma^3 c}{\rho e}$.

Equilibrium quantities at 18 GeV

Values of equilibrium quantities in the “theory” columns, Table below, are derived from SR integrals. Values in the “tracking” column are from Monte Carlo SR, 2,000 particles tracked over 2700 turns (about 6 damping times). ESR data are included for comparison.

The difference in the theoretical horizontal equilibrium emittances, between ESR and RCS, results from the difference in I_5/I_2 .

	ESR theory	RCS		SR integrals
		theory	tracking	
		Equilibrium quantities		
I1	1.82434	1.82434		
I2	0.02489	0.026737		
I3	1.0150e-4	1.137743e-4		
I4	≈ 0	3.3e-5		
I5	4.23E-06	7.38e-6		

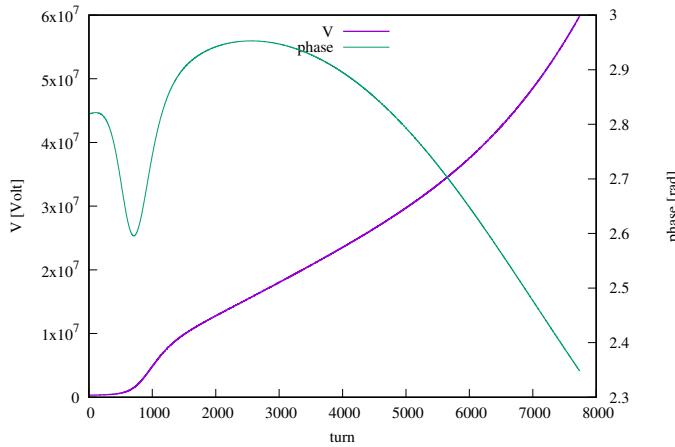
3 Simulation Hypotheses: RF, Phase Space, Spin

RF Ramp

- All the RF is located at RFCA1 ($s=1204$ m), rather than split over the 4 RFCA stations. It has been checked that this makes no difference on beam and spin dynamics over the acceleration cycle. It makes no difference either, to locate the RF at an end of the ring sequence instead.

Voltage and phase ramps are pre-calculated (Fig. 3). During tracking they are read from a dedicated log file.

This RF ramp is undergoing optimization, essentially in order to reduce losses (which are small anyway, here), results derived here are preliminary, however they produce the bulk of the behavior.



“CAVITE” input data: the RF is concatenated at station RFCA1 (located at $s=1240$ m).
RF program is read from a pre-computed ancillary file.

```
'CAVITE' accelCav_1
11 EICRCS_File      ! Cavity option 11(allows double-frequency, SR compensation).
3841.351268 7560   ! Circumference; harmonic number.
7.5E6 3.08 0. 1204.80 ! Voltage and RF phase not used, due to above EICRCS_File,
! indicating that they are read from zgoubi.RFLaw.In.
```

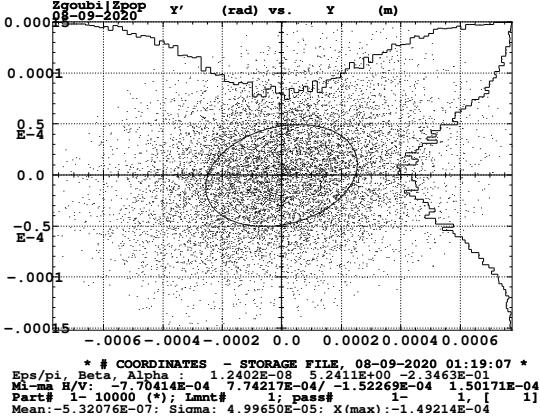
Figure 3: RF voltage and synchronous phase ramps.

- For the record: head and tail of the ancillary RF program file used in the present simulations:

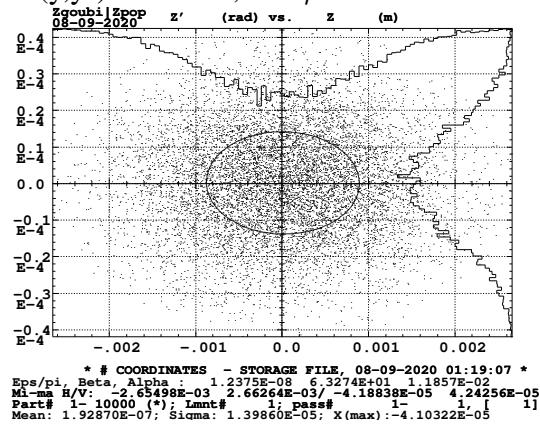
Turn	Energy (GeV)	Bunch Length (s)	Voltage (V)	Phase (rad)	1/Qs	time (s)	Qs	
1	1.0001035203394717e9	1.8028926548975248e-10	327539.3324794361	0.3227807532258099	75.66945204877118	0.00001281336860382258	0.013215372556886902	
2	1.0002070971351715e9	1.802620090722254e-10	327667.9795979095	0.32274077460969236	75.65800346777236	0.00002562673720764516	0.013217372309143272	
3	1.0003107310649942e9	1.802346291266711e-10	327797.1788409724	0.322700919749387	75.64650304121196	0.00003844010581146774	0.013219381726809016	
4	1.0004144228140453e9	1.802071251560068e-10	327926.9333388347	0.3226614078970054	75.63495056042323	0.00005125347441529032	0.013221400854901337	
5	1.0005181730747123e9	1.8017949666175083e-10	328057.2462205613	0.3226220249736046	75.6233458161519	0.0000640668430191129	0.013223429738629952	
.....	
7733	1.808993e10	6.600000000000004e-11	5.974381116086878e7	0.792380890938422	27.685530783648293	0.09908577941336001	0.03611995044684579	
7734	1.809214e10	6.600000000000004e-11	5.976144556333635e7	0.7925586218453715	27.685530772106933	0.09909859278196384	0.036119950461903236	
7735	1.809435e10	6.600000000000004e-11	5.9779086848687515e7	0.7927291388101053	27.68553076056979	0.09911140615056765	0.036119950476955175	
7736	1.809656e10	6.600000000000004e-11	5.9796735019235194e7	0.7928996399687998	27.685530749036875	0.09912421951917148	0.03611995049200160	
7737	1.809877e10	6.600000000000004e-11	5.9814390077292405e7	0.7930701253022269	27.6855307375082	0.09913703288777531	0.0361199505070425	
7738	1.810098e10	6.600000000000004e-11	5.983205202517209e7	0.7932405947911686	27.685530725983725	0.09914984625637913	0.036119950522077914	

Initial Phase Space, 1 GeV

(x,x') Gaussian, 26 $\pi/\mu\text{m}$ normalized



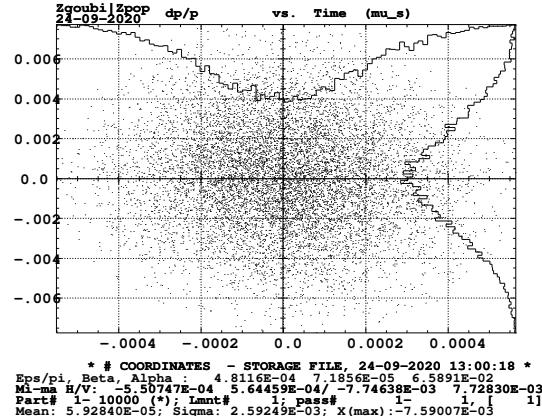
(y,y') Gaussian, 26 $\pi/\mu\text{m}$ normalized



- Initial Gaussian 6D phase space, input data:

```
'MCOBJET'
3.3366646935164153E+03      ! 1GeV, beta*gamma    1957.551806
3
10000
2 2 2 2 2 2
0. 0. 0. 0. 0. 1.
-0.232183 5.276444 1.3e-8 3. ! H beam parameters here. epsilon/pi=1.3e-8.
0.018529 64.157433 1.3e-8 3. ! V beam parameters here. epsilon/pi=1.3e-8.
0. 21.6 150e-6 3.           ! long. beam parameters here.
123456 234567 345678
```

Longitudinal (time-dp/p)
 $\text{rms } \sigma_{\delta E/E} = 2.592 \times 10^{-3}$,
 $\text{rms } \sigma_\delta t = 185.941 \text{ ps}$



◇ An excerpt from the output “.res” data file, corresponding to the graphs above, details 1 GeV initial bunch characteristics:

```
----- Concentration ellipses :
surface/pi          alpha        beta      <X>      <XP>      numb. of prtcls      ratio      space      pass#
                                         in ellips, out
1.2401E-08 [m.rad]   -2.3463E-01  5.2415E+00  -1.419431E-06  -5.320063E-07  10000     7835  0.7835  (Y,T)      2
1.2374E-08 [m.rad]   1.1856E-02   6.3279E+01   8.925807E-06  1.928701E-07  10000     7874  0.7874  (Z,P)      2
4.8116E-04 [mu_s.MeV] 6.5891E-02   7.1856E-05  2.182283E-06  9.998553E+02  10000     7811  0.7811  (t,K)      2

(Y,T) space (units : m, rad ) :
sigma_Y = sqrt(surface/pi * beta) =  2.549495E-04
sigma_T = sqrt(surface/pi * (1+alpha^2)/beta) =  4.996104E-05

(Z,P) space (units : m, rad ) :
sigma_Z = sqrt(surface/pi * beta) =  8.848836E-04
sigma_P = sqrt(surface/pi * (1+alpha^2)/beta) =  1.398487E-05

(t,K) space (units : mu_s, MeV) :
sigma_t = sqrt(surface/pi * beta) =  1.859411E-04
sigma_K = sqrt(surface/pi * (1+alpha^2)/beta) =  2.593287E+00

Beam sigma matrix and determinants :

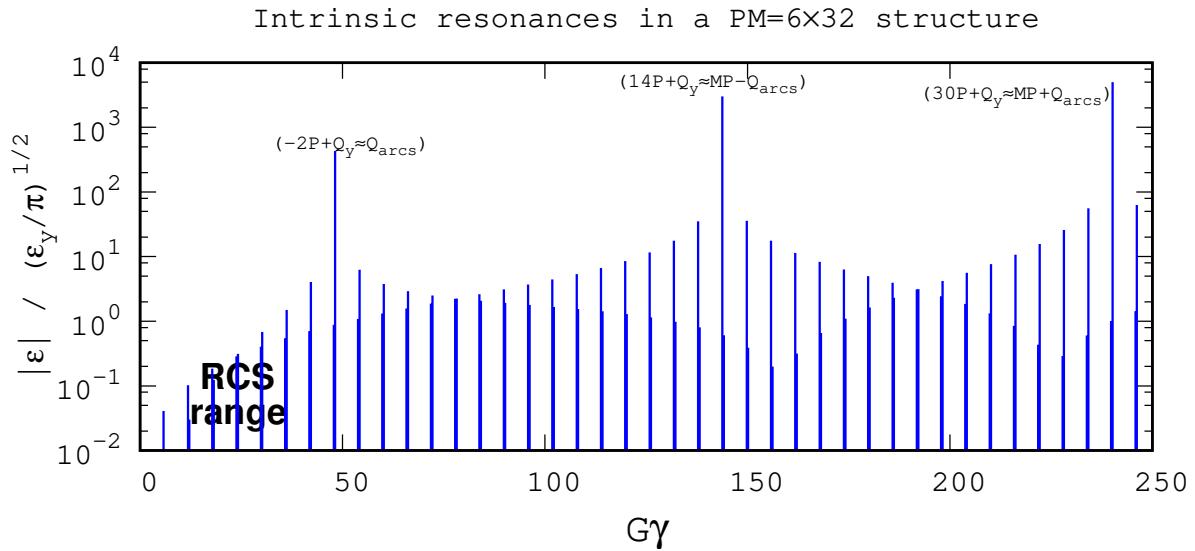
6.499922E-08  2.909594E-09  -2.187532E-09  4.342228E-12
2.909594E-09  2.496105E-09  5.959756E-10  3.056553E-12
-2.187532E-09 5.959756E-10  7.830190E-07  -1.467025E-10
4.342228E-12  3.056553E-12  -1.467025E-10  1.955765E-10

sqrt(det_Y), sqrt(det_Z) :  1.240077E-08  1.237411E-08  (Note : sqrt(determinant) = ellipse surface / pi)
normalized (*beta*gamma) :  2.427516E-05  2.422296E-05
```

Spin

All spins are launched vertical in these simulations. The vertical orbit is zero (no orbit defect included) (Fig. 1), so integer resonances are ineffective.

Several intrinsic resonances are crossed over an acceleration range $E : 400 \text{ MeV} \rightarrow 18 \text{ GeV}$ ($G\gamma : 0.9 \rightarrow 40.8$), with typical strength landscape as in the figure below: due to the lattice symmetries, all intrinsic resonances in the RCS energy range have negligible strength (theoretically, zero), and imperfection resonance strengths are minimized [1].



4 Acceleration From 1 to 18 GeV in 7738 Turns

These results are from a 1,000 particle tracking. Given this number, statistics is not that accurate, however it yields the bulk of the behavior, further refinements will be dealt with on NERSC computers.

The transmission here is 929/1000, these 71 particles are lost during the first 233 turns. Note that optimization of the ramp is on-going at this stage, toward getting closer to zero loss.

Figure 4 displays the evolution of various parameters along the acceleration cycle (a 30 particle sample, taken from the 1,000 tracked). The horizontal emittance grows from about turn 3000 (upper right plot, below), toward its equilibrium value, which is greater than the value attained during the ramp (Tab. 6); as a matter of fact:

- the horizontal emittance damping time is $\tau_x \approx 450$ turns (Tab. 4),
- betatron damping time constant is n [turns] such that emittance(n)=emittance(0)/e, thus $n \approx (1-1/e) \times E/\Delta E$; taking $E = 18 \times 10^9$ eV, $\Delta E = 18 \times 10^9 / 8000 = 2.25 \times 10^6$ eV/turn, that gives in the 18 GeV region $n = (1-1/e) * 8000 \approx 5000$ turns
- 450 turns versus 5000, so SR dominates, the acceleration rate ΔE does not allow betatron damping to compensate SR growth.

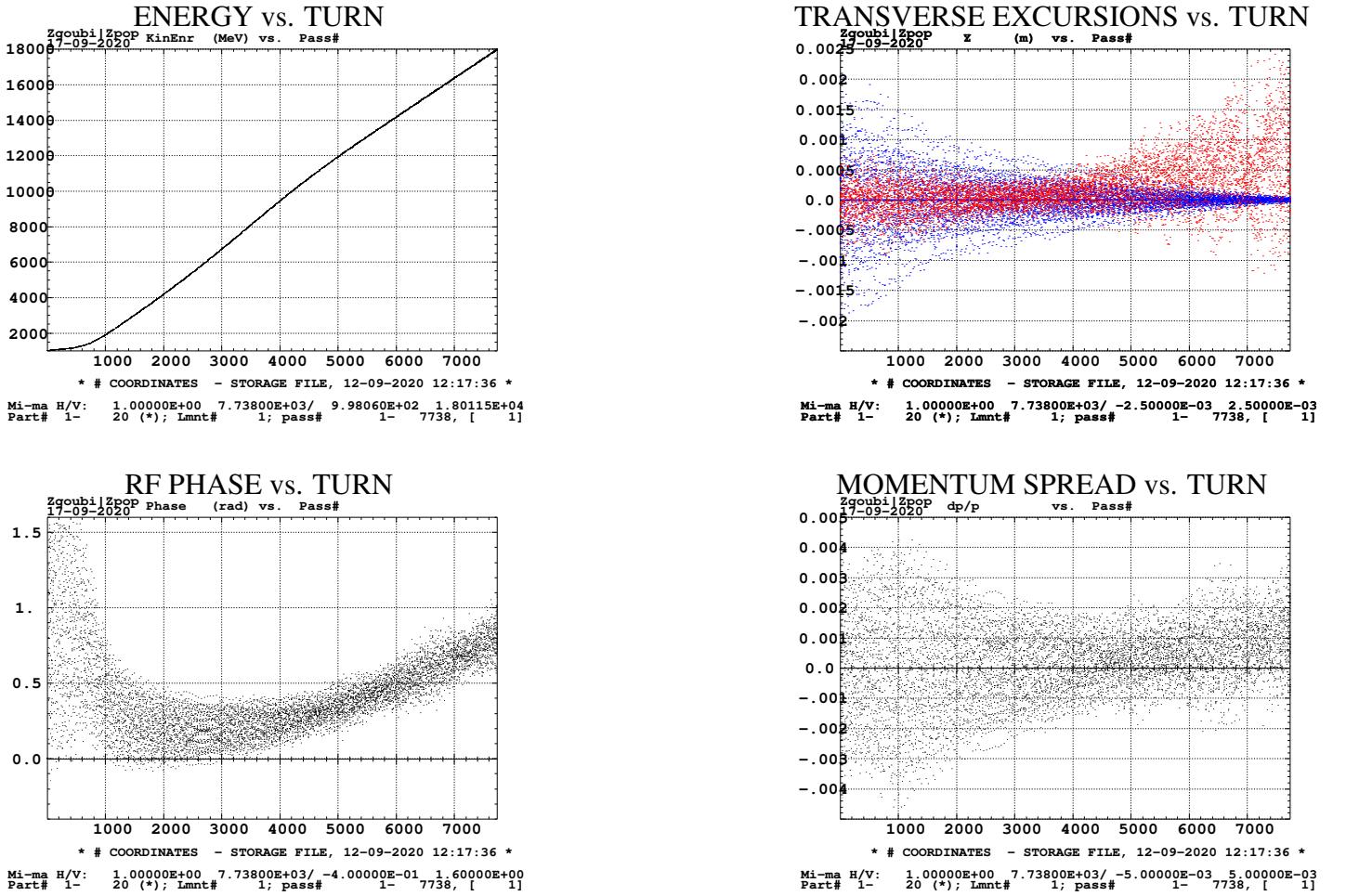


Figure 4: Dynamics during the ramp, 1,000 particle bunch, 1 to 18 GeV. Phase-space plots at the end of acceleration cycle are displayed in p. 11.

5 Final Bunch Densities; Spin

Table 5 summarizes SR statistics data over the acceleration ramp. Final phase spaces are given in Fig. 5.

Table 5: SR statistics over the acceleration ramp, from 1 to 18 GeV. Monte Carlo tracking, 1,000 particles, 7738 turns

```
* Monte Carlo S.R. statistics, from beginning of structure, on
steps :
Average energy loss per particle per pass : 7018.248 keV.
Average energy of radiated photon : 6.992134 keV.
rms energy of radiated photons : 16.78377 keV.
Smallest, BIGEST photon : 0.0000E+00 9.9831E+03 keV.
Number of photons radiated - Total : 7.7679044E+09
- per particle per pass : 1003.735
```

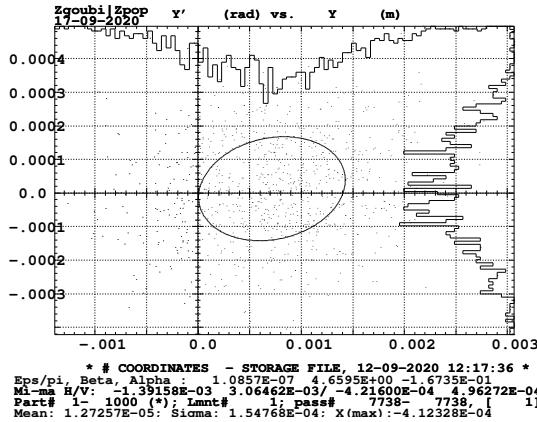
1000 particles, a total of -196351350 integration

Relative to initial energy : 7.0160943E-03

TRANSVERSE HORIZONTAL

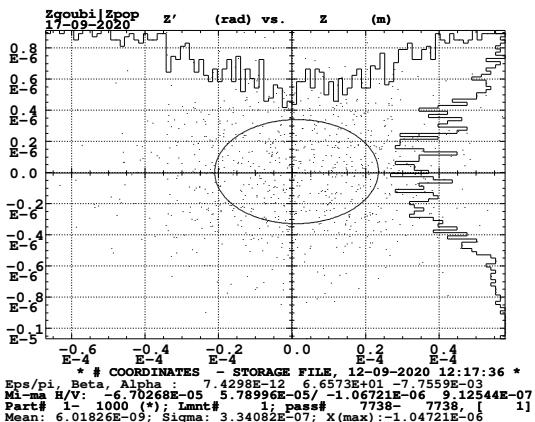
$$\text{rms } \epsilon_x/\pi = 108.6 \text{ nm}$$

$$\beta\gamma\epsilon_x/\pi = 3.83 \text{ mm}$$



TRANSVERSE VERTICAL

$$\epsilon_y/\pi = 7.4 \times 10^{-3} \text{ nm}$$



LONGITUDINAL (phase-dp/p)

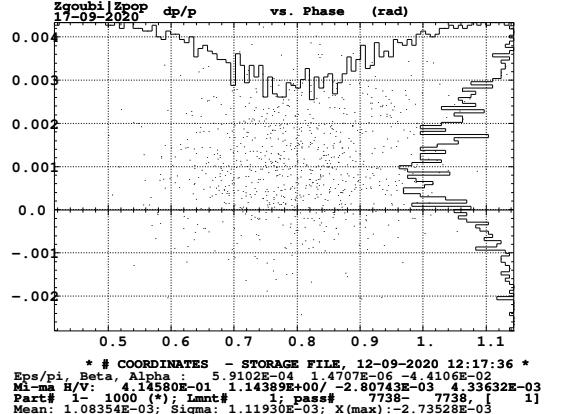
$$<\delta p/p> = 1.08354 \times 10^{-3},$$

$$\sigma_{\delta p/p} = 1.1193 \times 10^{-3}$$

$$<\phi> = 0.7984802 \text{ rad},$$

$$\sigma_{\delta\phi} = 0.1098435 \text{ rad} \xrightarrow{\hbar\omega_{\text{rev}}} \sigma_{\delta t} = 29.61 \text{ ps}$$

$$\Delta\phi = 0.72930858 \longrightarrow \Delta t = 196.6 \text{ ps}$$



Note: RF parameters above stem from CAVITE data (page 7), namely,

$$f_{\text{rev}} = c/3841.35 = 78.1 \text{ kHz}, h = 7560$$

$$< E > = 17.9076 \text{ GeV}, \sigma_E = 20.0661 \text{ MeV}$$

Figure 5: Final phase spaces, after acceleration from 1 to 18 GeV.

Recap: SR Parameters at 18 GeV, on the Ramp

Equilibrium data are added, for comparison.

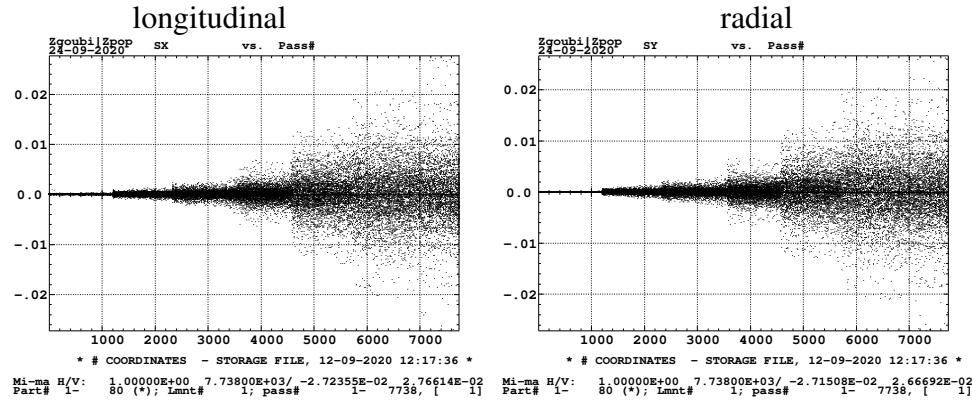
Table 6: Equilibrium emittances.

		– At equilibrium –		On the ramp	
		ESR theory	RCS theory	RCS tracking	tracking
ϵ_y/π	pm			0	7
$\gamma\epsilon_x/\pi$	mm	2.85	4.61	4.2	3.83
ϵ_x/π	nm	81	131	120	109
ϵ_l/π	$\mu\text{eV.s}$		≈ 400	363	591

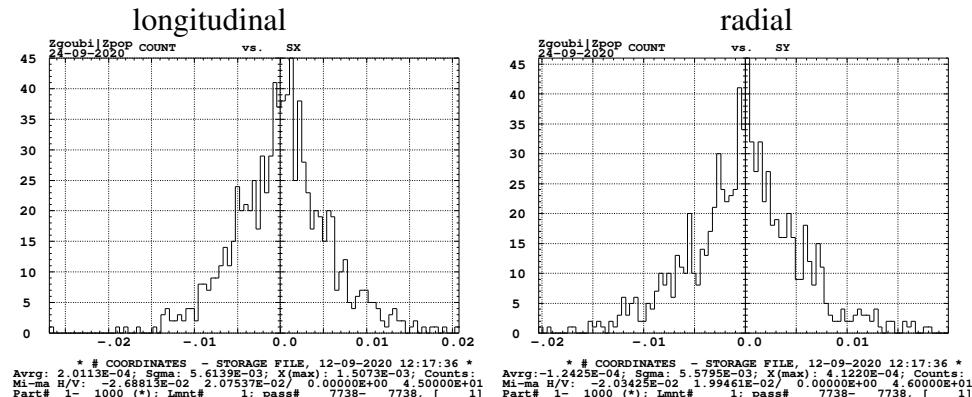
Spin

Resonance strengths are weak enough (page 9) that, in this perfectly aligned ring simulations, the rms spin tilt from vertical over the acceleration range is less than 10 mrad, figures below.

Evolution of horizontal spin components over 7738 turns (50 particle sample):



Horizontal spin component densities at 18 GeV, turn 7738, 1,000 particles:



References

- [1] Electron-Ion Conceptual Design Report.
<https://brookhavenlab.sharepoint.com/sites/eRHIC/cdr2020/Summary%20%20Status/Forms/AllItems.aspx?CT=1600103406774&OR=OWA%2DNT&CID=ec55f32b%2D0f57%2Dc5bb%2Dd8ab%2D2fa2b8df89f8&id=%2Fsites%2FeRHIC%2Fcdr2020%2FSummary%20%20Status%2FEIC%5FCDR%5FDraft%2Epdf&parent=%2Fsites%2FeRHIC%2Fcdr2020%2FSummary%20%20Status>
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